



$$\cancel{y} \in \mathbb{R}^N \quad y, z, x \in \mathbb{R}^N$$

$$\frac{\partial L}{\partial y} = \begin{bmatrix} \partial L / \partial y_1 \\ \vdots \\ \partial L / \partial y_N \end{bmatrix} \quad \frac{\partial L}{\partial z_i} = \left(\frac{\partial L}{\partial y} \right)^T \left(\frac{\partial y}{\partial z_i} \right)$$

matrix

$$\begin{bmatrix} \partial L / \partial y_1 \\ \vdots \\ \partial L / \partial y_N \end{bmatrix} \quad \begin{bmatrix} \partial y_1 / \partial z_i \\ \vdots \\ \partial y_N / \partial z_i \end{bmatrix}$$

$$\frac{\partial L}{\partial z} = \left(\frac{\partial L}{\partial y} \right)^T \frac{\partial y}{\partial z}$$

(1xN) (N x N)

$$\begin{bmatrix} \partial y_1 / \partial z_1 & \dots & \partial y_1 / \partial z_N \\ \vdots & \ddots & \vdots \\ \partial y_N / \partial z_1 & \dots & \partial y_N / \partial z_N \end{bmatrix}$$

$$(1 \times N) * (N \times N) = (1 \times N)$$