

**NED University of Engineering and Technology**  
**Feedback Control System (EE-374)**  
**(CEP)**

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**Section: F**

**Batch: 2018**

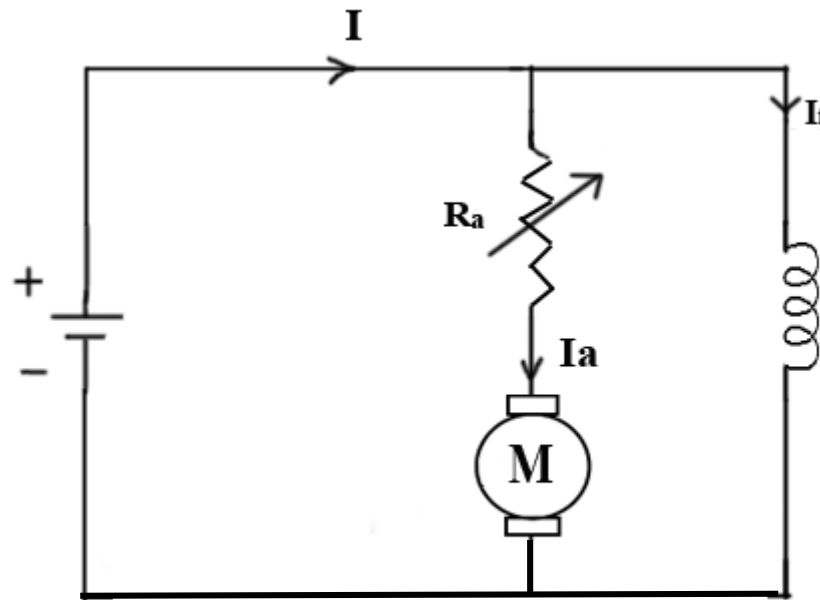
**Electrical Engineering Department**

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## Introduction:

While both A.C. and D.C. motors serve the same function of converting electrical energy into mechanical energy, they are powered, constructed and controlled differently [1]. D.C. motors are powered from direct current (D.C.), such as batteries, D.C. power supplies or an AC-to-DC power converter as opposed to AC motors. Brushes and a commutator are used in D.C winding field motors, which contribute to the maintenance, limit the speed, and lower the life expectancy of brushed D.C. motors. The speed of a D.C. motor is controlled by varying the armature winding's current while the speed of an A.C. motor is controlled by varying the frequency, which is commonly done with an adjustable frequency drive control [2]. Thus, the armature control method is exactly what we have used for our complex engineering problem. To understand how the armature controls the speed of the motor we will take a simple electrical circuit as shown below,



As clearly visible in the above diagram, Speed of a dc motor is directly proportional to the back emf  $E_b$  and  $E_b = V - I_a R_a$ . That is, if the supply voltage  $V$  and armature resistance  $R_a$  are constant, the speed is proportional to the armature current  $I_a$ . As a result, when we add resistance in series with the armature,  $I_a$  lowers, and the speed decreases as well. The lower the speed, the larger the resistance in series with the armature. The method explained above is put action in this problem and the results are illustrated in this report. The problem has been completed while keeping in mind of all the tasks that are required, some were optional while others were compulsory thus were held of utmost importance. From graphical representation to bode plots, the complete analysis of the problem has been performed. The coding was written on Arduino and the program was easily initiated in the hardware. Lastly we have presented our results in tables, graphs and wordings for all the analysis performed throughout the problem solving.

