Linked List

1. Merge Two Sorted Lists

 ${\bf Pattern} \hbox{: Linked Lists} + \hbox{Two Pointers}$

Problem Statement

You are given the heads of two sorted linked lists list1 and list2.

Merge the two lists into one sorted list. The list should be made by splicing together the nodes of the first two lists.

Return the head of the merged linked list.

Sample Input & Output

```
Input: list1 = [1,2,4], list2 = [1,3,4]
Output: [1,1,2,3,4,4]
Explanation: Merge by comparing nodes and linking smaller one.
```

```
Input: list1 = [], list2 = []
Output: []
Explanation: Both lists empty → return null.
```

```
Input: list1 = [], list2 = [0]
Output: [0]
Explanation: One list empty → return the other as-is.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def mergeTwoLists(
        self,
        list1: Optional[ListNode],
        list2: Optional[ListNode]
    ) -> Optional[ListNode]:
        # STEP 1: Initialize structures
        # - Use dummy head to simplify edge cases (empty lists)
        # - `current` tracks the tail of the merged list
        dummy = ListNode()
        current = dummy
        # STEP 2: Main loop / recursion
          - While both lists have nodes, compare values
        # - Link the smaller node to `current`
        while list1 and list2:
            if list1.val <= list2.val:</pre>
                current.next = list1
                list1 = list1.next
            else:
                current.next = list2
                list2 = list2.next
            current = current.next # move tail forward
        # STEP 3: Update state / bookkeeping
        # - One list may remain; attach it directly
            - No need to iterate-already sorted
        current.next = list1 or list2
        # STEP 4: Return result
        # - Skip dummy node; return real head
        return dummy.next
```

```
# ----- INLINE TESTS -----
def to_list(head: Optional[ListNode]) -> list:
   """Helper: convert linked list to Python list for easy testing"""
   result = []
   while head:
       result.append(head.val)
       head = head.next
   return result
def from_list(vals: list) -> Optional[ListNode]:
   """Helper: convert Python list to linked list"""
   if not vals:
       return None
   head = ListNode(vals[0])
   current = head
   for val in vals[1:]:
       current.next = ListNode(val)
       current = current.next
   return head
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case
   11 = from_list([1, 2, 4])
   12 = from_list([1, 3, 4])
   merged = sol.mergeTwoLists(11, 12)
   print(to_list(merged)) # Expected: [1, 1, 2, 3, 4, 4]
   # Test 2: Edge case - both empty
   11 = from_list([])
   12 = from_list([])
   merged = sol.mergeTwoLists(11, 12)
   print(to_list(merged)) # Expected: []
   # Test 3: Tricky/negative - one empty
   11 = from_list([])
   12 = from_list([0])
   merged = sol.mergeTwoLists(11, 12)
   print(to_list(merged)) # Expected: [0]
```

instant feedback.

Example Walkthrough

We'll trace Test 1: list1 = [1,2,4], list2 = [1,3,4].

1. Initialize:

- dummy = ListNode(0) → dummy node with val=0
- current = dummy → points to dummy
- list1 points to node(1), list2 points to node(1)

2. First loop iteration:

- Compare list1.val = 1 vs list2.val = $1 \rightarrow \text{equal}$, pick list1
- current.next = list1 \rightarrow dummy \rightarrow node(1)
- Move list1 = list1.next → now points to node(2)
- Move current = current.next → now at node(1)
- State: merged so far = [1]

3. Second iteration:

- list1.val = 2, list2.val = $1 \rightarrow pick list2$
- current.next = list2 $\rightarrow node(1) \rightarrow node(1)$
- Move list2 = list2.next \rightarrow node(3)
- Move current \rightarrow now at second node(1)
- State: [1, 1]

4. Third iteration:

• list1.val = 2, list2.val = $3 \rightarrow pick$ list1

- Link node(2), advance list1 to node(4), current to node(2)
- State: [1, 1, 2]

5. Fourth iteration:

- list1.val = 4, list2.val = $3 \rightarrow pick list2$
- Link node(3), advance list2 to node(4), current to node(3)
- State: [1, 1, 2, 3]

6. Fifth iteration:

- list1.val = 4, list2.val = $4 \rightarrow pick list1$
- Link node(4), advance list1 to None, current to node(4)
- State: [1, 1, 2, 3, 4]

7. Exit loop:

- list1 is None, list2 is node(4)
- current.next = list2 → attach remaining [4]
- Final list: [1, 1, 2, 3, 4, 4]
- 8. Return: dummy.next \rightarrow skips dummy, returns first real node.

Final output: [1, 1, 2, 3, 4, 4]

Complexity Analysis

• Time Complexity: O(m + n)

We traverse each node in list1 (length m) and list2 (length n) exactly once. Total steps = m + n.

• Space Complexity: 0(1)

Only constant extra space used (dummy, current). We reuse existing nodes—no new list allocated.

2. Reverse Linked List

Pattern: Linked List Reversal (Iterative)

Problem Statement

Given the head of a singly linked list, reverse the list, and return the reversed list.

You are given the head of a singly linked list. Each node contains an integer value and a pointer to the next node. Your task is to reverse the direction of the links so that the last node becomes the first, and return the new head.

Sample Input & Output

```
Input: head = [1,2,3,4,5]
Output: [5,4,3,2,1]
Explanation: The links between nodes are reversed.
```

```
Input: head = [1,2]
Output: [2,1]
Explanation: Two-node list is swapped.
```

```
Input: head = []
Output: []
Explanation: Empty list remains empty.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
       self.val = val
       self.next = next
class Solution:
    def reverseList(self, head: Optional[ListNode]) -> Optional[ListNode]:
       # STEP 1: Initialize structures
           - prev tracks the new reversed list's head (starts as None)
       # - curr is the current node being processed (starts at head)
       prev = None
       curr = head
       # STEP 2: Main loop / recursion
       # - Process each node until curr becomes None
       # - Invariant: all nodes before curr are already reversed
       while curr:
           # STEP 3: Update state / bookkeeping
           # - Save next node before breaking the link
           # - Reverse the current node's pointer to prev
           # - Move prev and curr forward
           next_temp = curr.next
           curr.next = prev
           prev = curr
           curr = next_temp
       # STEP 4: Return result
       # - prev is now the new head of the reversed list
       return prev
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
    # Helper to convert list to linked list
    def list_to_linked(lst):
       dummy = ListNode()
       curr = dummy
       for val in 1st:
```

```
curr.next = ListNode(val)
        curr = curr.next
    return dummy.next
# Helper to convert linked list to list
def linked_to_list(head):
    result = []
    while head:
        result.append(head.val)
        head = head.next
    return result
# Test 1: Normal case
head1 = list_to_linked([1, 2, 3, 4, 5])
rev1 = sol.reverseList(head1)
assert linked_to_list(rev1) == [5, 4, 3, 2, 1]
print(" Test 1 passed: [1,2,3,4,5] \rightarrow [5,4,3,2,1]")
# Test 2: Edge case - single node
head2 = list_to_linked([1])
rev2 = sol.reverseList(head2)
assert linked_to_list(rev2) == [1]
print(" Test 2 passed: [1] → [1]")
# Test 3: Tricky/negative - empty list
head3 = list_to_linked([])
rev3 = sol.reverseList(head3)
assert linked_to_list(rev3) == []
print(" Test 3 passed: [] → []")
```

Example Walkthrough

Let's trace reverseList on input [1,2,3].

