

Related work

# Adversarial Label Flips

Matthias Dellago & Maximilian Samsinger

June 10, 2021

### 1 Notation

We denote neural network classifiers as  $f_{\theta} \colon \mathcal{X} \to \mathcal{Y}, x \mapsto y$  with trainable parameter  $\theta$ .  $\mathcal{X}$  is a set of images with corresponding labels (classes)  $\mathcal{Y}$ . The parameter  $\theta$  is optimized by minimizing a training objective  $(\theta, x, y) \mapsto J(\theta, x, y)$  with respect to  $\theta$ .

#### 2 On neural networks

Convolutional neural networks are the de facto standard in computer vision related tasks. They were first introduced in [1] to classify handwritten digits. In [2], Krizhevsky et al. demonstrated the effectiveness of deep convolutional neural networks on ImageNet dataset [3], winning the ImageNet Large Scale Visual Recognition Challenge 2012 [4]. The architecture of convolutional neural networks has since been further optimized. Residual neural networks [5] and their variants are state-of-the-art for image recognition tasks and dominate the leaderboard on websites such as https://paperswithcode.com/task/image-classification.

**Experiments** For our experiments we will consider the MNIST [6], Fashion-MNIST [7] and CIFAR-10 [8] datasets. For MNIST and Fashion-MNIST we will use the convolutional neural network described in [9], Table 1. For CIFAR-10 we may use a ResNet-18 architecture [5] with the "pre-activation" optimization [10].

## 3 On adversarial attacks

Deep neural networks have been shown to be vulnerable to tiny, maliciously crafted perturbations applied to otherwise benign inputs. These so-called "adversarial examples" were first introduced in [11]. Further research showed that these adversarial examples generalize over multiple datasets and architectures [12]. Even very inexpensive attacks like the Fast Gradient Sign Method (FGSM) [12] can be used to fool neural networks. FGSM requires white-box access to the targeted neural networks architecture and its weights. Adversarial examples are computed by performing a gradient ascent step with respect to the sign of the gradient

$$FGSM_{\epsilon}(x) = x + \epsilon \operatorname{sign}(\nabla_x J(\theta, x, y))$$

given a step size  $\epsilon > 0$ . FGSM is an  $L^{\infty}$ -bounded attack<sup>1</sup>, i.e.  $||x - \text{FGSM}_{\epsilon}(x)||_{\infty} \le \epsilon$ , meaning that each pixel value of a benign image x may only be perturbed by up to  $\epsilon$ . Stronger attacks can be computed by repeatedly applying FGSM with smaller step sizes. This type of attack is known as Projected Gradient

<sup>&</sup>lt;sup>1</sup>While bounds with respect to an  $L^p$  norm are commonly used in the machine learning literature, we are aware that they are "[...] neither necessary nor sufficient for perceptual similarity [...]" [13].

Descent (PGD) and was first introduced [14]. Their experiments demonstrated the effectiveness of such attacks and showed that convergence is achieved after only a few hundred iterations or less.

Foolbox For our experiments we will use a suite of different attacks using the FoolBox library [15]. The documentation is available at https://foolbox.readthedocs.io/en/stable/.

#### References

- [1] Yann LeCun, Bernhard Boser, John S Denker, Donnie Henderson, Richard E Howard, Wayne Hubbard, and Lawrence D Jackel. Backpropagation applied to handwritten zip code recognition. *Neural computation*, 1(4):541–551, 1989.
- [2] Alex Krizhevsky, Ilya Sutskever, and Geoffrey E Hinton. Imagenet classification with deep convolutional neural networks. In *Advances in Neural Information Processing Systems*, pages 1097–1105, 2012.
- [3] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *IEEE Conference on Computer Vision and Pattern Recognition*, pages 248–255, 2009.
- [4] Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, Alexander C. Berg, and Li Fei-Fei. ImageNet Large Scale Visual Recognition Challenge. *International Journal of Computer Vision (IJCV)*, 115(3):211–252, 2015.
- [5] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 770–778, 2016.
- [6] Li Deng. The mnist database of handwritten digit images for machine learning research [best of the web]. *IEEE Signal Processing Magazine*, 29(6):141–142, 2012.
- [7] Han Xiao, Kashif Rasul, and Roland Vollgraf. Fashion-mnist: a novel image dataset for benchmarking machine learning algorithms. arXiv preprint arXiv:1708.07747, 2017.
- [8] Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. Master's thesis, University of Toronto.
- [9] Nicholas Carlini and David Wagner. Towards evaluating the robustness of neural networks. In 2017 IEEE Symposium on Security and Privacy (SP), pages 39–57. IEEE, 2017.

- [10] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Identity mappings in deep residual networks. In *European Conference on Computer Vision*, pages 630–645. Springer, 2016.
- [11] Christian Szegedy, Wojciech Zaremba, Ilya Sutskever, Joan Bruna, Dumitru Erhan, Ian Goodfellow, and Rob Fergus. Intriguing properties of neural networks. In *International Conference on Learning Representations (ICLR)*, 2014.
- [12] Ian J Goodfellow, Jonathon Shlens, and Christian Szegedy. Explaining and harnessing adversarial examples. arXiv preprint arXiv:1412.6572, 2014.
- [13] Mahmood Sharif, Lujo Bauer, and Michael K Reiter. On the suitability of lp-norms for creating and preventing adversarial examples. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition Workshops, pages 1605–1613, 2018.
- [14] Aleksander Madry, Aleksandar Makelov, Ludwig Schmidt, Dimitris Tsipras, and Adrian Vladu. Towards deep learning models resistant to adversarial attacks. arXiv preprint arXiv:1706.06083, 2017.
- [15] Jonas Rauber, Wieland Brendel, and Matthias Bethge. Foolbox: A python toolbox to benchmark the robustness of machine learning models. arXiv preprint arXiv:1707.04131, 2017.