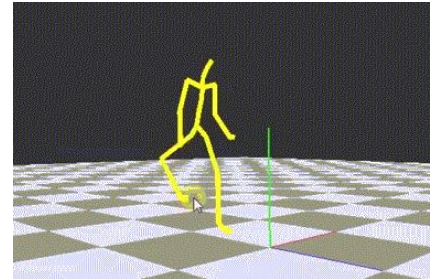
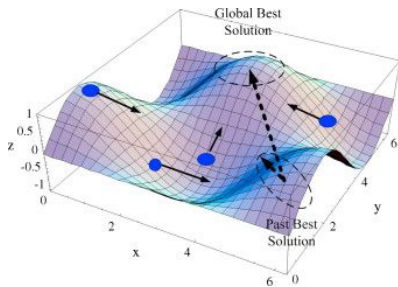


# Parallel Particle Swarm Optimization on Inverse kinematics

第六組

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劉禮榮 10967241



# Outline

Introduction to Inverse Kinematics

Introduction to Particle Swarm Optimization

Related Work

Parallel Particle Swarm Optimization

Experiment

Demo

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# Outline

## Introduction to Inverse Kinematic

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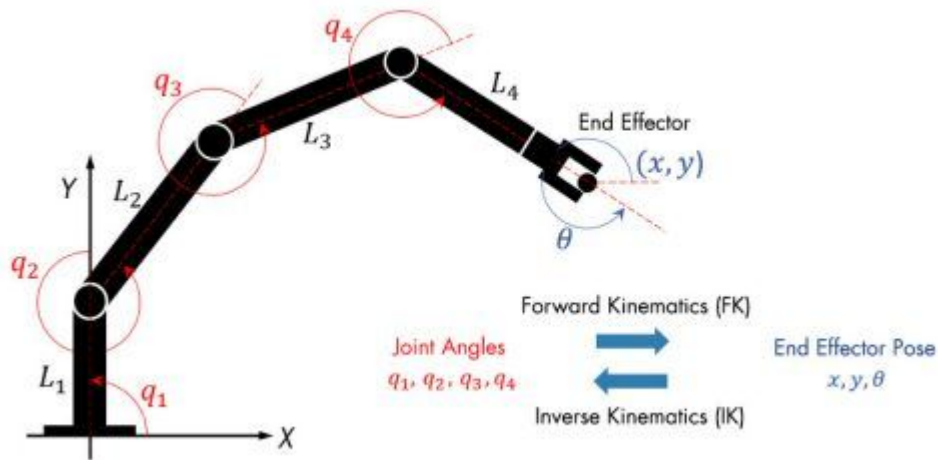
Conclusion and Future work

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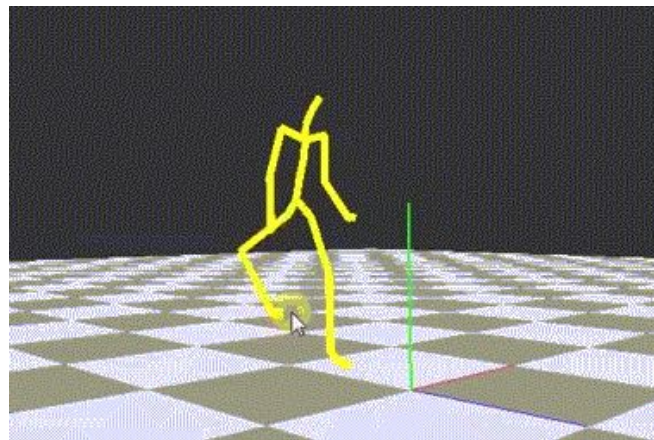
# Introduction to Inverse Kinematics

## [Neutrino's Blog: 電腦動畫中的反向動力法 \(Inverse Kinematics\)](#)

> 常見的方法包含 Cyclic Coordinate Descent 方法、Jacobian Pseudoinverse 方法、Jacobian Transpose 方法、Levenberg-Marquardt Damped Least Squares 方法、Quasi-Newton and Conjugate Gradient 方法、神經網路方法