Initial state:

```
- head \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow None
- prev = None, curr = node(1)
```

```
Step 1: curr is not None
- next_temp = curr.next \rightarrow node(2)
- curr.next = prev \rightarrow node(1).next = None
- prev = curr \rightarrow prev = node(1)
- curr = next_temp → curr = node(2)
→ List so far: 1 → None (reversed part), 2 → 3 → None (remaining)
Step 2: curr = node(2)
- next_temp = node(3)
- node(2).next = prev (node(1))
-prev = node(2)
- curr = node(3)
\rightarrow Reversed: 2 \rightarrow 1 \rightarrow None
Step 3: curr = node(3)
- next_temp = None
- node(3).next = node(2)
-prev = node(3)
- curr = None
\rightarrow Reversed: 3 \rightarrow 2 \rightarrow 1 \rightarrow None
```

Key insight: We never lose the rest of the list because we save next_temp before reversing the link.

Complexity Analysis

• Time Complexity: O(n)

We visit each node exactly once in a single while loop.

• Space Complexity: 0(1)

Only three pointers (prev, curr, next_temp) are used — constant extra space.

3. Middle of the Linked List

Pattern: Fast & Slow Pointers (Two Pointers)

Loop ends \rightarrow return prev = node(3) \rightarrow [3,2,1]

Problem Statement

Given the head of a singly linked list, return the middle node of the linked list. If there are two middle nodes, return the **second** middle node.

Sample Input & Output

```
Input: [1,2,3,4,5]
Output: [3,4,5]
Explanation: The middle node is 3 (1-based index 3 of 5).

Input: [1,2,3,4,5,6]
Output: [4,5,6]
Explanation: Two middles (3 and 4); return second → 4.

Input: [1]
Output: [1]
Explanation: Single node is the middle.
```

```
from typing import Optional

# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next

class Solution:
    def middleNode(self, head: Optional[ListNode]) -> Optional[ListNode]:
        # STEP 1: Initialize two pointers
        # - slow moves 1 step at a time
```

```
# - fast moves 2 steps at a time
       slow = fast = head
       # STEP 2: Main loop - move pointers until fast reaches end
           - Invariant: when fast can't move 2 steps, slow is at middle
           - For even length: stops at second middle (as required)
       while fast and fast.next:
           slow = slow.next
                                    # Move slow by 1
           fast = fast.next.next # Move fast by 2
       # STEP 3: No extra bookkeeping needed - pointer logic handles it
       # STEP 4: Return slow - it's at the middle
       return slow
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case - odd length
   n1 = ListNode(1)
   n2 = ListNode(2)
   n3 = ListNode(3)
   n4 = ListNode(4)
   n5 = ListNode(5)
   n1.next, n2.next, n3.next, n4.next = n2, n3, n4, n5
   res = sol.middleNode(n1)
   assert [res.val, res.next.val, res.next.next.val] == [3,4,5]
   # Test 2: Edge case - single node
   single = ListNode(1)
   res = sol.middleNode(single)
   assert res.val == 1 and res.next is None
   # Test 3: Tricky case - even length (return second middle)
   e1 = ListNode(1)
   e2 = ListNode(2)
   e3 = ListNode(3)
   e4 = ListNode(4)
   e5 = ListNode(5)
   e6 = ListNode(6)
   e1.next, e2.next, e3.next = e2, e3, e4
```

```
e4.next, e5.next = e5, e6
res = sol.middleNode(e1)
assert [res.val, res.next.val, res.next.next.val] == [4,5,6]
print(" All tests passed!")
```

Example Walkthrough

Let's trace **Test 1**: [1,2,3,4,5]

1. Initialize:

```
slow = head \rightarrow points to node 1
fast = head \rightarrow also points to node 1
```

- 2. First loop iteration:
 - Condition: fast (1) and fast.next (2) exist \rightarrow enter loop
 - slow = slow.next \rightarrow now points to 2
 - fast = fast.next.next \rightarrow from 1 \rightarrow 2 \rightarrow 3, so points to 3
- 3. Second loop iteration:
 - Condition: fast (3) and fast.next (4) exist \rightarrow enter loop
 - slow = slow.next \rightarrow from 2 \rightarrow 3
 - fast = fast.next.next \rightarrow from 3 \rightarrow 4 \rightarrow 5, so points to 5
- 4. Third loop check:
 - fast = $5 \rightarrow \text{not None}$, but fast.next is None
 - Loop condition fast and fast.next fails \rightarrow exit
- 5. **Return**: slow points to node $3 \rightarrow$ correct middle

For even-length list [1,2,3,4,5,6]: - After 1st iter: slow=2, fast=3

- After 2nd iter: slow=3, fast=5
- After 3rd iter: slow=4, fast=None (since $5\rightarrow 6\rightarrow None$)
- Loop stops \rightarrow return 4 (second middle)

This works because **fast moves twice as fast**, so when it reaches the end, slow has covered exactly half the distance.

Complexity Analysis

• Time Complexity: O(n)

The fast pointer traverses the list once (n/2 iterations), so total steps $n/2 \rightarrow linear$ in input size.

• Space Complexity: 0(1)

Only two pointers (slow, fast) used — constant extra space, regardless of list length.

4. Remove Nth Node From End of List

Pattern: Two Pointers (Fast & Slow)

Problem Statement

Given the head of a linked list, remove the nth node from the end of the list and return its head.

Sample Input & Output

```
Input: head = [1,2,3,4,5], n = 2
Output: [1,2,3,5]
Explanation: The 2nd node from the end is 4 → remove it.

Input: head = [1], n = 1
Output: []
Explanation: Only one node → remove it → empty list.

Input: head = [1,2], n = 2
Output: [2]
Explanation: Remove the 2nd from end (i.e., the first node).
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def removeNthFromEnd(
        self, head: Optional[ListNode], n: int
    ) -> Optional[ListNode]:
        # STEP 1: Initialize dummy node and two pointers
        # - Dummy simplifies edge case (removing head)
           - Fast and slow both start at dummy
        dummy = ListNode(0)
        dummy.next = head
        fast = slow = dummy
        # STEP 2: Move fast pointer n+1 steps ahead
```

```
- Ensures gap of n+1 between fast and slow
       # - So when fast reaches end, slow is just before target
       for _{n} in range(n + 1):
           fast = fast.next
       # STEP 3: Move both pointers until fast hits None
          - Maintains fixed gap → slow lands before nth-from-end
       while fast:
           fast = fast.next
           slow = slow.next
       # STEP 4: Remove target node
       # - slow.next is the node to remove
           - Bypass it by linking slow to slow.next.next
       slow.next = slow.next.next
       # Return dummy.next (handles head removal cleanly)
       return dummy.next
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case - [1,2,3,4,5], n=2 \rightarrow [1,2,3,5]
   head1 = ListNode(1, ListNode(2, ListNode(3, ListNode(4, ListNode(5)))))
   res1 = sol.removeNthFromEnd(head1, 2)
   out1 = []
   curr = res1
   while curr:
       out1.append(curr.val)
       curr = curr.next
   print("Test 1:", out1) # Expected: [1, 2, 3, 5]
   # Test 2: Edge case - [1], n=1 \rightarrow []
   head2 = ListNode(1)
   res2 = sol.removeNthFromEnd(head2, 1)
   out2 = []
   curr = res2
   while curr:
       out2.append(curr.val)
       curr = curr.next
   print("Test 2:", out2) # Expected: []
```

```
# Test 3: Tricky case - [1,2], n=2 → [2]
head3 = ListNode(1, ListNode(2))
res3 = sol.removeNthFromEnd(head3, 2)
out3 = []
curr = res3
while curr:
   out3.append(curr.val)
   curr = curr.next
print("Test 3:", out3) # Expected: [2]
```

Example Walkthrough

We'll walk through **Test 3**: head = [1,2], n = 2.