## Objective:

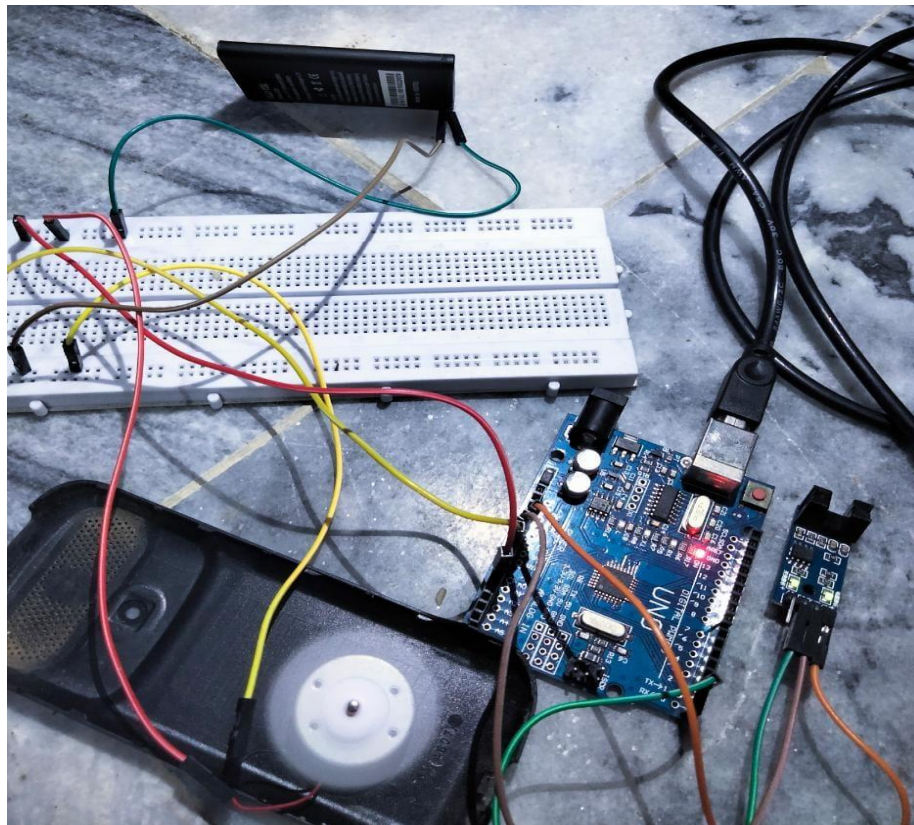
DC motor control for two methods

1. Armature control method
2. Field control method

Tasks:

- 1) Identify physical parameters (for example via system Identification toolbox on MATLAB or via step response method etc.)
- 2) Convert the motor differential equation into Laplace transform (Transfer function)
- 3) Plot or obtain different stable responses studied in FCS by adding a control parameter.
- 4) Apply Routh Criteria and find the range of stability for motor speed control.
- 5) Plot root locus indicating the all the responses.
- 6) Add gears at the shaft of the motor to control different speed levels and repeat above exercises (Bonus Marks)
- 7) Plot bode plot (Bonus Marks)
- 8) And any other analysis you learnt etc. (Bonus Marks)

Hardware:



## Components,

- Speed sensor
- Arduino UNO
- Breadboard
- Jumpers (for connection)
- 3.8 V Battery (for input voltage)
- DC motor