<https://www.mathworks.com/discovery/inverse-kinematics.html>



<https://nagachiang.github.io/assets/images/IK.gif>

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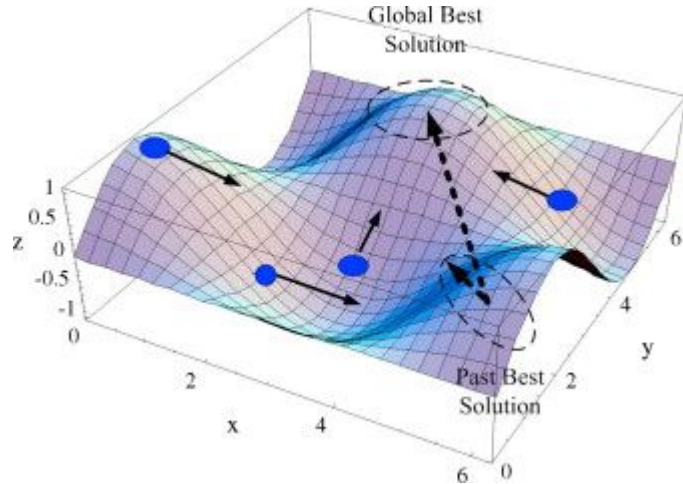
Conclusion and Future work

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# Introduction to Particle Swarm Optimization

$$V_{ij}^{t+1} = wV_{ij}^t + c_1r_1^t(pbest_{ij} - X_{ij}^t) + c_2r_2^t(gbest_j - X_{ij}^t)$$

$$X_{ij}^{t+1} = X_{ij}^t + V_{ij}^{t+1}$$



## 1. Initialization

1.1. For each particle  $i$  in a swarm population size  $P$ :

1.1.1. Initialize  $X_i$  randomly

1.1.2. Initialize  $V_i$  randomly

1.1.3. Evaluate the fitness  $f(X_i)$

1.1.4. Initialize  $pbest_i$  with a copy of  $X_i$

1.2. Initialize  $gbest$  with a copy of  $X_i$  with the best fitness

## 2. Repeat until a stopping criterion is satisfied:

2.1. For each particle  $i$ :

2.1.1. Update  $V_i^t$  and  $X_i^t$  according to Eqs. (1) and (2)

2.1.2. Evaluate the fitness  $f(X_i^t)$

2.1.3.  $pbest_i \leftarrow X_i^t$  if  $f(pbest_i) < f(X_i^t)$

2.1.4.  $gbest \leftarrow X_i^t$  if  $f(gbest) < f(X_i^t)$

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# Related Work

Parallel global optimization with the particle swarm algorithm, by J. F. Schutte , J. A. Reinbolt.

Int J Numer Methods Eng. 2004 December 7

Particle swarm optimization within the CUDA architecture, by Luca Mussi, Stefano Cagn

, Conference: Genetic and Evolutionary Computation Conference - GECCO 2009

Parallel asynchronous particle swarm optimization, by Byung-II Koh , Alan D. George. Int J

Numer Methods Eng. 2006 July 23

## 1. Initialization

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1.2. Initialize  $gbest$  with a copy of  $X_i$  with the best fitness



# Related Work

- Master processor
  1. Initializes all optimization parameters and particle positions and velocities;
  2. Holds a queue of particles for slave processors to evaluate;
  3. Updates particle positions and velocities based on currently available information  $p^i, p^g$ ;
  4. Sends the position  $x^i$  of the next particle in the queue to an available slave processor;
  5. Receives cost function values from slave processors;
  6. Checks convergence.
- Slave processor
  7. Receives a particle position from the master processor;
  8. Evaluates the analysis function  $f(x^i)$  at the given particle position  $x^i$ ;
  9. Sends a cost function value to the master processor.

