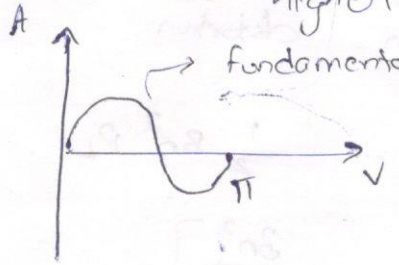
Harmonic :- It deals with waves with particular periodic waves. It is generally employed in music and acoustics, electronic power transmission, radio technology.

distortion :- This refers to disturbance in waves

As we know it is applied to repeating waves or signals, such as sin, cosine waves. A harmonic of such a wave is a wave with the freq that is the integral multiple of frequency of the orginal wave, known as fundamental frequency

* The orignal wave is the first harmonic, the following harmonics are higher harmonics.




How this harmonics Related to (Electrical power)

Harmonic voltages & current is an Elt power system are a result of non-linear Elt loads. Harmonic freq in the power grid are a freq cause of power quality problems. Harmonic in power system result in increased heating in the equipment and conductors, misfiring in variable speed drives, and torque pulsation in motors. Reduction of harmonic is considered desirable.

Power o/p due to distortion

$P_{ac} = V \cdot I$ $\qquad V = iR$

$= \frac{I_m V_m}{2}$ $\qquad V_m = i_m R_L$

$P_{ac} = \frac{I_m^2 R_L}{2}$

$I_m$ = Peak value of the o/p current

$= \frac{I_{pp}}{2} = \frac{I_{max} - I_{min}}{2}$

$B_1 = \frac{I_{max} - I_{min}}{2}$

$I_m = B_1$

$$\boxed{P_{ac} = \tfrac{1}{2} B_1^2 R_L}$$

Hence o/p power with harmonic distortion

$(P_{ac})_D = \frac{1}{2} B_1^2 R_L + \frac{1}{2} B_2^2 R_L + \cdots \frac{1}{2} B_n^2 R_L$

$= \frac{1}{2} B_1^2 R_L \left[ 1 + \frac{B_2^2}{B_1^2} + \frac{B_3^2}{B_1^2} + \cdots \frac{B_n^2}{B_1^2} \right]$

$(P_{ac})_D = P_{ac} [ 1 + D_2^2 + D_3^2 + \cdots D_n^2 ]$

$D^2 = D_2^2 + D_3^2 + \cdots + D_n^2$

$(P_{ac})_D = P_{ac} [ 1 + D^2 )$

If the total harmonic distortion $D = 0.15$

$(P_{ac})_D = P_{ac} [ 1 + (0.15)^2 ]$

$= 1.0225 P_{ac}$

So that is 2.25 % increase in the power given to the load.

$B_1, B_2, B_3$ and $B_4$ are the Amp of the fundamental, second 3rd & 4th harmonic components.

| | | |
|---|---|---|
| Cos 0 = | 1 | 0 |
| Cos 30° = | $\sqrt{3}/2$ | $\pi/6$ |
| Cos 45 = | $1/\sqrt{2}$ | $\pi/4$ |
| Cos 60° = | $1/2$ | $\pi/3$ |
| Cos 90 = | 0 | $\pi/2$ |
| Cos 120 = | $-1/2$ | $2\pi/3$ |
| Cos 135 = | $-1/\sqrt{2}$ | |
| Cos 150 = | $-\sqrt{3}/2$ | |
| Cos 180 = | -1 | $\pi$ |
| Cos $3\pi/2$ = 270 = | 0 | |