## Arduino:

### Code,

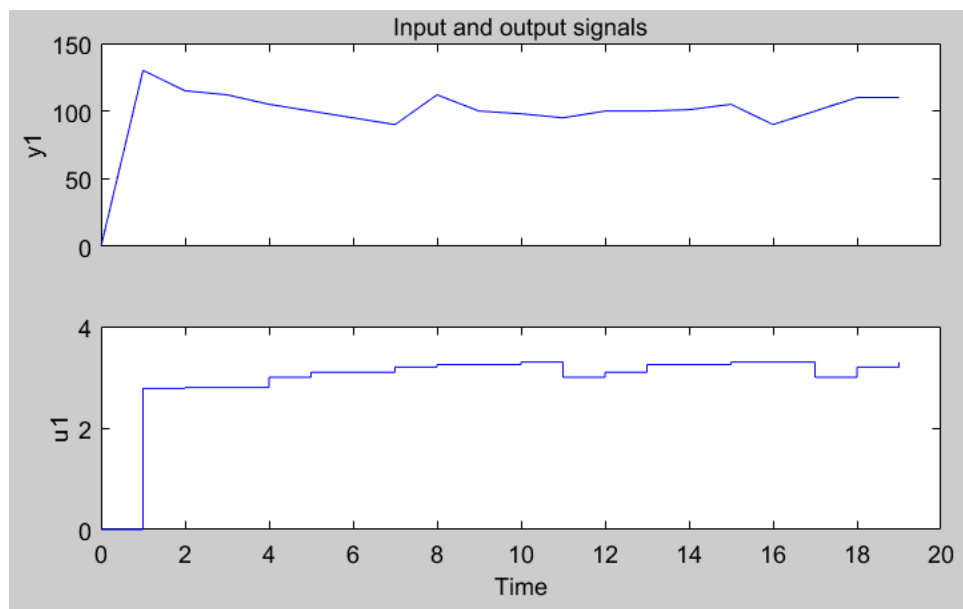
```
int encoder_pin = 2;
int analog_pin = A0;
int rpm = 0;
float velocity = 0;
float voltage = 0.0;
volatile byte pulses = 0;
unsigned long timeold = 0;
unsigned int pulsesperturn = 20;
const int wheel_diameter = 64;
static volatile unsigned long debounce = 0;
void setup() {
  Serial.begin(9600);
  pinMode(encoder_pin, INPUT);
  pinMode(analog_pin, INPUT);
  attachInterrupt(0, counter, RISING);
  pulses = 0;
  rpm = 0;
  timeold = 0;
  voltage = 0;
  Serial.print("Seconds ");
  Serial.print("RPM ");
  Serial.print("Pulses ");
  Serial.print("voltage ");
  Serial.println("velocity[km/h]");
}
void loop() {
  if (millis() - timeold >= 1000)
  {
    noInterrupts();
    rpm = (60 * 1000 / pulsesperturn) / (millis() - timeold) * pulses;
    voltage = analogRead(A0);
    velocity = rpm * 3.1416 * wheel_diameter * 60 / 1000000;
    timeold = millis();
    Serial.print(millis() / 1000); Serial.print(" ");
    Serial.print(rpm, DEC); Serial.print(" ");
    Serial.print(pulses, DEC); Serial.print(" ");
    Serial.print(voltage/266, 2); Serial.print(" ");
    Serial.println(velocity, 2);
    pulses = 0;
    interrupts();
  }
}

void counter() {
  if ( digitalRead (encoder_pin) && (micros() - debounce > 500) && digitalRead (encoder_pin) ) {
    debounce = micros();
    pulses++;
  }
  else ;
}
```

Readings Obtained,

Time/s	Voltage/V	Speed
0	0	0
1	2.78	130
2	2.8	115
3	2.8	112
4	3	105
5	3.1	100
6	3.1	95
7	3.2	90
8	3.25	112
9	3.25	100
10	3.3	98
11	3	95
12	3.1	100
13	3.25	100
14	3.25	101
15	3.3	105
16	3.3	90
17	3	100
18	3.2	110
19	3.3	110

Graphical representation of Speed and Voltage:



**Task 1:**

(Optional)

**Task 2:**

Convert the motor differential equation into Laplace transform (Transfer function)

Response,

Model name:	<input type="text" value="tf1"/>
Color:	<input type="text" value="[0,0,1]"/>

From input "u1" to output "y1":  
30.37  
-----  
 $s^2 + 3.211 s + 0.9592$   
Name: tf1  
Continuous-time identified transfer function.