# Related Work

## Rastrigin's function

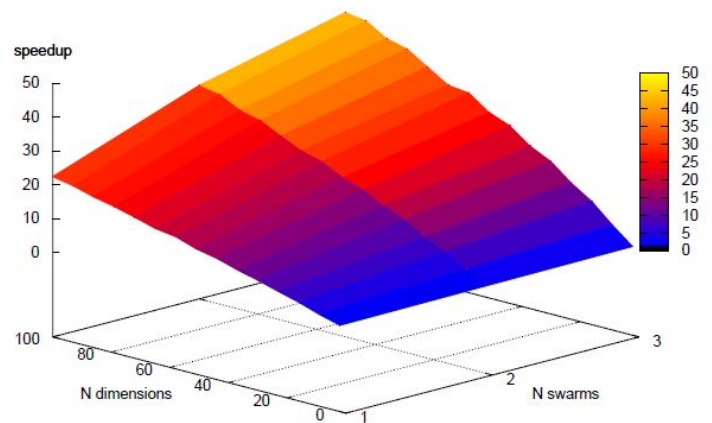
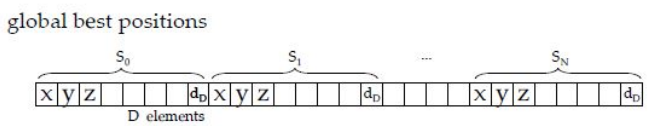
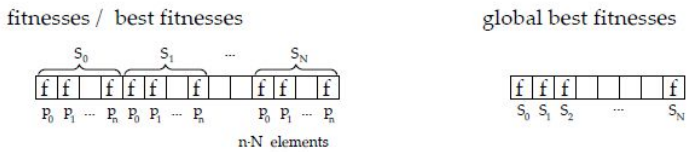
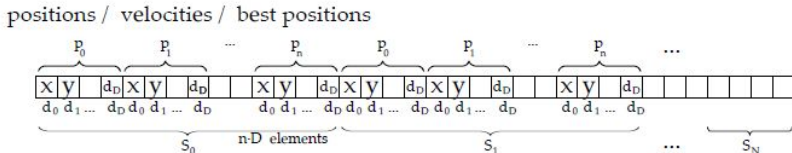
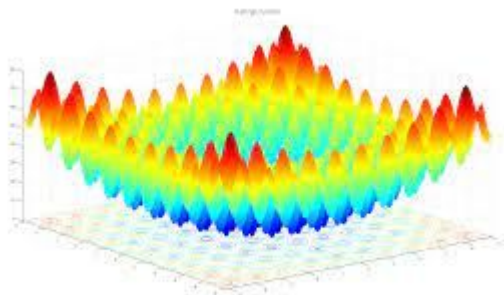


Figure 3: CUDAPSO vs sequentialPSO: Speedup

# Outline

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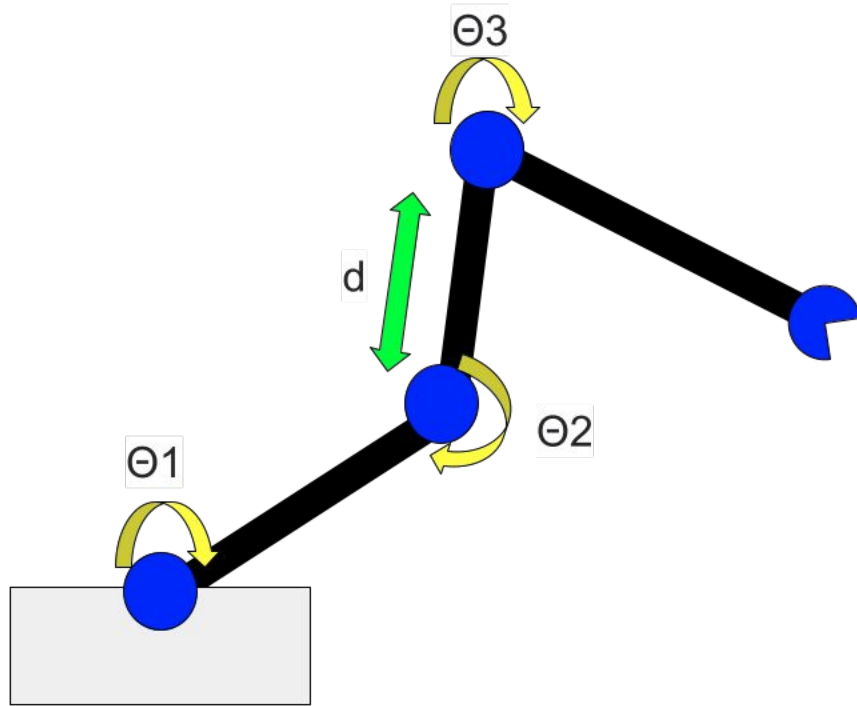
- OpenMP
- CUDA

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# Problem Definition



# Paralle Particle Swarm Optimization : CUDA

1. Introduce MTGP32 random number generator
2. Reduce memory copy between host to device
3. Reduction when evaluating pBestFit

# Paralle Particle Swarm Optimization : CUDA

random number generator is needed when :

1. particle is out of bound
2. generating R1 R2

Generating  $32768 * 128 * 256$  random floats between 1000000 and 0 costs:

5.65640s for GPU with  $128 * 256$  threads

57.94887s for CPU

```
lin@lin-Genuine-ZEUS-15H-GNB15H-9RG60:/media/lin/9C33-6BBD/multithreadPractice/FinalProject/proj$ ./generateRandom
gpu time elapsed: 5.65640
cpu time elapsed: 35.94887
```

# Parallel Particle Swarm Optimization : CUDA

Reduce memory copy between host to device

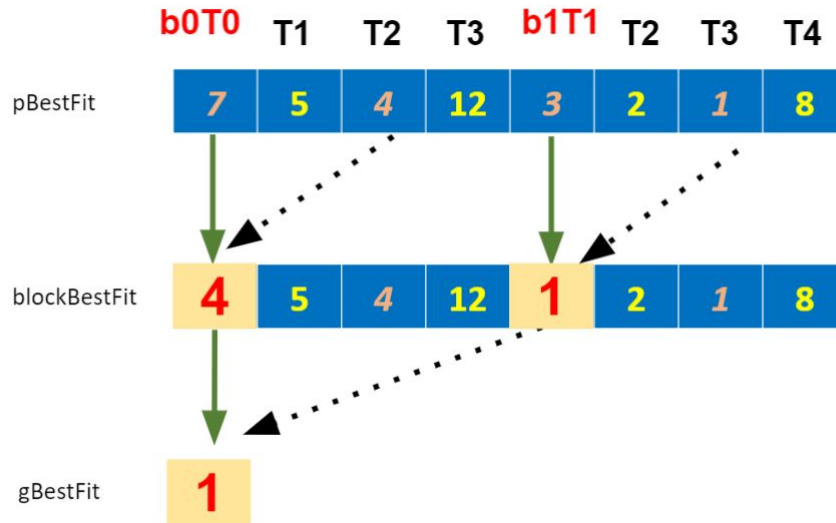
Type	Time(%)	Time	Calls	Avg	Min	Max	Name
GPU activities:	97.63%	549.72ms	10000	54.972us	44.575us	104.93us	deviceSearch(double*, double*, double*, double*, double*, double*, int*, int*, curandStateMtg32*)
	2.37%	13.345ms	20038	665ns	543ns	126.14us	[CUDA memcpy HtoD]
	0.00%	4.5130us	6	752ns	672ns	928ns	[CUDA memcpy DtoH]
	0.00%	832ns	1	832ns	832ns	832ns	[CUDA memset]
API calls:	70.77%	567.56ms	10000	56.756us	2.0550us	510.99us	cudaDeviceSynchronize
	16.23%	130.14ms	17	7.6553ms	1.2310us	130.00ms	cudaMalloc
	9.16%	73.466ms	20017	3.6700us	2.2340us	947.63us	cudaMemcpyToSymbol
	3.69%	29.599ms	10000	2.9590us	2.6690us	256.10us	cudaLaunchKernel
	0.07%	557.79us	27	20.659us	4.9910us	35.661us	cudaMemcpy
	0.03%	253.08us	1	253.08us	253.08us	253.08us	cuDeviceTotalMem
	0.02%	182.71us	17	10.747us	1.3650us	95.969us	cudaFree