At 5 instants

At point 1 $\omega t = 0$ $i_c = I_{max}$

$$I_{max} = I_{CQ} + B_0 + B_1 + B_2 + B_3 + B_4 \longrightarrow (6)$$

At point 2 $\omega t = \pi/3$ $i_c = I_{1/2}$

$$i_c = I_{CQ} + B_0 + B_1 \cos\pi/3 + B_2 \cos 2\pi/3 + B_3 \cos\frac{3\pi}{3} + B_4 \cos\frac{4\pi}{3}$$

$$I_{1/2} = I_{CQ} + B_0 + 0.5B_1 - 0.5B_2 - B_3 - 0.5B_4 \longrightarrow (7)$$

At point 3 $\omega t = \pi/2$, $i_c = i_{CQ}$

$$i_c = I_{CQ} + B_0 + B_1 \cos\frac{\pi}{2} + B_2 \cos 2\pi/2 + B_3 \cos\frac{3\pi}{2} + B_4 \cos 4\pi/2$$

$$I_{CQ} = I_{CQ} + B_0 - B_2 + B_4 \longrightarrow (8)$$

At point 4 $\omega t = \frac{2\pi}{3}$ $i_c = I_{-1/2}$

$$I_{-1/2} = I_{CQ} + B_0 - 0.5B_1 - 0.5B_2 + B_3 - 0.5B_4 \longrightarrow 9$$

At point 4 $\omega t = \pi$, $i_c = I_{min}$

$$i_c = I_{CQ} + B_0 + B_1 \cos\pi + B_2 \cos 2\pi + B_3 \cos 3\pi + B_4 \cos 4\pi$$

$$I_{min} = I_{CQ} + B_0 - B_1 + B_2 - B_3 + B_4 \longrightarrow (10)$$

Solving (5) Eq we get $B_0, B_1, B_2, B_3, B_4$ we get.

$$I_{max} + I_{min} = I_{CQ} + B_0 + B_1 + B_2 + B_3 + B_4$$

$$= I_{CQ} + B_0 - B_1 + B_2 - B_3 + B_4$$

$$I_{max} + I_{min} = 2I_{CQ} + 2B_0 + 2B_2 + 2B_4 \longrightarrow 11$$

$$2I_{1/2} = 2I_{CQ} + 2B_0 + B_1 - B_2 - 2B_3 - B_4$$

$$2I_{-1/2} = 2I_{CQ} + 2B_0 - B_1 - B_2 + 2B_3 - B_4$$

Adding Eqs (11) & (12) to find $B_0$

$$I_{max} + I_{min} + 2I_{1/2} + 2I_{-1/2} = 6I_{CQ} + 6B_0$$

$$= 6[I_{CQ} + B_0]$$

$$= 6B_0$$

$$\therefore B_0 = \frac{1}{6}\left[I_{max} + I_{min} + 2I_{1/2} + 2I_{-1/2}\right]$$

$$I_{max} - I_{min} = 2B_1 + 2B_3$$

$$2I_{-1/2} - 2I_{1/2} = -2B_1 + 4B_3$$

$$I_{max} - I_{min} + 2I_{-1/2} - 2I_{1/2} = 2B_1 + 2B_3 - 2B_1 + 4B_3$$

$$= 6B_3$$

$$\therefore B_3 = \frac{1}{6}\left[I_{max} - I_{min} + 2I_{-1/2} - 2I_{1/2}\right]$$

Finally

$$B_0 = \frac{1}{6}\left[I_{max} + 2I_{1/2} + 2I_{-1/2} + I_{min}\right]$$

$$B_1 = \frac{1}{3}\left[I_{max} + I_{1/2} - I_{-1/2} - I_{min}\right]$$

$$B_2 = \frac{1}{4}\left[I_{max} - 2I_{CQ} + I_{min}\right]$$

$$B_3 = \frac{1}{6}\left[I_{max} - 2I_{1/2} + 2I_{-1/2} - I_{max}\right]$$

$$B_4 = \frac{1}{12}\left[I_{max} - 4I_{1/2} + 6I_{CQ} - 4I_{-1/2} + I_{min}\right]$$