Diary and Notes

```
% Import    mydata

% Transfer function estimation
Options = tfestOptions;
Options.Display = 'on';
Options.WeightingFilter = [];

tf1 = tfest(mydata, 2, 0, Options)
```

Show in LTI Viewer

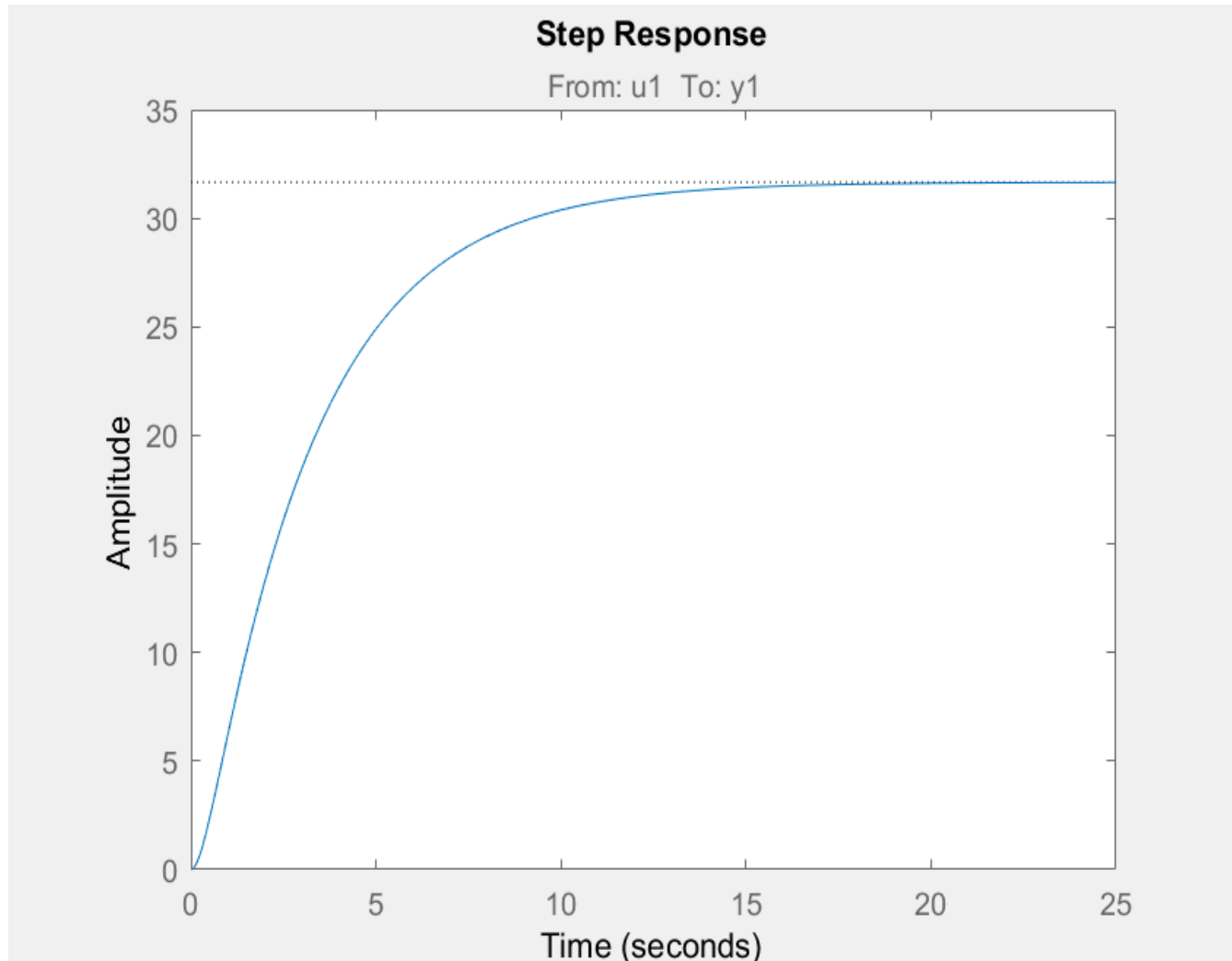
Present      Export      Close      Help

### Task 3:

Plot or obtain different stable responses studied in FCS by adding a control parameter.

