

# Audio Math

## Fundamental Signal RMS Voltage

The RMS voltage is calculated one of two ways. For time domain data it's just the RMS definition

$$V_{RMS} = \frac{\sqrt{\left(\sum_{t=0}^T V_t^2\right)}}{n}$$

For frequency data it's a bit different since frequencies values are like densities.

$$V_{RMS} = \frac{\sqrt{\left(\sum_{f_{min}}^{f_{max}} V_f^2\right)}}{ENBW(windowing)}$$

**ENBW** is the equivalent noise bandwidth of the fft windowing method. In some ways it's a measure of how much the signal is smeared into adjacent channels. It can be calculated by

$$ENBW = \frac{\sqrt{\left(\sum_{t=0}^T W_t^2\right)}}{\left(\sum_{t=0}^T W_t\right)}$$

Where  $W_t$  is the fft weight at time  $t$ . Note this is scale-independent of the weights.

## Intermodulation Distortion

### CCIF style math for IMD

When close together fundamentals ( $f_H/f_L < 2$ ) use the 2<sup>nd</sup> order CCIF2 or 3<sup>rd</sup> order CCIF3. QA40xPlot uses CCIF3.

CCIF2 uses a single value

$$\text{CCIF2 IMD} = \frac{V_{f_H-f_L}}{V_{f_H}+V_{f_L}}$$

CCIF3 uses a different single value

$$\text{CCIF3 IMD} = \frac{\sqrt{V_{f_H-f_L}^2 + (V_{2f_L-f_H} + V_{2f_H-f_L})^2}}{V_{f_H}+V_{f_L}}$$

## SMPTE/DIN IMD (or MOD IMD)

When the fundamentals are far apart ( $f_H/f_L > 7$ ) use SMPTE/DIN math

$$\text{SMPTE/DIN IMD} = \frac{\sqrt{(V_{f_H-f_L} + V_{f_H+f_L})^2 + (V_{f_H-2f_L} + V_{f_H+2f_L})^2}}{V_{f_H}}$$

## RMS Power IMD

Finally, when  $2 < f_H/f_L < 7$  use IMD RMS power methods using RMS addition

$$\text{POWER IMD} = \frac{\sqrt{V_{f_H-f_L}^2 + V_{f_H+f_L}^2 + V_{f_L-2f_H}^2 + V_{f_L+2f_H}^2 + V_{f_H-2f_L}^2 + V_{f_H+2f_L}^2}}{\sqrt{V_{f_H}^2 + V_{f_L}^2}}$$