Here the harmonic distortion CO-efficient can be obtained by

$$D_n = \frac{|B_n|}{|B_1|}$$

$$B_2 = \frac{I_{max} + I_{min} - 2I_{CQ}}{4}$$

As the Amp of the fundamental & 2nd harmonic are

wn, the 2nd harmonic distortion can be cal as

$$\% D_2 = \frac{|B_2|}{|B_1|} \times 100$$

As the method uses three point on the collector

urrent waveform to obtain the amplitude of the harmonics

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As the non-linearity present in dynamic characte

rease, the order of the harmonic distortion also increases

Let the mathematical expression for the Collector

urrent due to higher order harmonic be

$$i_c = K_1 i_b + K_2 i_b^2 + K_3 i_b^3 + K_4 i_b^4 \longrightarrow (1)$$

sub i/p signal $i_b = I_{bm} \cos\omega t$ we get.

$$i_c = K_1 I_{bm} \cos\omega t + K_2 I_{bm} \cos^2\omega t + K_3 I_{bm} \cos^3\omega t + K_4 I_{bm} \cos^4\omega t \longrightarrow (2)$$

Sub $\cos^2\omega t$, $\cos^3\omega t$, & $\cos^4\omega t$ & doing trigonometric ope, we get.

(3)

$$i_c = B_0 + B_1 \cos\omega t + K_2 I_{bm} \frac{1 + \cos 2\omega t}{2} \longrightarrow$$

$$i_c = B_0 + B_1 \cos\omega t + B_2 \cos 2\omega t + B_3 \cos 3\omega t + B_4 \cos 4\omega t \longrightarrow 4$$

The total current at Collector including dc bias can be written as

$$i_c = i_{CQ} + B_0 + B_1 \cos\omega t + B_2 \cos 2\omega t + B_3 \cos 3\omega t + B_4 \cos 4\omega t$$

↳ (5).

where $\underline{I_{CQ} + B_0}$ is the dc component

It can be seen that due to presence of harmonics, the dc current increases practically the presence of harmonic can be detected by connecting millimeter in the Collector circuit. The readings can be observed without an a.c input signal and with ac input signal. If the two readings are almost same there are no harmonic present But if milliammeter shown an increase in current, when an input is applied, then the harmonics can be concluded to present in the o/p signal.

Now to find the value of total collector current at the various instant 1, 2 & 3

At point 1, $\omega t = 0$, sub in 5

$$\therefore i_c = I_{CQ} + B_0 + B_1 + B_2 = I_{max} \longrightarrow 6$$

Hence the Eq

At point 2 $\omega t = \pi/2$

$$\therefore i_C = I_{CQ} + B_0 - B_2 = I_{CQ} \rightarrow 7$$

At point 3 $\omega t = \pi$

$$\therefore i_C = I_{CQ} + B_0 - B_1 + B_2 = I_{min} \rightarrow 8$$

But at

$\omega t = 0$, $i_c = I_{max}$

$\omega t = \pi/2$, $i_c = I_{CQ}$

$\omega t = \pi$ ; $i_C = I_{min}$

Hence the Eq

from Eq (3) $B_0 = B_2$

Now $I_{max} - I_{min} = \cancel{I_{CQ}} + \cancel{B_0} + B_1 + \cancel{B_2} - \cancel{I_{CQ}} - \cancel{B_0} + B_1 - \cancel{B_2}$

$$I_{max} - I_{min} = 2B_1$$

$$B_1 = \frac{I_{max} - I_{min}}{2}$$

$$I_{max} + I_{min} = I_{CQ} + B_0 + \cancel{B_1} + B_2 + I_{CQ} + B_0 - \cancel{B_1} + B_2$$

$$= 2I_{CQ} + 2B_0 + 2B_2$$

$$I_{max} + I_{min} = 2I_{CQ} + 4B_2$$

$$B_2 = \frac{I_{max} + I_{min} - 2I_{CQ}}{4}$$

As the Amp of the fundamental & 2nd harmonic are known, the 2nd harmonic distortion can be cal as

$$\% D_2 = \frac{|B_2|}{|B_1|} \times 100$$

As the method uses three point on the collector current waveform to obtain the amplitude of the harmonics This is called 3-point method of determing 2nd harmonic distor

Higher order harmonic distortion (five point method

As the non-linearity present in dynamic characteristics increase, the order of the harmonic distortion also increases

