

Audio Math

Fundamental Signal RMS Voltage

The RMS voltage at the fundamental frequency is simply the height of the fundamental frequency's bin in the FFT.

V @ Frequency

Signal RMS Voltage

The RMS voltage is calculated one of two ways. For time domain data it's just the RMS definition

$$V_{RMS} = \frac{\sqrt{\left(\sum_{t=0}^T V_t^2 \right)}}{n}$$

For bandlimited frequency data it's a bit different since frequencies values are like densities.

$$V_{RMS} = \frac{\sqrt{\left(\sum_{f_{min}}^{f_{max}} V_f^2 \right)}}{ENBW(windowing)}$$

ENBW is the equivalent noise bandwidth of the fft windowing method. In some ways it's a measure of how much the signal is smeared into adjacent channels. It can be calculated by

$$ENBW = \frac{\sqrt{\left(\sum_{t=0}^T W_t^2 \right)}}{\left(\sum_{t=0}^T W_t \right)}$$

Where W_t is the fft weight at time t . Note this is scale-independent of the weights.

Intermodulation Distortion

CCIF style math for IMD

When close together fundamentals ($f_H/f_L < 2$) use the 2nd order CCIF2 or 3rd order CCIF3.
QA40xPlot uses CCIF3.

CCIF2 uses a single value

$$\text{CCIF2 IMD} = \frac{V_{f_H - f_L}}{V_{f_H} + V_{f_L}}$$

CCIF3 uses a different single value

$$\text{CCIF3 IMD} = \frac{\sqrt{V_{f_H - f_L}^2 + (V_{2f_L - f_H} + V_{2f_H - f_L})^2}}{V_{f_H} + V_{f_L}}$$

SMPTE/DIN IMD (or MOD IMD)

When the fundamentals are far apart ($f_H/f_L > 7$) use SMPTE/DIN math

$$\text{SMPTE/DIN IMD} = \frac{\sqrt{(V_{f_H - f_L} + V_{f_H + f_L})^2 + (V_{f_H - 2f_L} + V_{f_H + 2f_L})^2}}{V_{f_H}}$$

RMS Power IMD

Finally, when $2 < f_H/f_L < 7$ use IMD RMS power methods using RMS addition

$$\text{POWER IMD} = \frac{\sqrt{V_{f_H - f}^2 + V_{f_H + f}^2 + V_{f_L - 2f}^2 + V_{f_L + 2f}^2 + V_{f_H - 2f_L}^2 + V_{f_H + 2f_L}^2}}{\sqrt{V_{f_H}^2 + V_{f_L}^2}}$$