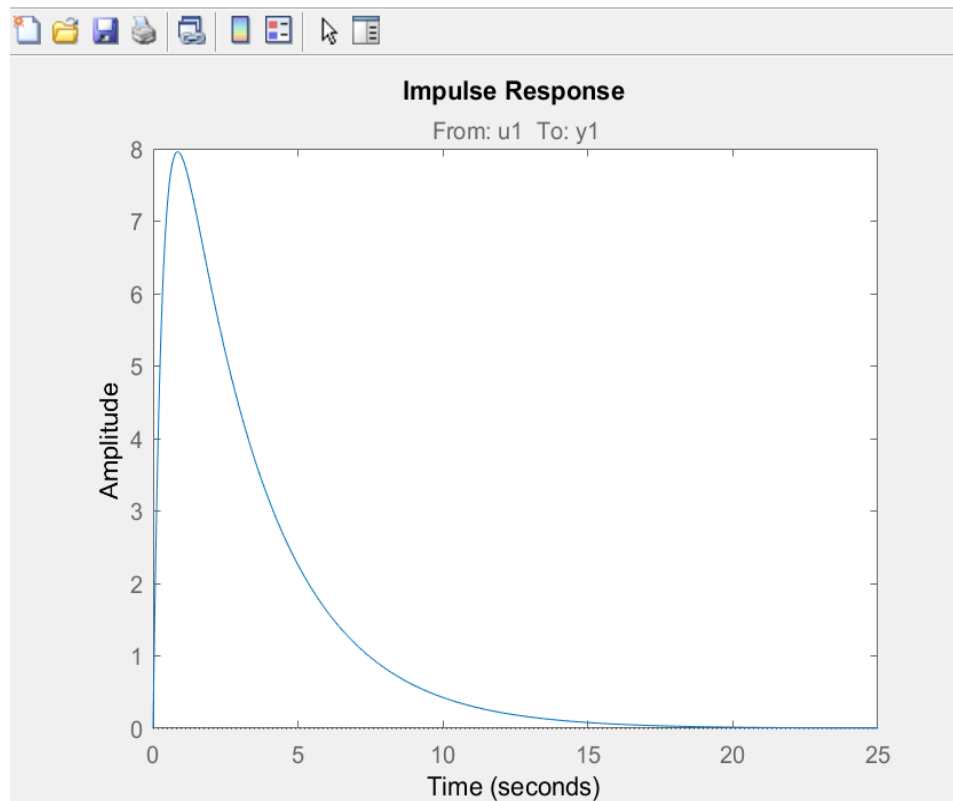
#### Response,

Below is an image of the step response graph, the graph is a curve and not a straight line. For step input, only gain  $K_p$  will exist and rest  $K_v$  and  $K_a$  will become zero for the step input. The graph rises to a peak value of 32 after 15 seconds and that peak value is maintained throughout the passage of time.