Let the mathematical expression for the collector current due to higher order harmonic be

$$i_c = K_1 i_b + K_2 i_b^2 + K_3 i_b^3 + K_4 i_b^4 \longrightarrow (1)$$

sub i/p signal $i_b = I_{bm} \cos\omega t$ eqn.

$$i_c = K_1 I_{bm} \cos\omega t + K_2 I_{bm} \cos^2\omega t + K_3 I_{bm} \cos^3\omega t + K_4 I_{bm} \cos^4\omega t \longrightarrow (2)$$

Sub $\cos^2\omega t$, $\cos^3\omega t$, & $\cos^4\omega t$ & doing trigonometric eqn, eqn.

$$i_c = B_0 + B_1 \cos\omega t + K_2 I_{bm} \frac{1 + \cos 2\omega t}{2} \longrightarrow (3)$$

$$i_c = B_0 + B_1 \cos\omega t + B_2 \cos 2\omega t + B_3 \cos 3\omega t + B_4 \cos 4\omega t \longrightarrow 4$$

The total current at Collector including dc bias can be written

$$i_c = I_{CQ} + B_0 + B_1 \cos\omega t + B_2 \cos 2\omega t + B_3 \cos 3\omega t + B_4 \cos 4\omega t \longrightarrow (5)$$

where $I_{CQ} + B_0$ is the dc component

$B_1, B_2, B_3$ and $B_4$ are the Amp of the fundamental, second 3rd & 4th harmonic Components.

| | | |
|---|---|---|
| Cos 0 = | 1 | 0 |
| Cos 30° = | $\sqrt{3}/2$ | $\pi/6$ |
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| Cos 120 = | $-1/2$ | $2\pi/3$ |
| Cos 135 = | $-1/\sqrt{3}$ | |
| Cos 150 = | $-\sqrt{3}/2$ | |
| Cos 180 = | -1 | $\pi$ |
| Cos $3\pi/2$ = 270 = | 0 | |

At 5 instants

At point 1 $\omega t = 0$ $i_c = I_{max}$

$$I_{max} = I_{C\theta} + B_0 + B_1 + B_2 + B_3 + B_4 \longrightarrow (6)$$

At point 2 $\omega t = \pi/3$ $i_c = I_{1/2}$

$$i_c = I_{C\theta} + B_0 + B_1 \cos \pi/3 + B_2 \cos 2\pi/3 + B_3 \cos \frac{3\pi}{3} + B_4 \cos \frac{4\pi}{3}$$

$$I_{1/2} = I_{C\theta} + B_0 + 0.5B_1 - 0.5B_2 - B_3 - 0.5B_4 \longrightarrow (7)$$

At point 3 $\omega t = \pi/2$, $i_c = i_{C\theta}$

$$i_c = I_{C\theta} + B_0 + B_1 \cos \frac{\pi}{2} + B_2 \cos 2\pi/2 + B_3 \cos \frac{3\pi}{2} + B_4 \cos 4\pi/2$$

$$I_{C\theta} = I_{C\theta} + B_0 - B_2 + B_4 \longrightarrow (8)$$

At point 4 $\omega t = \frac{2\pi}{3}$ $i_c = I_{-1/2}$

$$I_{-1/2} = I_{C\theta} + B_0 - 0.5B_1 - 0.5B_2 + B_3 - 0.5B_4 \longrightarrow 9$$

At point 4 $\omega t = \pi$, $i_c = I_{min}$

$$i_c = I_{C\theta} + B_0 + B_1 \cos\pi + B_2 \cos 2\pi + B_3 \cos 3\pi + B_4 \cos 4\pi$$

$$I_{min} = I_{C\theta} + B_0 - B_1 + B_2 - B_3 + B_4 \longrightarrow (10)$$

Solving (5) eq we get $B_0, B_1, B_2, B_3, B_4$ we get.