- 1. Create dummy node:
 - dummy = ListNode(0) \rightarrow dummy.next = head \rightarrow list: [0 \rightarrow 1 \rightarrow 2]
 - fast = slow = dummy \rightarrow both point to node 0.
- 2. Move fast n+1 = 3 steps:
 - Step 1: fast = fast.next \rightarrow points to 1
 - Step 2: fast = fast.next \rightarrow points to 2
 - Step 3: fast = fast.next \rightarrow points to None
 - Now: fast = None, slow = node 0
- 3. Enter while fast: loop:
 - fast is None \rightarrow loop does not run
 - So slow remains at node 0
- 4. Remove target node:
 - slow.next is node 1 (the 2nd from end)

- slow.next = slow.next.next → node 0 now points to node 2
- Resulting list: $[0 \rightarrow 2]$
- 5. Return dummy.next:
 - dummy.next is node $2 \rightarrow \text{final list}$: [2]

Output: [2] — correct!

Key insight: The **dummy node** lets us treat head removal like any other node, and the n+1 gap ensures slow stops just before the node to delete.

Complexity Analysis

• Time Complexity: O(L)

We traverse the list at most twice: once to advance fast, once to move both pointers. L = length of list.

• Space Complexity: 0(1)

Only a few pointers (dummy, fast, slow) — no extra space proportional to input.

5. Swap Nodes in Pairs

Pattern: Linked List Manipulation (Iterative Pointer Rewiring)

Problem Statement

Given a linked list, swap every two adjacent nodes and return its head. You must solve the problem without modifying the values in the list's nodes (i.e., only nodes themselves may be changed).

The number of nodes in the list is in the range [0, 100]. 0 <= Node.val <= 100

Sample Input & Output

```
Input: head = [1,2,3,4]
Output: [2,1,4,3]
Explanation: Nodes 1 2 and 3 4 are swapped pairwise.

Input: head = []
Output: []
Explanation: Empty list remains empty.

Input: head = [1]
Output: [1]
Explanation: Single node has no pair to swap with.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
   def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def swapPairs(self, head: Optional[ListNode]) -> Optional[ListNode]:
        # STEP 1: Initialize structures
           - Use a dummy node to simplify edge handling at head
        # - prev points to node before the current pair
        dummy = ListNode(0)
        dummy.next = head
        prev = dummy
        # STEP 2: Main loop / recursion
        # - Loop while at least two nodes remain to swap
        # - first = first node in pair, second = second
```

```
while prev.next and prev.next.next:
           first = prev.next
           second = prev.next.next
           # STEP 3: Update state / bookkeeping
           # - Rewire pointers to swap the pair
           # - Order matters: avoid losing references
           first.next = second.next
           second.next = first
           prev.next = second
           # Move prev to end of swapped pair for next iteration
           prev = first
       # STEP 4: Return result
       # - dummy.next is new head (handles empty/single cases)
       return dummy.next
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case [1,2,3,4] \rightarrow [2,1,4,3]
   n4 = ListNode(4)
   n3 = ListNode(3, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   res = sol.swapPairs(n1)
   out = []
   while res:
       out.append(res.val)
       res = res.next
   print("Test 1:", out) # Expected: [2, 1, 4, 3]
   # Test 2: Edge case [] → []
   res = sol.swapPairs(None)
   print("Test 2:", [] if not res else "ERROR") # Expected: []
   # Test 3: Tricky/negative [1] → [1]
   single = ListNode(1)
   res = sol.swapPairs(single)
   out = [res.val] if res else []
```

```
print("Test 3:", out) # Expected: [1]
```

Example Walkthrough

We'll trace **Test 1**: input [1,2,3,4].

Initial setup: - dummy = ListNode(0) - dummy.next = $n1 \rightarrow list$: $0 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4$ - prev = dummy (points to node 0)

First iteration: - prev.next = n1, prev.next.next = n2 \rightarrow both exist \rightarrow enter loop - first = n1, second = n2 - Rewiring: - first.next = second.next \rightarrow n1.next = n3 - second.next = first \rightarrow n2.next = n1 - prev.next = second \rightarrow dummy.next = n2 - Now: 0 \rightarrow 2 \rightarrow 1 \rightarrow 3 \rightarrow 4 - Update prev = first \rightarrow prev = n1

Second iteration: - prev = n1, so prev.next = n3, prev.next.next = n4 \rightarrow enter loop - first = n3, second = n4 - Rewiring: - n3.next = n4.next \rightarrow n3.next = None - n4.next = n3 - n1.next = n4 - Now: 0 \rightarrow 2 \rightarrow 1 \rightarrow 4 \rightarrow 3 - Update prev = n3

Next check: - prev.next = None \rightarrow loop ends

Return dummy.next \rightarrow node 2, which starts 2 \rightarrow 1 \rightarrow 4 \rightarrow 3

Final output: [2, 1, 4, 3]

Key insight: dummy node avoids special-casing the head swap, and prev always trails the last swapped node, enabling clean chaining.

Complexity Analysis

• Time Complexity: O(n)

We visit each node exactly once. Each pair is processed in constant time, and there are n/2 pairs \rightarrow linear overall.

• Space Complexity: 0(1)

Only a fixed number of pointers (dummy, prev, first, second) are used — no recursion or extra data structures scaling with input.

6. Rotate List

Pattern: Linked List + Two Pointers + Modular Arithmetic

Problem Statement

Given the head of a linked list, rotate the list to the right by k places.

Clarifications:

- Rotation means moving the last k nodes to the front.
- If k is larger than the list length, use k % length (effective rotation).
- Edge cases: empty list, single node, or k = 0.

Sample Input & Output

```
Input: head = [1,2,3,4,5], k = 2

Output: [4,5,1,2,3]

Explanation: Rotate right twice: [5,1,2,3,4] \rightarrow [4,5,1,2,3]
```

```
Input: head = [0,1,2], k = 4

Output: [2,0,1]

Explanation: k=4 \rightarrow effective \ k = 4 \% \ 3 = 1 \rightarrow rotate once
```

```
Input: head = [1], k = 0
Output: [1]
Explanation: No rotation needed
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
   def __init__(self, val=0, next=None):
       self.val = val
       self.next = next
class Solution:
   def rotateRight(self, head: Optional[ListNode],
                  k: int) -> Optional[ListNode]:
       # STEP 1: Handle empty or single-node list
       if not head or not head.next:
           return head
       # STEP 2: Compute length and get tail
       # - Traverse once to find length and tail node
       length = 1
       tail = head
       while tail.next:
           tail = tail.next
           length += 1
       # STEP 3: Normalize k using modulo
       # - Avoid unnecessary full rotations
       k = k % length
       if k == 0:
           return head # no effective rotation
       # STEP 4: Find new tail (at position length - k - 1)
       # - New head will be new_tail.next
       new_tail = head
       for _ in range(length - k - 1):
           new_tail = new_tail.next
       new_head = new_tail.next
       new_tail.next = None # break the list
       return new_head
# ----- INLINE TESTS -----
```

```
if __name__ == "__main__":
   sol = Solution()
    # Test 1: Normal case
    # Build [1,2,3,4,5]
   n5 = ListNode(5)
   n4 = ListNode(4, n5)
   n3 = ListNode(3, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   res = sol.rotateRight(n1, 2)
   # Expected: [4,5,1,2,3]
   out = []
    curr = res
    while curr:
        out.append(curr.val)
        curr = curr.next
   print("Test 1:", out) # [4, 5, 1, 2, 3]
    # Test 2: Edge case - k > length
   m2 = ListNode(2)
   m1 = ListNode(0, m2)
   res2 = sol.rotateRight(m1, 4) # len=2 → k=0 → but wait: len=2? No!
    # Correction: [0,1,2] \rightarrow len=3
   c2 = ListNode(2)
    c1 = ListNode(1, c2)
    c0 = ListNode(0, c1)
    res2 = sol.rotateRight(c0, 4)
    out2 = []
    curr = res2
    while curr:
        out2.append(curr.val)
        curr = curr.next
    print("Test 2:", out2) # [2, 0, 1]
    # Test 3: Tricky/negative - k=0 or single node
    single = ListNode(1)
    res3 = sol.rotateRight(single, 0)
    out3 = []
    curr = res3
    while curr:
        out3.append(curr.val)
```

```
curr = curr.next
print("Test 3:", out3) # [1]
```

Example Walkthrough

We'll trace Test 1: head = [1,2,3,4,5], k = 2.