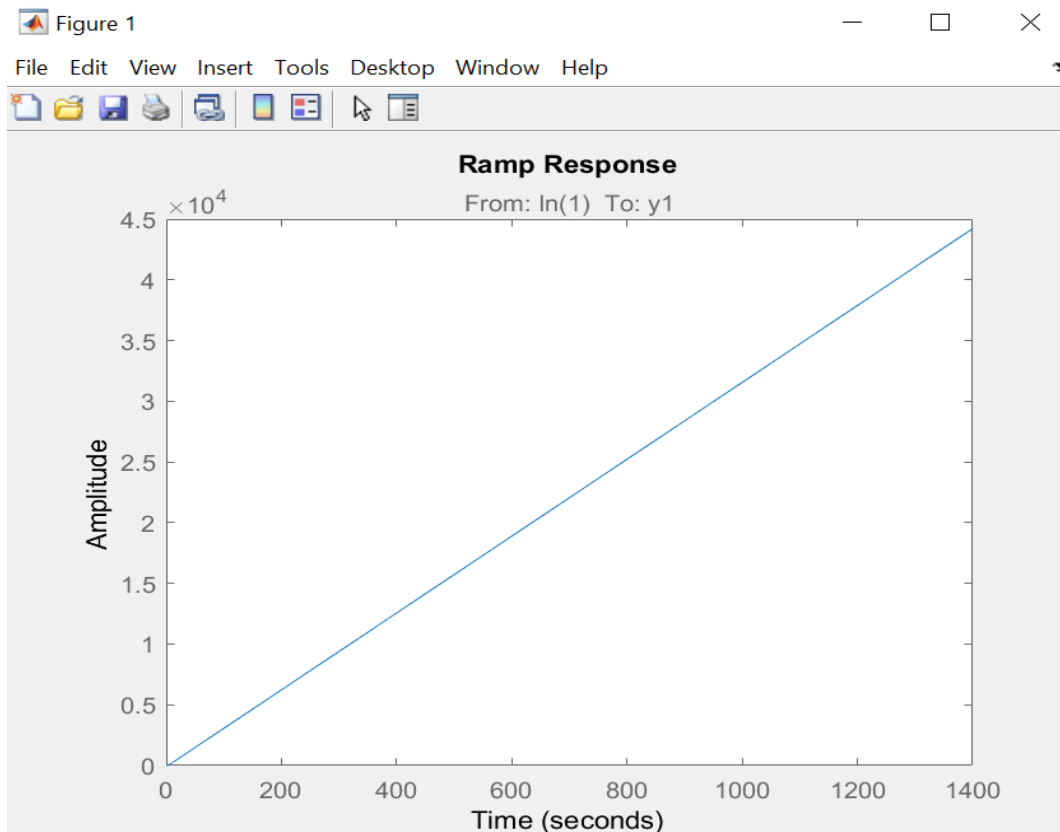


Below is an image of the impulse response graph, the graph is a curve and not a straight line. The graph rises to a peak value of 8 after 1 second and that peak value instantly starts dropping until it reaches completely zero after 19 seconds, reaching completely zero at 20 seconds.





Below is the ramp response. For this, only  $K_v$  gain will exist and rest  $K_a$  will be zero and  $K_p$  will be infinite.



## Task 4:

Apply Routh Criteria and find the range of stability for motor speed control.

Response,

TRANSFER FUNCTION ::

$$\frac{C(s)}{R(s)} = \frac{30.37}{s^2 + 3.211s + 0.9592}$$

∴

$$s^2 + 3.211s + 0.9592 = 0 \quad (\text{Characteristic Equation})$$

$s^2$	1	0.9592
$s^1$	3.211	0
$s^0$	0.9592	0

$$\boxed{s_1 = -0.33} \quad , \quad \boxed{s_2 = -2.87}$$

As there is no sign change it means that all the roots are on left side of s-plane  
Thus system is stable.