$$I_{max} + I_{min} = I_{C\theta} + B_0 + B_1 + B_2 + B_3 + B_4$$
$$= I_{C\theta} + B_0 - B_1 + B_2 - B_3 + B_4$$

$$I_{max} + I_{min} = 2I_{C\theta} + 2B_0 + 2B_2 + 2B_4 \longrightarrow 11$$

$$2I_{1/2} = 2I_{C\theta} + 2B_0 + B_1 - B_2 - 2B_3 - B_4$$
$$2I_{-1/2} = 2I_{C\theta} + 2B_0 - B_1 - B_2 + 2B_3 - B_4$$

$$2I_{1/2} + 2I_{-1/2} = 4I_{C\theta} + 4B_0 - 2B_2 - 2B_4 \longrightarrow 12$$

Adding Eqs (11) & (12) to find $B_0$

$$I_{max} + I_{min} + 2I_{1/2} + 2I_{-1/2} = 6I_{CQ} + 6B_0$$

$$= 6[I_{CQ} + B_0]$$

$$\simeq 6B_0$$

$$\therefore B_0 = \frac{1}{6}\left[I_{max} + I_{min} + 2I_{1/2} + 2I_{-1/2}\right]$$

$$I_{max} - I_{min} = 2B_1 + 2B_3$$

$$2I_{-1/2} - 2I_{1/2} = -2B_1 + 4B_3$$

$$I_{max} - I_{min} + 2I_{-1/2} - 2I_{1/2} = 2B_1 + 2B_3 - 2B_1 + 4B_3$$

$$= 6B_3$$

$$\therefore B_3 = \frac{1}{6}\left[I_{max} - I_{min} + 2I_{-1/2} - 2I_{1/2}\right]$$

Finally

$$B_0 = \frac{1}{6}\left[I_{max} + 2I_{1/2} + 2I_{-1/2} + I_{min}\right]$$

$$B_1 = \frac{1}{3}\left[I_{max} + I_{1/2} - I_{-1/2} - I_{min}\right]$$

$$B_2 = \frac{1}{4}\left[I_{max} - 2I_{CQ} + I_{min}\right]$$

$$B_3 = \frac{1}{6}\left[I_{max} - 2I_{1/2} + 2I_{-1/2} - I_{max}\right]$$

$$B_4 = \frac{1}{12}\left[I_{max} - 4I_{1/2} + 6I_{CQ} - 4I_{-1/2} + I_{min}\right]$$

Here the harmonic distortion co-efficient can be obtained by

$$D_n = \frac{|B_n|}{|B_1|}$$

Power o/p due to distortion

$P_{ac} = V \cdot I$ $\qquad V = iR$

$= \frac{I_m V_m}{2}$ $\qquad V_m = i_m R_L$

$P_{ac} = \frac{I_m^2 R_L}{2}$

$I_m$ = Peak value of the o/p current

$= \frac{I_{pp}}{2} = \frac{I_{max} - I_{min}}{2}$

$B_1 = \frac{I_{max} - I_{min}}{2}$

$I_m = B_1$

$$\boxed{P_{ac} = \tfrac{1}{2} B_1^2 R_L}$$

Hence o/p power with harmonic distortion

$(P_{ac})_D = \frac{1}{2} B_1^2 R_L + \frac{1}{2} B_2^2 R_L + \cdots \frac{1}{2} B_n^2 R_L$

$= \frac{1}{2} B_1^2 R_L \left[ 1 + \frac{B_2^2}{B_1^2} + \frac{B_3^2}{B_1^2} + \cdots \frac{B_n^2}{B_1^2} \right]$