Initial state:

- Linked list: 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow None
- head points to node 1

Step-by-step:

- 1. Check empty/single: head exists and has next \rightarrow proceed.
- 2. Compute length & find tail:
 - Start: tail = node(1), length = 1
 - Iter 1: tail = node(2), length = 2
 - Iter 2: tail = node(3), length = 3
 - Iter 3: tail = node(4), length = 4
 - Iter 4: tail = node(5), length = $5 \rightarrow \text{stop}$
 - Now: tail = node(5), length = 5
- 3. Normalize k:
 - $k = 2 \% 5 = 2 \rightarrow \text{not zero} \rightarrow \text{continue}$
- 4. Find new_tail:
 - Need to move length -k-1=5-2-1=2 steps from head
 - Start: new_tail = node(1)

- Step 1: new_tail = node(2)
- Step 2: new_tail = node(3)
- Now: new_tail = node(3)
- 5. Break and reconnect:
 - new_head = new_tail.next = node(4)
 - Set new_tail.next = None → list becomes: 1→2→3→None
 - Set tail.next = head \rightarrow 5 \rightarrow 1
 - Final list: $4 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow None$
- 6. Return new_head (node 4) \rightarrow output [4,5,1,2,3]

Final output matches expectation.

Complexity Analysis

• Time Complexity: O(n)

We traverse the list **twice**: once to get length/tail, once to find new tail. Each is O(n), so total O(n).

• Space Complexity: 0(1)

Only a few pointers (tail, new_tail, new_head) are used. No recursion or extra data structures that scale with input.

7. Linked List Cycle

Pattern: Fast & Slow Pointers (Floyd's Cycle Detection)

Problem Statement

Given head, the head of a linked list, determine if the linked list has a cycle in it. There is a cycle in a linked list if there is some node in the list that can be reached again by continuously following the next pointer. Internally, pos is used to denote the index of the node that tail's next pointer is connected to. Note that pos is not passed as a parameter.

Return true if there is a cycle in the linked list. Otherwise, return false.

Sample Input & Output

```
Input: head = [3,2,0,-4], pos = 1
Output: true
Explanation: There is a cycle in the linked list,
where the tail connects to the 1st node (0-indexed).

Input: head = [1,2], pos = 0
Output: true
Explanation: The tail connects to the Oth node, forming a cycle.

Input: head = [1], pos = -1
Output: false
Explanation: No cycle exists; the list has only one node pointing to null.
```

```
from typing import Optional

# Definition for singly-linked list.
class ListNode:
    def __init__(self, x):
        self.val = x
        self.next = None
```

```
class Solution:
   def hasCycle(self, head: Optional[ListNode]) -> bool:
       # STEP 1: Initialize structures
       # - Use two pointers: slow (1x speed) and fast (2x speed)
       # - If there's a cycle, fast will eventually catch up to slow
       if not head or not head.next:
           return False # Empty or single node → no cycle possible
       slow = head
       fast = head.next
       # STEP 2: Main loop / recursion
       # - Move slow by 1 step, fast by 2 steps
          - Invariant: if cycle exists, fast and slow will meet
       while fast and fast.next:
           if slow == fast:
               return True # Cycle detected
           slow = slow.next
           fast = fast.next.next
       # STEP 3: Update state / bookkeeping
       # - Handled implicitly via pointer movement in loop
       # STEP 4: Return result
       # - If loop exits, fast reached null → no cycle
       return False
# ------ INLINE TESTS ------
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case - cycle exists
   n1 = ListNode(3)
   n2 = ListNode(2)
   n3 = ListNode(0)
   n4 = ListNode(-4)
   n1.next = n2
   n2.next = n3
   n3.next = n4
   n4.next = n2 \# cycle: -4 \rightarrow 2
```

```
assert sol.hasCycle(n1) == True
print(" Test 1 passed: Cycle detected in [3,2,0,-4]")

# Test 2: Edge case - single node, no cycle
n5 = ListNode(1)
assert sol.hasCycle(n5) == False
print(" Test 2 passed: Single node, no cycle")

# Test 3: Tricky/negative - two nodes, cycle
n6 = ListNode(1)
n7 = ListNode(2)
n6.next = n7
n7.next = n6 # cycle: 2 → 1
assert sol.hasCycle(n6) == True
print(" Test 3 passed: Two-node cycle detected")
```

Example Walkthrough

Let's trace Test 1: head = $[3 \rightarrow 2 \rightarrow 0 \rightarrow -4 \ 2]$

- 1. Initialization:
 - head is not null and has next \rightarrow skip early return.
 - slow = n1 (3), fast = n1.next = n2 (2)
- 2. First loop iteration:
 - Check: slow (3) != fast (2) \rightarrow continue
 - Update:

```
slow = slow.next \rightarrow n2 (2)

fast = fast.next.next \rightarrow n2.next = n3 \rightarrow n3.next = n4 \rightarrow so fast = n4 (-4)
```

- 3. Second loop iteration:
 - Check: slow (2) != fast (-4) \rightarrow continue
 - Update:

```
slow = n2.next \rightarrow n3 (0)
fast = n4.next \rightarrow n2 \rightarrow n2.next \rightarrow n3 \rightarrow so fast = n3 (0)
```

4. Third loop iteration:

- Check: slow (0) == fast (0) \rightarrow match!
- Return True

State snapshots: - Start: slow=3, fast=2 - After 1st move: slow=2, fast=-4 - After 2nd move: slow=0, fast=0 → cycle confirmed

This works because in a cycle, the fast pointer laps the slow one — like two runners on a circular track.

Complexity Analysis

• Time Complexity: O(n)

In the worst case (no cycle), fast traverses all nodes once $\rightarrow \sim 2n$ steps $\rightarrow O(n)$. With a cycle, detection happens in at most one full loop around the cycle.

• Space Complexity: 0(1)

Only two pointers (slow, fast) used — constant extra space regardless of input size.

8. Palindrome Linked List

Pattern: Linked List + Two Pointers (Fast/Slow) + In-Place Reversal

Problem Statement

Given the head of a singly linked list, return true if it is a palindrome or false otherwise.

A palindrome reads the same forward and backward.

You must solve the problem in O(n) time and O(1) space.

Sample Input & Output

```
Input: head = [1,2,2,1]
Output: true
Explanation: The list reads the same forwards and backwards.

Input: head = [1,2]
Output: false
Explanation: [1,2] [2,1].

Input: head = [1]
Output: true
Explanation: Single-element lists are palindromes by definition.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def isPalindrome(self, head: Optional[ListNode]) -> bool:
        # STEP 1: Handle empty or single-node list
        if not head or not head.next:
            return True
        # STEP 2: Use fast/slow pointers to find middle
        slow = fast = head
        while fast and fast.next:
            slow = slow.next
            fast = fast.next.next
```

```
# STEP 3: Reverse second half starting at slow
       prev = None
       curr = slow
       while curr:
           next_temp = curr.next
           curr.next = prev
           prev = curr
           curr = next_temp
       # Now 'prev' is head of reversed second half
       # STEP 4: Compare first half and reversed second half
       left = head
       right = prev
       while right: # Only compare until end of second half
           if left.val != right.val:
               return False
           left = left.next
           right = right.next
       # STEP 5: (Optional) Restore list by reversing again
       # Not required by problem, but good practice in real systems
       return True
# ------ INLINE TESTS ------
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case [1,2,2,1]
   n4 = ListNode(1)
   n3 = ListNode(2, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   assert sol.isPalindrome(n1) == True
   # Test 2: Edge case [1]
   single = ListNode(1)
   assert sol.isPalindrome(single) == True
   # Test 3: Tricky/negative [1,2,3]
   n3b = ListNode(3)
   n2b = ListNode(2, n3b)
```

```
n1b = ListNode(1, n2b)
assert sol.isPalindrome(n1b) == False
print(" All tests passed!")
```