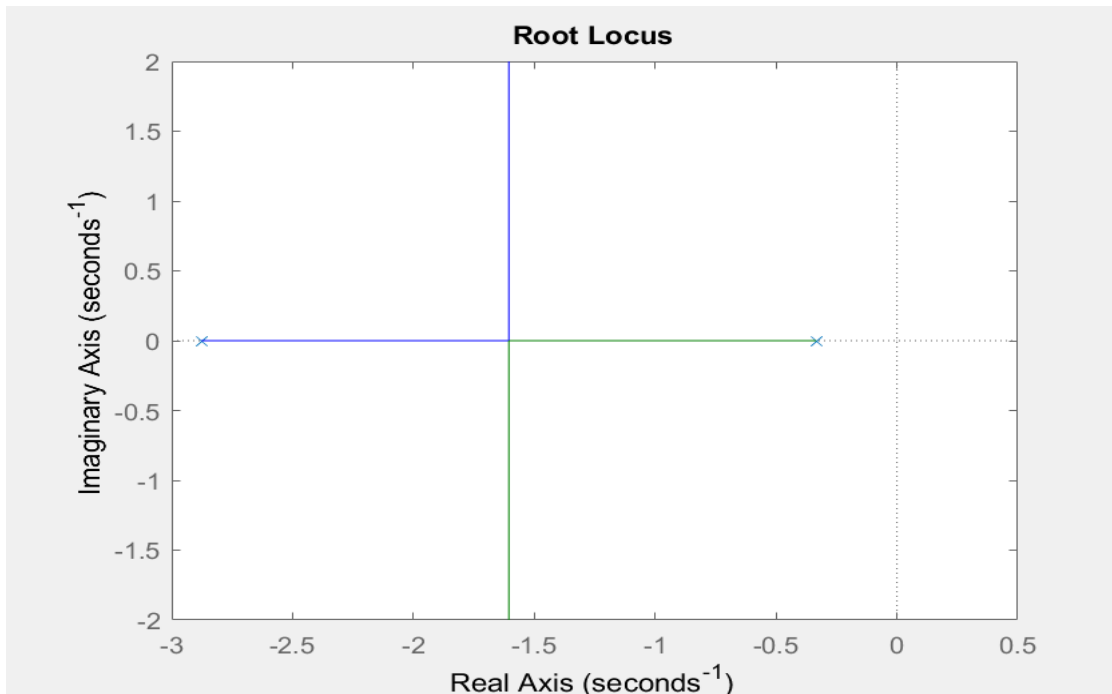
As system roots are found to be -0.33 and -2.87 respectively so the stability is observed to lie between these mentioned roots.

## Task 5:

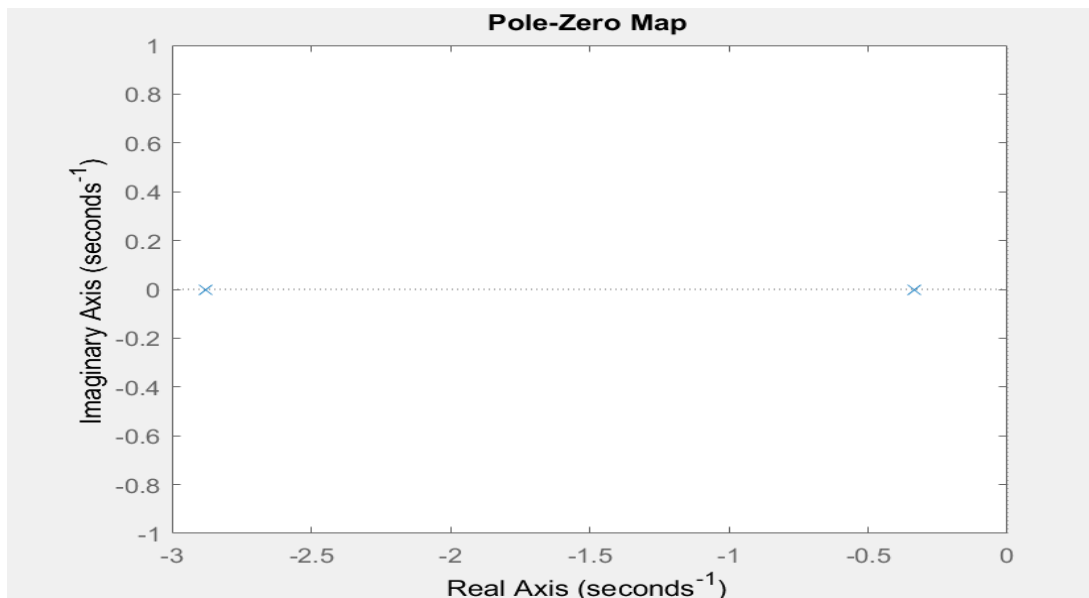
Plot root locus indicating the all the responses.

Response,

The root locus plot below shows us the responses on a concise plot with an imaginary and a real axis. We found two poles at -0.3 and -2.9 on real or sigma axis respectively.



In the below graph of pole zero we are again shown to have two poles on the plot with the points -2.9 and -0.3 on sigma axis respectively.