$(P_{ac})_D = P_{ac} \left[ 1 + D_2^2 + D_3^2 + \cdots D_n^2 \right]$

$D^2 = D_2^2 + D_3^2 + \cdots + D_n^2$

$(P_{ac})_D = P_{ac} \left[ 1 + D^2 \right)$

If the total harmonic distortion $D = 0.15$

$(P_{ac})_D = P_{ac} \left[ 1 + (0.15)^2 \right]$

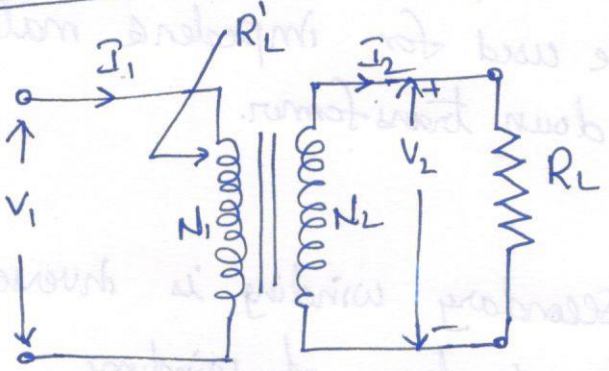
$= 1.0225 P_{ac}$

So that is 2.25 % increase in the power given to the load.

## Transformer Coupled class A Amplifier :-

* For maximum power transfer to the load, the impedence matching is necessary.
* For loads like loudspeaker, having low impedence values, impedence matching is difficult using directly coupled amplifier circuit.
* This is because loudspeaker resistance is in the range of 3 to 4 ohms to 16 ohms while the output impedence of series fed directly coupled class A amplifier is very much high.
* This problem can be eliminated by using transformer to deliver power to the load. The transformer is called an output transformer. and amplifier is called transformed coupled class A amplifier.

## Properties of transformer :-




* Consider a transformer as shown in the fig. which is connected to a load resistance $R_L$.
* while analysing transformer, is is assumed that the transformer is ideal and there are no loses in transformer. Similarly the winding resistances are assumed to be zero.

$N_1$ = Number of turns on primary
$N_2$ = Number of turns on secondary
$V_1$ = Voltage applied to primary
$V_2$ = Voltage on secondary

$I_2$ = primary Current.

1) Turns ratio:-

The ratio of no. of turns on secondary to the no. of turns on primary is called turns ratio and is denoted by n.

$$n = \frac{N_2}{N_1}$$

* Sometimes it is specified as $\frac{N_2}{N_1}:1$ (or) $\frac{N_1}{N_2}:1$

2) Voltage transformation:-

The transformer transforms the voltage applied on or to otherside proportional to turns ratio. The transformer be step up (or) step down transformer.

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} = n$$

In amplifier analysis, load impedence is going to be sma And the transformer is to be used for impedence matchin Hence it has to be a step down transformer.

3) Current transformation:-

The current in the secondary winding is inversely proportional to the number of turns of windings.

$$\frac{I_2}{I_1} = \frac{N_1}{N_2} = \frac{1}{n}$$

4) Impedence transformation:-

As current and voltage get transformed from primary to secondary, an impedence seen from either side also changes. The impedence of the load on secondary is $R_L$.

$$R_L = \frac{V_2}{I_2} \quad \text{and} \quad R_L = \frac{V_1}{I_1}$$

$$V_1 = \frac{N_1}{N_2} V_2 \quad \text{and} \quad \frac{I_1}{I_2} = \frac{N_2}{N_1}$$

$$I_1 = \frac{N_2}{N_1} I_2$$

$$R_L' = \frac{\frac{N_1}{N_2} V_2}{\frac{N_2}{N_1} I_2} = \left[\frac{N_1}{N_2}\right]^2 \times \frac{V_2}{I_2}$$

$$\boxed{R_L' = \frac{R_L}{n^2}}$$

The $R_L'$ is reflected impedence.

Problem

The load of 4Ω is connected to the secondary of a transformer having primary turns of 200 and secondary turns of 20. Calculate the reflected load impedence on primary.