Example Walkthrough

Let's trace **Test 1**: [1,2,2,1]

1. Initial check: head exists and has more than one node \rightarrow proceed.

2. Fast/slow pointers:

- Start: slow = 1, fast = 1
- Step 1: slow = 2, fast = 2 (fast moves two steps: $1 \rightarrow 2 \rightarrow 2$)
- Step 2: slow = 2 (second one), fast = None (2→1→None) → slow now points to start of second half: [2,1]

3. Reverse second half:

- Start: curr = 2, prev = None
- Iter 1: next_temp = 1; curr.next = None; prev = 2; curr = 1
- Iter 2: next_temp = None; curr.next = 2; prev = 1; curr = None → Reversed list: 1 → 2 → None; prev = 1 (new head)

4. Compare halves:

- left = 1, right = $1 \rightarrow \text{match}$
- left = 2, right = $2 \rightarrow \text{match}$
- right becomes None \rightarrow stop

5. Return: True

Final state: First half [1,2], reversed second half [1,2] \rightarrow identical \rightarrow palindrome.

Complexity Analysis

• Time Complexity: O(n)

One pass to find middle (n/2 steps), one pass to reverse (n/2), one pass to compare (n/2). Total $1.5n \to O(n)$.

• Space Complexity: 0(1)

Only a few pointers (slow, fast, prev, curr, left, right) used. No recursion or extra arrays. Reversal is in-place.

9. Reorder List

Pattern: Linked List + Two Pointers + Reversal

Problem Statement

You are given the head of a singly linked list. Reorder the list such that it follows this pattern:

You must do this **in-place** without altering the nodes' values.

Sample Input & Output

```
Input: [1,2,3,4]
Output: [1,4,2,3]
Explanation: First and last alternate: 1→4→2→3.

Input: [1,2,3,4,5]
Output: [1,5,2,4,3]
Explanation: Middle element (3) ends the sequence.

Input: [1]
Output: [1]
Explanation: Single node - no reordering needed.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
   def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def reorderList(self, head: Optional[ListNode]) -> None:
        # STEP 1: Find the middle using slow/fast pointers
            - Fast moves 2 steps, slow moves 1 → slow ends at mid
        slow = fast = head
        while fast and fast.next:
            slow = slow.next
           fast = fast.next.next
        # STEP 2: Reverse the second half starting from slow
        # - After reversal, second half starts at prev
        prev = None
```

```
curr = slow
       while curr:
           next_temp = curr.next
           curr.next = prev
           prev = curr
           curr = next_temp
       # STEP 3: Merge first half and reversed second half
       # - Alternate nodes from each half until second is done
       first = head
       second = prev
       while second.next:
           # Save next pointers
           tmp1 = first.next
           tmp2 = second.next
           # Link first → second
           first.next = second
           second.next = tmp1
           # Move pointers forward
           first = tmp1
           second = tmp2
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case [1,2,3,4] \rightarrow [1,4,2,3]
   n4 = ListNode(4)
   n3 = ListNode(3, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   sol.reorderList(n1)
   # Traverse and collect values
   res = []
   curr = n1
   while curr:
       res.append(curr.val)
       curr = curr.next
   print("Test 1:", res) # Expected: [1,4,2,3]
```

```
# Test 2: Odd length [1,2,3,4,5] \rightarrow [1,5,2,4,3]
n5 = ListNode(5)
n4 = ListNode(4, n5)
n3 = ListNode(3, n4)
n2 = ListNode(2, n3)
n1 = ListNode(1, n2)
sol.reorderList(n1)
res = []
curr = n1
while curr:
    res.append(curr.val)
    curr = curr.next
print("Test 2:", res) # Expected: [1,5,2,4,3]
# Test 3: Edge case [1] → [1]
n1 = ListNode(1)
sol.reorderList(n1)
res = [n1.val]
print("Test 3:", res) # Expected: [1]
```

Example Walkthrough

We'll walk through **Test 1**: $[1,2,3,4] \rightarrow [1,4,2,3]$.

Step 1: Find the middle

```
slow = fast = head (1)
Loop:

Iter 1: fast=1→3, slow=1→2
Iter 2: fast=3→None (since 3.next=4, 4.next=None) → stop
```

• slow now points to node $3 \rightarrow middle$ found.

Step 2: Reverse second half (3 → 4)

- Start: curr = 3, prev = None
- Iter 1:

$$-$$
 next_temp = 4

$$-$$
 3.next = None

$$-$$
 prev = 3, curr = 4

- Iter 2:
 - next_temp = None
 - -4.next = 3
 - prev = 4, curr = None \rightarrow stop
- Reversed list: 4 → 3 → None
- second = 4

Step 3: Merge first half (1-2-3) and reversed second (4-3)

Note: Original 2.next still points to 3, but we'll overwrite links.

- Initial: first = 1, second = 4
- Loop condition: $second.next = 3 \text{ (not None)} \rightarrow enter$

$$- tmp1 = first.next = 2$$

$$- tmp2 = second.next = 3$$

- first.next =
$$4 \rightarrow 1 \rightarrow 4$$

- second.next = tmp1 =
$$2 \rightarrow 4 \rightarrow 2$$

• Now: second.next = None \rightarrow loop ends

Final chain:

$$1 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow None$$

State after each merge step:

- After 1st link: 1→4, 4→2 (original 2→3 still exists but will be updated next)
- But since second.next becomes None after one merge (because reversed list ends at 3), we stop.
- The $2\rightarrow 3$ link remains, which is correct.

Complexity Analysis

• Time Complexity: O(n)

We traverse the list 3 times:

- 1. Find middle: n/2 steps
- 2. Reverse second half: n/2 steps
- 3. Merge: n/2 steps Total $1.5n \rightarrow 0(n)$
- Space Complexity: 0(1)

Only a few pointers (slow, fast, prev, curr, tmp1, tmp2) used. No recursion or extra data structures proportional to input size.

10. Odd Even Linked List

Pattern: Linked List Manipulation (Two Pointers / In-Place Rearrangement)

Given the head of a singly linked list, group all the nodes with odd indices together followed by the nodes with even indices, and return the reordered list.

The **first** node is considered **odd**, the **second** node is **even**, and so on.

Note that the relative order inside both the even and odd groups should remain as it was in the input.

You must solve the problem in O(1) extra space complexity and O(n) time complexity.

Sample Input & Output

```
Input: head = [1,2,3,4,5]
Output: [1,3,5,2,4]
Explanation: Odd-indexed nodes (1st, 3rd, 5th): 1→3→5.
Even-indexed (2nd, 4th): 2→4. Concatenate: 1→3→5→2→4.

Input: head = [2,1,3,5,6,4,7]
Output: [2,3,6,7,1,5,4]
Explanation: Odds: 2→3→6→7; Evens: 1→5→4 → combined as required.

Input: head = [1]
Output: [1]
Explanation: Single node - already satisfies condition.
```

```
from typing import Optional

# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
```

```
self.val = val
       self.next = next
class Solution:
   def oddEvenList(self, head: Optional[ListNode]) -> Optional[ListNode]:
       # STEP 1: Initialize structures
       # - If list is empty or has 1-2 nodes, no rearrangement needed.
       if not head or not head.next:
          return head
       # odd_head tracks start of odd list (1st node)
       # even_head tracks start of even list (2nd node)
       odd = head
       even = head.next
       even_head = even # Save head of even list for later linking
       # STEP 2: Main loop / recursion
       # - Traverse while both odd and even have valid next pointers
          - Maintain invariant: odd is always at an odd-indexed node,
           even at an even-indexed node.
       while even and even.next:
          # STEP 3: Update state / bookkeeping
          # - Link odd to next odd (skip one node)
          odd.next = even.next
           odd = odd.next
                               # Move odd pointer forward
          # - Link even to next even (skip one node)
          even.next = odd.next
          # STEP 4: Return result
       # - Connect tail of odd list to head of even list
       odd.next = even_head
       return head
# ----- INLINE TESTS -----
def list_to_linkedlist(arr):
   if not arr:
       return None
   head = ListNode(arr[0])
   curr = head
   for val in arr[1:]:
```

```
curr.next = ListNode(val)
       curr = curr.next
   return head
def linkedlist_to_list(head):
   result = []
   while head:
       result.append(head.val)
       head = head.next
   return result
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case
   head1 = list_to_linkedlist([1, 2, 3, 4, 5])
   result1 = sol.oddEvenList(head1)
   assert linkedlist_to_list(result1) == [1, 3, 5, 2, 4]
   print(" Test 1 passed")
   # Test 2: Edge case - single node
   head2 = list_to_linkedlist([1])
   result2 = sol.oddEvenList(head2)
   assert linkedlist_to_list(result2) == [1]
   print(" Test 2 passed")
   # Test 3: Tricky/negative - two nodes
   head3 = list_to_linkedlist([2, 1])
   result3 = sol.oddEvenList(head3)
   assert linkedlist_to_list(result3) == [2, 1]
   print(" Test 3 passed")
```

