



Related work

# Adversarial Label Flips

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## 1 Notation

We denote neural network classifiers with  $f_\theta: \mathcal{X} \rightarrow \mathcal{Y}, x \mapsto y$  with trainable parameter  $\theta$ , where  $\mathcal{X}$  are a set of images with corresponding labels (classes)  $\mathcal{Y}$ . The parameter  $\theta$  are optimized by minimizing a training objective  $(\theta, x, y) \mapsto J(\theta, x, y)$  with respect to  $\theta$ .

## 2 On neural networks

Convolutional neural networks are the de-facto standard in computer vision related tasks. They were first introduced in [1] to classify hand-written digits. In [2] demonstrated the effectiveness of deep convolutional neural networks on ImageNet dataset [3], winning the ImageNet Large Scale Visual Recognition Challenge 2012 [4]. The architecture of convolutional neural networks has since been further optimized. Residual neural networks [5] are state-of-the-art for image recognition tasks.

**Experiments** For our experiments we will consider the MNIST [6], Fashion-MNIST [7] and CIFAR-10 [8] dataset. For MNIST and Fashion-MNIST we use the convolutional neural networks described in [9], Table 1. For CIFAR-10 we may use a ResNet-18 architecture [5] with the "pre-activation" optimization [10].

## 3 On adversarial attacks

Deep neural networks have been shown to be vulnerable to tiny, maliciously crafted perturbations applied to otherwise benign inputs. These so-called "adversarial examples" were first introduced in [11]. Further research [12] showed that these adversarial examples generalize over multiple dataset and architectures. Even very inexpensive attacks like the Fast Gradient Sign Method (FGSM) [12] can be used to fool neural networks. FGSM requires white-box access to the targeted neural networks architecture and its weights. Adversarial examples are computed by performing a gradient ascent step with respect to the sign of the gradient

$$\text{FGSM}_\epsilon(x) = x + \epsilon \text{sign}(\nabla_x J(\theta, x, y))$$

given a step size  $\epsilon$ . FGSM is an  $L^\infty$ -bounded attack<sup>1</sup>, i.e.  $\|x - \text{FGSM}_\epsilon(x)\|_\infty \leq \epsilon$ , meaning that each pixel value of a benign image  $x$  may only be perturbed by up to  $\epsilon$ . Stronger attacks can be computed by repeatedly applying FGSM with smaller step sizes. This type of attack is known as Projected Gradient Descent (PGD) and was first introduced [14]. Their experiments demonstrated the effectiveness of such attacks and showed that convergence is achieved after only a few hundred iterations.

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<sup>1</sup>While bounds with respect to an  $L^p$  norm are commonly used in the machine learning literature, we are aware that they are "[...] neither necessary nor sufficient for perceptual similarity [...]" [13].

**Foolbox** For our experiments we will use a suit of different attacks using the FoolBox library [15]. The documentation is available at <https://foolbox.readthedocs.io/en/stable/>.

## References

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