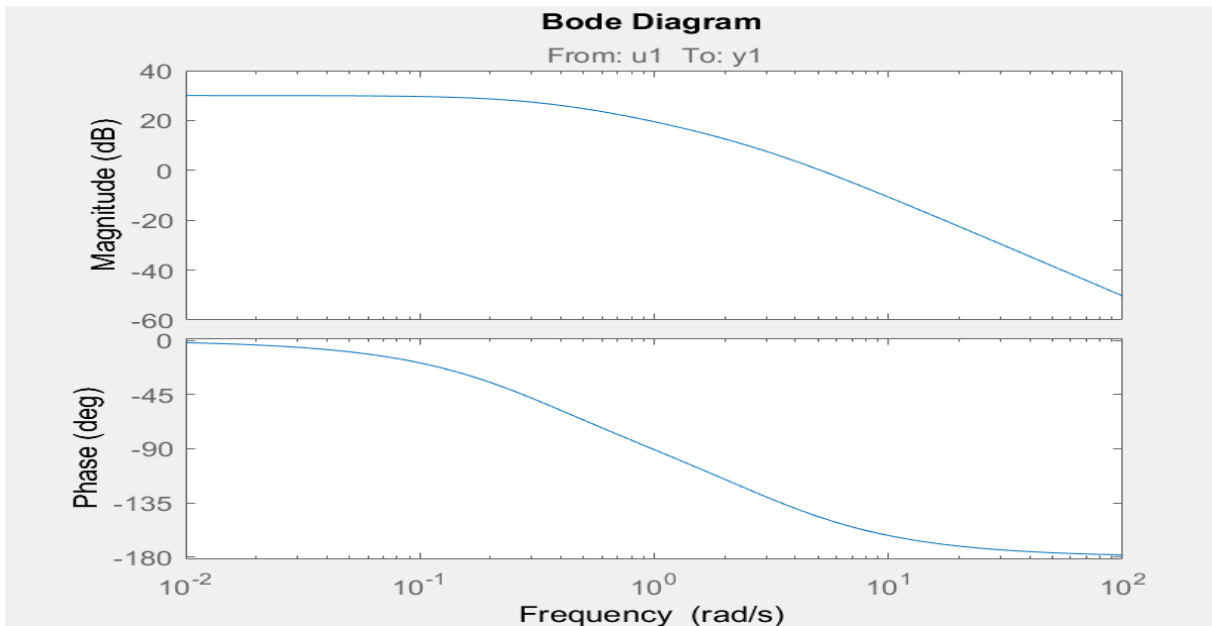


**Task 6:**

(Optional)

**Task 7:**

Plot bode plot (Bonus Marks)



As visible above in fig.1, the Bode diagram has been issued showing, magnitude with respect to the frequency and phase with respect to the frequency.

**Conclusion:**

We controlled the speed of the DC motor using the armature control method. While doing so we used all the theoretical and analytical methods taught to us in FCS to complete the tasks provided. We found out the transfer function, plotted different response graphs. Like the step, ramp and impulse response graphs. In order to check the stability of our motor, we also applied the Routh criteria. Leading us to the conclusion that our motor is indeed stable. The range for its stability was also found out and shown by the root locus.

This complete complex engineering problem is in fact our practical implementation of all the theoretical studies made in FCS. From solving the mathematical models of systems to determining the transfer functions and from constructing differential equations to checking the stability of the feedback control system. These analyses of the DC motor have trained us to the point where we now know how to properly analyze a system in order to optimize it. All the tasks provided below completed single but important parts of the project helping us to understand the importance of feedback in any system. We have implemented many techniques that have helped us deeply understand the depths and importance of feedback control systems in our daily engineering lives.

## References:

[1] Saeed Niku. Introduction to Robotics: Analysis, Control, Applications. 2nd ed. John Wiley & Sons, Inc., 2011. Page 280.

[2] Robert S. Carrow. Electrician's technical reference: Variable frequency drives. Delmar Thomson Learning, 2001. Page 45.