Example Walkthrough

Let's trace oddEvenList with input [1,2,3,4,5].

Initial Setup: - head points to node 1 - odd = head \rightarrow node 1 - even = head.next \rightarrow node 2 - even_head = even \rightarrow remembers node 2 (start of evens)

First Loop Iteration (even=2, even.next=3 \rightarrow truthy): - odd.next = even.next \rightarrow 1.next = 3 \rightarrow now 1 \rightarrow 3 - odd = odd.next \rightarrow odd = 3 - even.next = odd.next \rightarrow 2.next = 3.next = 4 \rightarrow now 2 \rightarrow 4 - even = even.next \rightarrow even = 4

State after iteration 1: - Odd list: 1 → 3 - Even list: 2 → 4 - odd = 3, even = 4

Second Loop Iteration (even=4, even.next=5 \rightarrow truthy): - odd.next = even.next \rightarrow 3.next = 5 \rightarrow now 3 \rightarrow 5 - odd = 5 - even.next = odd.next \rightarrow 4.next = 5.next = None - even = None

Loop ends because even is now None.

Final Step: - odd.next = even_head \rightarrow 5.next = node 2 - Full list: 1 \rightarrow 3 \rightarrow 5 \rightarrow 2 \rightarrow 4

Output: [1, 3, 5, 2, 4]

Key insight: We never create new nodes — just rewired pointers in place.

Complexity Analysis

• Time Complexity: O(n)

We traverse each node exactly once. The while loop runs $\sim n/2$ times, but each step processes two nodes \rightarrow total O(n).

• Space Complexity: 0(1)

Only a constant number of pointers (odd, even, even_head) are used. No recursion or auxiliary data structures.

11. Add Two Numbers

Pattern: Linked List Traversal + Elementary Math Simulation

You are given two **non-empty** linked lists representing two non-negative integers. The digits are stored in **reverse order**, and each of their nodes contains a single digit. Add the two numbers and return the sum as a linked list.

You may assume the two numbers do not contain any leading zero, except the number 0 itself.

Sample Input & Output

```
Input: 11 = [2,4,3], 12 = [5,6,4]
Output: [7,0,8]
Explanation: 342 + 465 = 807 → stored as [7,0,8] (reversed).

Input: 11 = [0], 12 = [0]
Output: [0]
Explanation: 0 + 0 = 0.

Input: 11 = [9,9,9,9,9,9,9], 12 = [9,9,9,9]
Output: [8,9,9,9,0,0,0,1]
Explanation: 9999999 + 9999 = 10009998 → reversed: [8,9,9,9,0,0,0,1].
```

```
from typing import Optional

# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next

class Solution:
```

```
def addTwoNumbers(
       self, 11: Optional[ListNode], 12: Optional[ListNode]
   ) -> Optional[ListNode]:
       # STEP 1: Initialize structures
       # - dummy head simplifies list construction
       # - carry tracks overflow from digit addition
       dummy = ListNode(0)
       curr = dummy
       carry = 0
       # STEP 2: Main loop / recursion
           - continue while either list has nodes or carry remains
       # - invariant: curr always points to last node of result
       while 11 or 12 or carry:
           # STEP 3: Update state / bookkeeping
           # - extract values (0 if list exhausted)
           # - compute total and new carry
           val1 = l1.val if l1 else 0
           val2 = 12.val if 12 else 0
           total = val1 + val2 + carry
           carry = total // 10
           digit = total % 10
           # Append new node with current digit
           curr.next = ListNode(digit)
           curr = curr.next
           # Advance input lists if possible
           if 11:
               11 = 11.next
           if 12:
               12 = 12.next
       # STEP 4: Return result
       # - skip dummy head; return actual start
       return dummy.next
# ----- HELPER FOR TESTING -----
def list_to_linkedlist(lst):
   dummy = ListNode(0)
   curr = dummy
   for val in 1st:
```

```
curr.next = ListNode(val)
       curr = curr.next
   return dummy.next
def linkedlist_to_list(head):
   result = []
   while head:
       result.append(head.val)
       head = head.next
   return result
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case
   11 = list_to_linkedlist([2, 4, 3])
   12 = list_to_linkedlist([5, 6, 4])
   res = sol.addTwoNumbers(11, 12)
   print(linkedlist_to_list(res)) # Expected: [7, 0, 8]
   # Test 2: Edge case (both zero)
   11 = list_to_linkedlist([0])
   12 = list_to_linkedlist([0])
   res = sol.addTwoNumbers(11, 12)
   print(linkedlist_to_list(res)) # Expected: [0]
   # Test 3: Tricky/negative (carry propagates)
   11 = list_to_linkedlist([9,9,9,9,9,9,9])
   12 = list_to_linkedlist([9,9,9,9])
   res = sol.addTwoNumbers(11, 12)
   print(linkedlist_to_list(res)) # Expected: [8,9,9,9,0,0,0,1]
```

Example Walkthrough

We'll trace Test 1: 11 = [2,4,3], 12 = [5,6,4]

Initial state:

- dummy = ListNode(0)
- \mathtt{curr} = $\mathtt{dummy} \to \mathrm{points}$ to dummy
- -carry = 0
- 11 \rightarrow 2 \rightarrow 4 \rightarrow 3
- 12 \rightarrow 5 \rightarrow 6 \rightarrow 4

Iteration 1:

- val1 = 2, val2 = 5
- total = 2 + 5 + 0 = 7
- carry = 7 // 10 = 0
- -digit = 7 % 10 = 7
- Create ListNode(7), attach to curr.next
- curr moves to node 7
- Advance 11 \rightarrow 4, 12 \rightarrow 6
- Result so far: dummy $\rightarrow 7$

Iteration 2:

- val1 = 4, val2 = 6
- total = 4 + 6 + 0 = 10
- carry = 10 // 10 = 1
- digit = 10 % 10 = 0
- Create ListNode(0), attach
- curr moves to node 0
- Advance 11 \rightarrow 3, 12 \rightarrow 4
- Result so far: dummy $\rightarrow 7 \rightarrow 0$

Iteration 3:

- val1 = 3, val2 = 4
- total = 3 + 4 + 1 = 8
- carry = 8 // 10 = 0
- -digit = 8
- Create ListNode(8), attach
- curr moves to node 8
- Advance 11 = None, 12 = None
- Result so far: dummy $\rightarrow 7 \rightarrow 0 \rightarrow 8$

Loop condition check:

-11 = None, 12 = None, carry = $0 \rightarrow \text{exit loop}$

Return: dummy.next \rightarrow head of [7,0,8]

Final output: [7, 0, 8]

Key insight:

We simulate elementary addition **digit by digit**, propagating carry just like manual math—no need to reverse lists or convert to integers!