Solution Given that

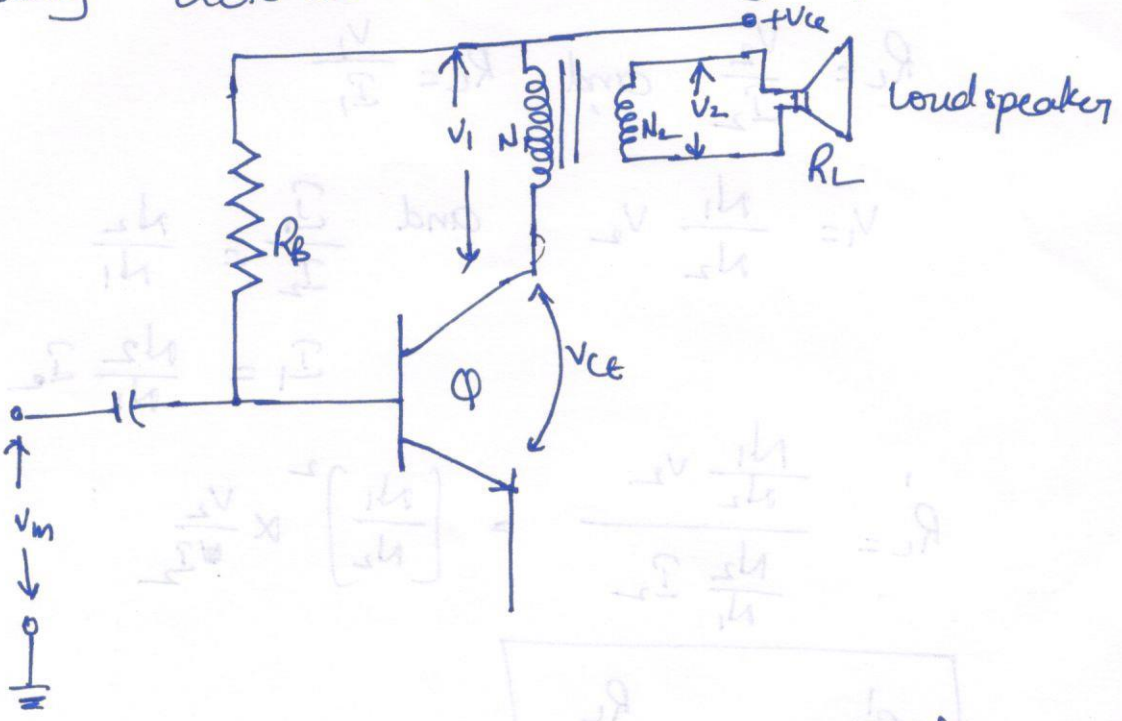
$$R_L = 4\Omega \quad N_1 = 200 \quad N_2 = 20$$

$$n = \frac{N_2}{N_1} = \frac{20}{200} = 0.1$$

$$R_L' = \frac{R_L}{n^2} = \frac{4}{(0.1)^2} = 400\Omega$$

## Circuit diagram of transformer Coupled Amplifier

The basic circuit of a transformer coupled amplifier is shown in below fig. The loudspeaker connected to the secondary acts as a load having impedance of $R_L\,\Omega$.




The transformer used is a step down transforma with turns ratio as $n = \frac{N_2}{N_1}$.

## DC operation

- It is assumed that winding resistances are 0Ω. Hence for dc. purposes the resistance is 0Ω.
- There is no voltage drop across the primary winding of the transformer.
- The slope of the d.c load line is reciprocal of the d.c resistance in collector circuit, which is zero in this case.
- Hence slope of d.c load line is ideally infinite. The d.c load line is vertically straight line

Apply KVL at Collector side

$$V_{cc} - V_{CE} = 0$$

$$V_{cc} = V_{CE}$$

This is dc bias voltage $V_{CEQ}$ for the transistor

$$\therefore V_{cc} = V_{CEQ}$$

(*) the intersection of d-c load line and the base current set by the circuit is the Quiescent operating point. the d-c load line as shown in fig (1).