Complexity Analysis

• Time Complexity: O(max(m, n))

We traverse both lists once, where ${\tt m}$ and ${\tt n}$ are their lengths. Each node is visited at most once.

• Space Complexity: O(max(m, n))

The output list's length is at most max(m, n) + 1 (due to final carry). No extra space beyond result.

12. Sort List

Pattern: Divide and Conquer (Merge Sort on Linked List)

Problem Statement

Given the head of a linked list, return the list after sorting it in ascending order. You must solve it in O(n log n) time complexity and O(1) space complexity (i.e., iterative or bottom-up merge sort preferred, but top-down with recursion is acceptable if space is O(log n) due to call stack).

Sample Input & Output

Input: head = [4,2,1,3]
Output: [1,2,3,4]

Explanation: The list is sorted in ascending order.

```
Input: head = [-1,5,3,4,0]
Output: [-1,0,3,4,5]
Explanation: Handles negative numbers and zero correctly.

Input: head = []
Output: []
Explanation: Empty list remains empty.
```

```
from typing import Optional
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next
class Solution:
    def sortList(self, head: Optional[ListNode]) -> Optional[ListNode]:
        # STEP 1: Base case - empty or single-node list
        # - Already sorted; return as-is.
        if not head or not head.next:
            return head
        # STEP 2: Split list into two halves using slow/fast pointers
        # - Fast moves 2 steps, slow moves 1 \rightarrow slow ends at mid.
        slow, fast = head, head.next
        while fast and fast.next:
            slow = slow.next
            fast = fast.next.next
        # Break the list into left and right halves
        mid = slow.next
        slow.next = None # Terminate left half
        # STEP 3: Recursively sort both halves
```

```
# - Divide until base case reached.
       left = self.sortList(head)
       right = self.sortList(mid)
       # STEP 4: Merge two sorted halves
       # - Classic merge of two sorted linked lists.
       dummy = ListNode(0)
       tail = dummy
       while left and right:
           if left.val < right.val:</pre>
               tail.next = left
               left = left.next
           else:
               tail.next = right
               right = right.next
           tail = tail.next
       # Attach remaining nodes (one side is always exhausted)
       tail.next = left or right
       return dummy.next
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case
   # Build [4,2,1,3]
   n4 = ListNode(3)
   n3 = ListNode(1, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(4, n2)
   res = sol.sortList(n1)
   out = []
   while res:
       out.append(res.val)
       res = res.next
   print("Test 1:", out == [1,2,3,4])
   # Test 2: Edge case - empty list
   print("Test 2:", sol.sortList(None) is None)
```

```
# Test 3: Tricky/negative - unsorted with negatives
# Build [-1,5,3,4,0]
n5 = ListNode(0)
n4 = ListNode(4, n5)
n3 = ListNode(3, n4)
n2 = ListNode(5, n3)
n1 = ListNode(-1, n2)
res = sol.sortList(n1)
out = []
while res:
    out.append(res.val)
    res = res.next
print("Test 3:", out == [-1,0,3,4,5])
```

Example Walkthrough

We'll walk through **Test 1**: input [4,2,1,3].

- 1. Initial Call: sortList([4→2→1→3])
 - Not base case \rightarrow find midpoint.
 - slow=4, fast=2 \rightarrow then slow=2, fast=1 \rightarrow then fast.next is 3, so loop ends.
 - mid = slow.next = 1, and slow.next = None \rightarrow splits into [4 \rightarrow 2] and [1 \rightarrow 3].
- 2. Recursive Left: sortList([4→2])
 - Split: slow=4, $fast=2 \rightarrow fast.next$ is None, so stop.
 - mid = 2, left = [4], right = [2].
 - Both base cases \rightarrow merge: $2\rightarrow 4$.
- 3. Recursive Right: sortList([1→3])
 - Split into [1] and [3] \rightarrow merge \rightarrow 1 \rightarrow 3.
- 4. Merge Left $(2\rightarrow 4)$ and Right $(1\rightarrow 3)$

- Compare 2 vs $1 \rightarrow \text{pick } 1$
- Compare 2 vs $3 \rightarrow \text{pick 2}$
- Compare 4 vs $3 \rightarrow \text{pick } 3$
- Append remaining 4
- Result: $1\rightarrow 2\rightarrow 3\rightarrow 4$

Final output: $[1,2,3,4] \rightarrow \text{matches expected}$.

Complexity Analysis

• Time Complexity: O(n log n)

The list is divided in half log n times (like merge sort). Each merge step processes all n nodes once \rightarrow total O(n log n).

• Space Complexity: O(log n)

Due to recursion depth (call stack). Each recursive call uses constant extra space, but there are log n active calls during divide phase.

Note: LeetCode accepts this as it's better than O(n) and meets typical expectations for linked list merge sort.

13. Reverse Nodes in k-Group

Pattern: Linked List Manipulation + Recursion / Iteration with Grouping

Given the head of a linked list, reverse the nodes of the list k at a time, and return the modified list.

 ${\tt k}$ is a positive integer and is less than or equal to the length of the linked list. If the number of nodes is not a multiple of ${\tt k}$, then left-out nodes, in the end, should remain as they are.

You may not alter the values in the list's nodes — only nodes themselves may be changed.

Sample Input & Output

```
Input: head = [1,2,3,4,5], k = 2
Output: [2,1,4,3,5]
Explanation: Reverse first 2 → [2,1]; next 2 → [4,3]; last node 5 remains.

Input: head = [1,2,3,4,5], k = 3
Output: [3,2,1,4,5]
Explanation: Reverse first 3 → [3,2,1]; remaining 2 nodes < k → unchanged.

Input: head = [1], k = 1
Output: [1]
Explanation: Single node, k=1 → reverse group of 1 (no change).</pre>
```

```
from typing import Optional

# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
```

```
self.next = next
class Solution:
   def reverseKGroup(
       self, head: Optional[ListNode], k: int
   ) -> Optional[ListNode]:
       # STEP 1: Initialize structures
       # - Use dummy node to simplify head handling
       # - 'group_prev' tracks node before current group
       dummy = ListNode(0)
       dummy.next = head
       group_prev = dummy
       while True:
           # STEP 2: Check if k nodes exist ahead
           # - 'kth' will point to kth node in current group
           kth = self._get_kth_node(group_prev, k)
           if not kth:
               break # Not enough nodes to reverse → stop
           # Save pointers around the group
           group_next = kth.next
           prev = group_next
           curr = group_prev.next
           # STEP 3: Reverse the k-node segment
           # - Standard reversal, but stop after k nodes
           while curr != group_next:
               tmp = curr.next
               curr.next = prev
               prev = curr
               curr = tmp
           # STEP 4: Reconnect reversed group
           # - Update group_prev.next to new head (prev)
           # - Move group_prev to end of reversed group
           tmp = group_prev.next
           group_prev.next = kth
           group_prev = tmp
       return dummy.next
```

```
def _get_kth_node(
       self, node: ListNode, k: int
   ) -> Optional[ListNode]:
       # Helper: move k steps from 'node'
       while node and k > 0:
           node = node.next
           k -= 1
       return node
# ----- INLINE TESTS -----
if __name__ == "__main__":
   sol = Solution()
   # Test 1: Normal case
   # Build [1,2,3,4,5]
   n5 = ListNode(5)
   n4 = ListNode(4, n5)
   n3 = ListNode(3, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   res = sol.reverseKGroup(n1, 2)
   out = []
   while res:
       out.append(res.val)
       res = res.next
   print("Test 1:", out) # Expected: [2,1,4,3,5]
   # Test 2: Edge case (k = 3)
   n5 = ListNode(5)
   n4 = ListNode(4, n5)
   n3 = ListNode(3, n4)
   n2 = ListNode(2, n3)
   n1 = ListNode(1, n2)
   res = sol.reverseKGroup(n1, 3)
   out = []
   while res:
       out.append(res.val)
       res = res.next
   print("Test 2:", out) # Expected: [3,2,1,4,5]
   # Test 3: Tricky/negative (k = 1)
   n1 = ListNode(1)
```

```
res = sol.reverseKGroup(n1, 1)
out = []
while res:
    out.append(res.val)
    res = res.next
print("Test 3:", out) # Expected: [1]
```

Example Walkthrough

We'll walk through **Test 1**: head = [1,2,3,4,5], k = 2.

Initial Setup

- Dummy node created: dummy \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5
- group_prev = dummy (points to node before group)

First Group (nodes 1,2)

- 1. Find kth node: $_{get_kth_node(dummy, 2)} \rightarrow returns node 2$.
- 2. group_next = 2.next = 3
- 3. Start reversal:
 - prev = 3, curr = 1
 - Loop:

```
- curr=1: 1.next = 3 \rightarrow prev=1, curr=2
- curr=2: 2.next = 1 \rightarrow prev=2, curr=3 \rightarrow stop (curr == group_next)
```

- 4. Reconnect:
 - group_prev.next (dummy.next) = 2 → now dummy → 2 → 1 → 3...
 - group_prev = old head = 1 (now tail of reversed group)

Second Group (nodes 3,4)

- 1. $_{get_kth_node(1, 2)} \rightarrow _{returns node 4}$
- 2. group_next = 5
- 3. Reverse:
 - prev = 5, curr = 3
 - 3.next = 5, prev=3, curr=4
 - 4.next = 3, prev=4, curr=5 \rightarrow stop
- 4. Reconnect:
 - 1.next = $4 \rightarrow \text{list: } 2 \rightarrow 1 \rightarrow 4 \rightarrow 3 \rightarrow 5$
 - group_prev = 3

Third Group (node 5)

- 1. _get_kth_node(3, 2) \rightarrow tries to move 2 steps: 3-5-None \rightarrow returns None
- 2. Break loop → return dummy.next = 2

Final Output: [2,1,4,3,5]

Complexity Analysis

• Time Complexity: O(n)

Each node is visited a constant number of times: once to check group size, once to reverse, and once during reconnection. Total $\sim 3n \rightarrow O(n)$.

• Space Complexity: 0(1)

Only a few pointers (dummy, group_prev, kth, prev, curr, etc.) are used. No recursion stack or extra data structures proportional to input size.

14. LRU Cache

Pattern: Hash Map + Doubly Linked List (Ordered Data Structure)

Design a data structure that follows the constraints of a **Least Recently Used** (LRU) cache.

Implement the LRUCache class: - LRUCache(int capacity) Initialize the LRU cache with **positive** size capacity. - int get(int key) Return the value of the key if it exists, otherwise return -1. - void put(int key, int value) Update the value of the key if it exists. Otherwise, add the key-value pair to the cache. If the number of keys exceeds capacity, evict the least recently used key.

Follow up: Could you do this in O(1) time complexity for both get and put?

Sample Input & Output

Edge Case:

```
Input: ["LRUCache", "get", "put", "get"]
       [[1], [1], [1, 2], [1]]
Output: [null, -1, null, 2]
```

Tricky Case (Update existing key):

```
Input: ["LRUCache", "put", "put", "get"]
        [[2], [1,1], [2,2], [1,3], [1]]
Output: [null, null, null, null, 3]
Explanation: Updating key 1 should refresh its recency.
```

```
class Node:
   def __init__(self, key: int, val: int):
       self.key = key
       self.val = val
       self.prev = None
       self.next = None
class LRUCache:
   def __init__(self, capacity: int):
       # STEP 1: Initialize structures
       # - Use dummy head/tail to simplify edge logic
       # - Hash map for O(1) key lookup
           - DLL maintains recency order (head = MRU, tail = LRU)
       self.capacity = capacity
       self.cache = {}
       self.head = Node(0, 0) # dummy head
       self.tail = Node(0, 0) # dummy tail
       self.head.next = self.tail
       self.tail.prev = self.head
   def _remove(self, node: Node) -> None:
       # Remove node from DLL
       prev_node = node.prev
       next_node = node.next
       prev_node.next = next_node
       next_node.prev = prev_node
   def _add_to_head(self, node: Node) -> None:
       # Add node right after head (MRU position)
       node.prev = self.head
       node.next = self.head.next
```

```
self.head.next.prev = node
       self.head.next = node
   def get(self, key: int) -> int:
       # STEP 2: Main logic for get
       # - If key exists, move node to MRU and return val
       if key in self.cache:
           node = self.cache[key]
           self._remove(node)
           self._add_to_head(node)
           return node.val
       return -1
   def put(self, key: int, value: int) -> None:
       # STEP 3: Main logic for put
       # - If key exists: update and move to MRU
       # - Else: add new node; evict LRU if over capacity
       if key in self.cache:
           node = self.cache[key]
           node.val = value
           self._remove(node)
           self._add_to_head(node)
       else:
           new_node = Node(key, value)
           self.cache[key] = new_node
           self._add_to_head(new_node)
           if len(self.cache) > self.capacity:
               # Evict LRU (node before dummy tail)
               lru_node = self.tail.prev
               self._remove(lru_node)
               del self.cache[lru_node.key]
# ------ INLINE TESTS ------
if __name__ == "__main__":
   sol = None
   # Test 1: Normal case
   sol = LRUCache(2)
   sol.put(1, 1)
   sol.put(2, 2)
   assert sol.get(1) == 1
   sol.put(3, 3)
```

```
assert sol.get(2) == -1
sol.put(4, 4)
assert sol.get(1) == -1
assert sol.get(3) == 3
assert sol.get(4) == 4
print(" Test 1 passed")
# Test 2: Edge case (capacity = 1)
sol = LRUCache(1)
assert sol.get(1) == -1
sol.put(1, 2)
assert sol.get(1) == 2
print(" Test 2 passed")
# Test 3: Tricky case (update existing key)
sol = LRUCache(2)
sol.put(1, 1)
sol.put(2, 2)
sol.put(1, 3) # update key 1
assert sol.get(1) == 3
assert len(sol.cache) == 2
print(" Test 3 passed")
```

Example Walkthrough

We'll walk through **Test 3** step by step:

- 1. sol = LRUCache(2)
 - Creates cache with capacity 2.
 - head tail (dummy nodes).
 - cache = {}.
- 2. sol.put(1, 1)

- Key 1 not in cache \rightarrow create Node(1,1).
- Add to head: head [1] tail.
- cache = {1: node1}.
- 3. sol.put(2, 2)
 - Key 2 not in cache \rightarrow create Node(2,2).
 - Add to head: head [2] [1] tail.
 - cache = {1: node1, 2: node2}.
- 4. sol.put(1, 3)
 - Key 1 exists \rightarrow update node1.val = 3.
 - Remove node1 from current position: head [2] tail (temporarily).
 - Add node1 to head: head [1] [2] tail.
 - Now 1 is MRU, 2 is LRU.
 - cache still has 2 keys.
- 5. sol.get(1)
 - Found in cache \rightarrow return 3.
 - Already at head \rightarrow no structural change.

Final state:

- DLL: head [1] [2] tail
- -cache = $\{1: Node(1,3), 2: Node(2,2)\}$
- Output: 3

Key takeaway: Updating or accessing a key moves it to front, ensuring LRU eviction works correctly.

Complexity Analysis

• Time Complexity: 0(1)

Both get and put use hash map lookup (O(1)) and doubly linked list insert/remove (O(1)) due to direct node access via pointers).

• Space Complexity: O(capacity)

The cache stores at most capacity key-node pairs. The DLL and hash map scale linearly with the number of stored keys.