DC power input:

The d-c Power input is provided by supply voltage with no signal input. the dc current drawn is the Collector bias current $I_{CQ}$

$$P_{DC} = V_{cc} I_{CQ}$$

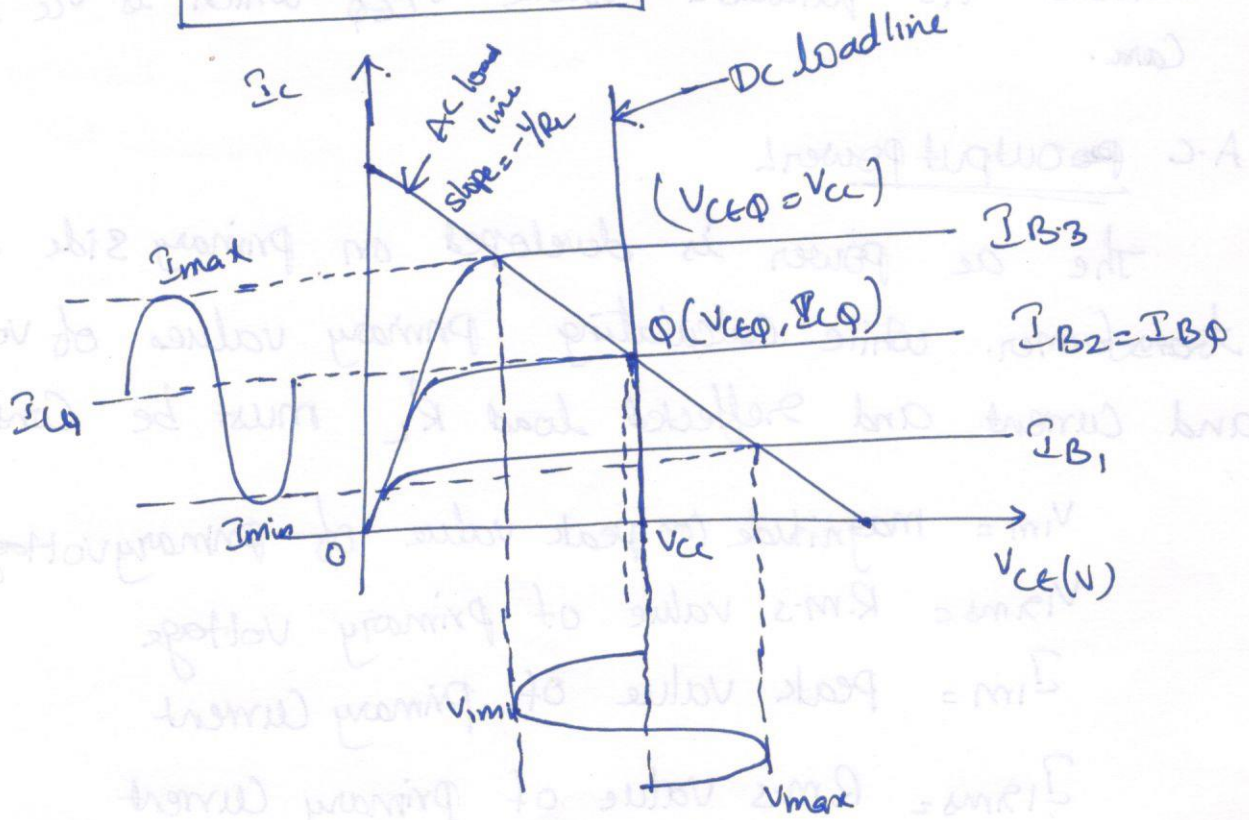



Fig (1).

## A.C Operation:-

(*) For a.c analysis, it is necessary to draw an ac load line on the output characteristics.

(*) For ac purposes, the load on secondary is the load impedance $R_L$ Ω and the reflected load on primary is $R'_L$

(*) The load line drawn with a slope of $\left[\frac{-1}{R'_L}\right]$ and passing through the operating point is called a.c load line. Shown in fig(1).

(*) The output current i.e. collector current varies around its quiescent value $I_{CQ}$, when a.c input signal applied to the amplifier.

(*) The corresponding output voltage also varies sinusoidally around its quiescent value $V_{CEQ}$ which is $V_{CC}$ in this case.

## A.C output power:-

The ac power is developed on primary side of transformer. While calculating primary values of voltage and current and reflected load $R'_L$ must be considered.

$V_{im}$ = magnitude (or) peak value of primary voltage

$V_{1rms}$ = R.M.S value of primary voltage

$I_{im}$ = peak value of primary current

$I_{1rms}$ = R.M.S value of primary current