CUDA MEMCPY HtoD Only costs 2.37%

CUDA MEMCPY DtoH Only costs 0.00%

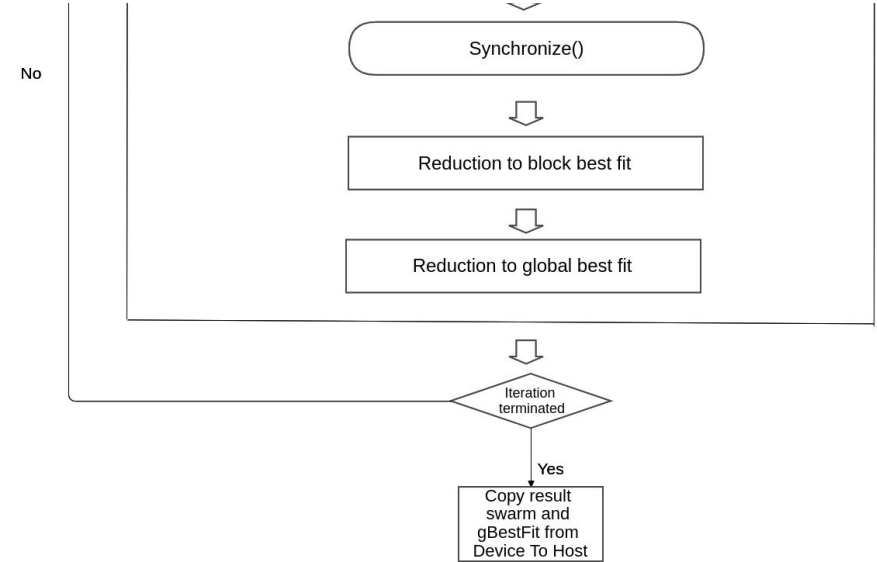
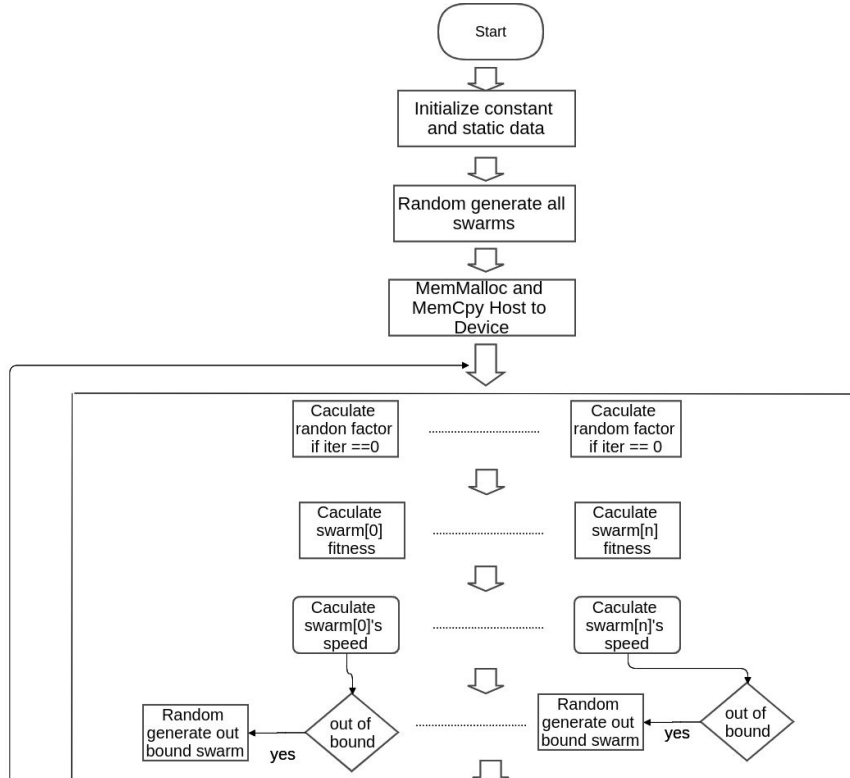
# Parallel Particle Swarm Optimization : CUDA

## 1. Reduction when evaluating pBestFit





# Paralle Particle Swarm Optimization : CUDA



# Parallel Particle Swarm Optimization : OpenMP

work sharing:

#pragma omp parallel for

## 1. Initialization

1.1. For each particle  $i$  in a swarm population size  $P$ :

1.1.1. Initialize  $X_i$  randomly

1.1.2. Initialize  $V_i$  randomly

1.1.3. Evaluate the fitness  $f(X_i)$

1.1.4. Initialize  $pbest_i$  with a copy of  $X_i$

1.2. Initialize  $gbest$  with a copy of  $X_i$  with the best fitness

## 2. Repeat until a stopping criterion is satisfied:

2.1. For each particle  $i$ :

2.1.1. Update  $V_i^t$  and  $X_i^t$  according to Eqs. (1) and (2)

2.1.2. Evaluate the fitness  $f(X_i^t)$

2.1.3.  $pbest_i \leftarrow X_i^t$  if  $f(pbest_i) < f(X_i^t)$

2.1.4.  $gbest \leftarrow X_i^t$  if  $f(gbest) < f(X_i^t)$

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# Experiment--Platform



Ubuntu 18.04.4 LTS

Device name

Memory 15.4 GiB

Processor Intel® Core™ i7-9750H CPU @ 2.60GHz × 12

Graphics NVIDIA GeForce RTX 2060/PCIe/SSE2

GNOME 3.28.2

OS type 64-bit

Disk 202.5 GB

Parallel platform:

OpenMp

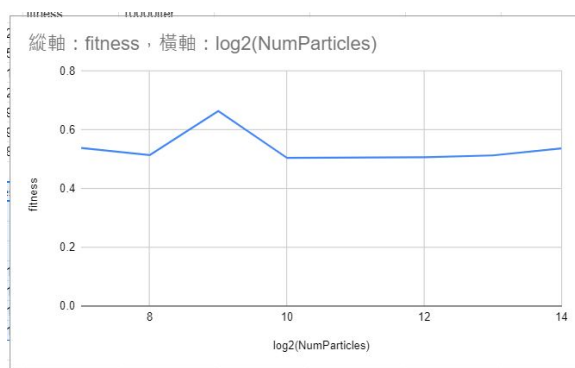
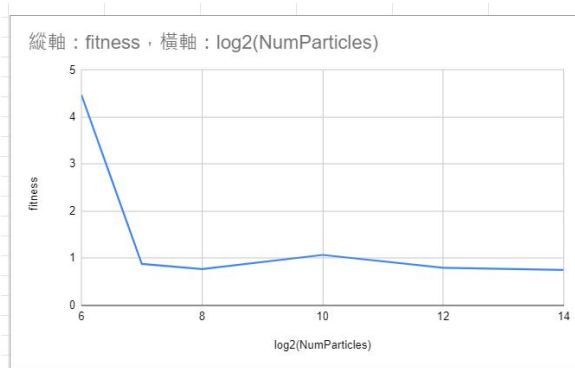
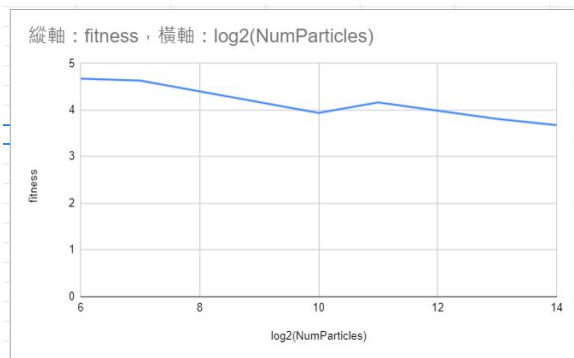
Cuda

C++

Demo platform:

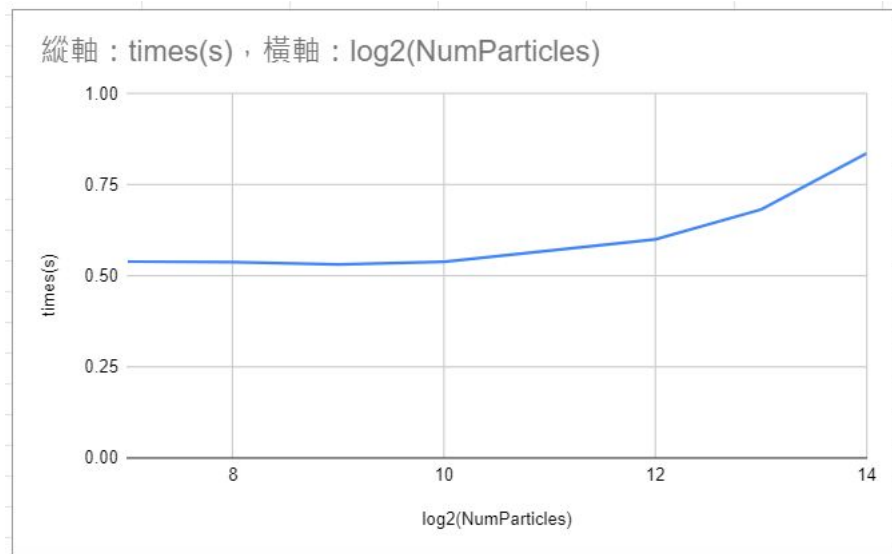
Qt

# Experiment--CUDA evaluation

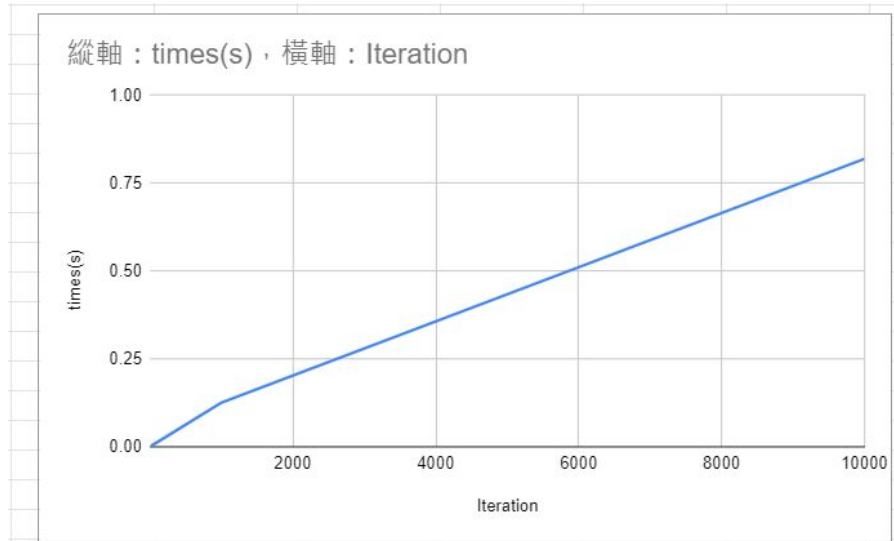


10, 100, 10000 iteration:  $\log_2(\text{NumParticle})$  to fitness

# Experiment--CUDA evaluation

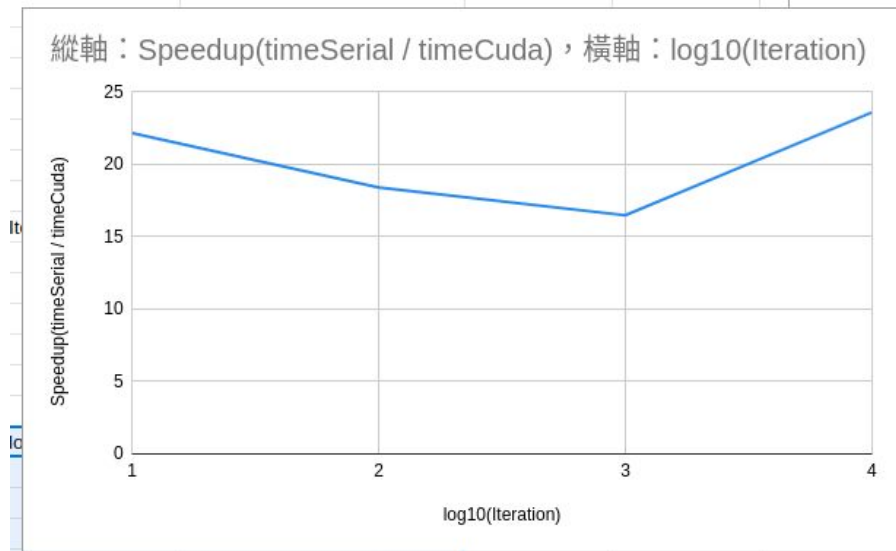


10000 iteration: log2(NumParticle) to time

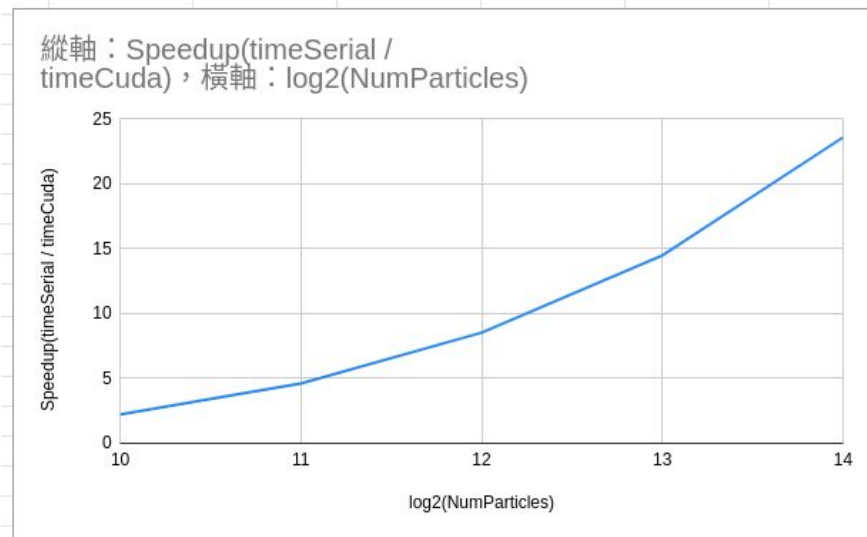


16384NumParticles: iteration to time

# Experiment--CUDA vs Serialize

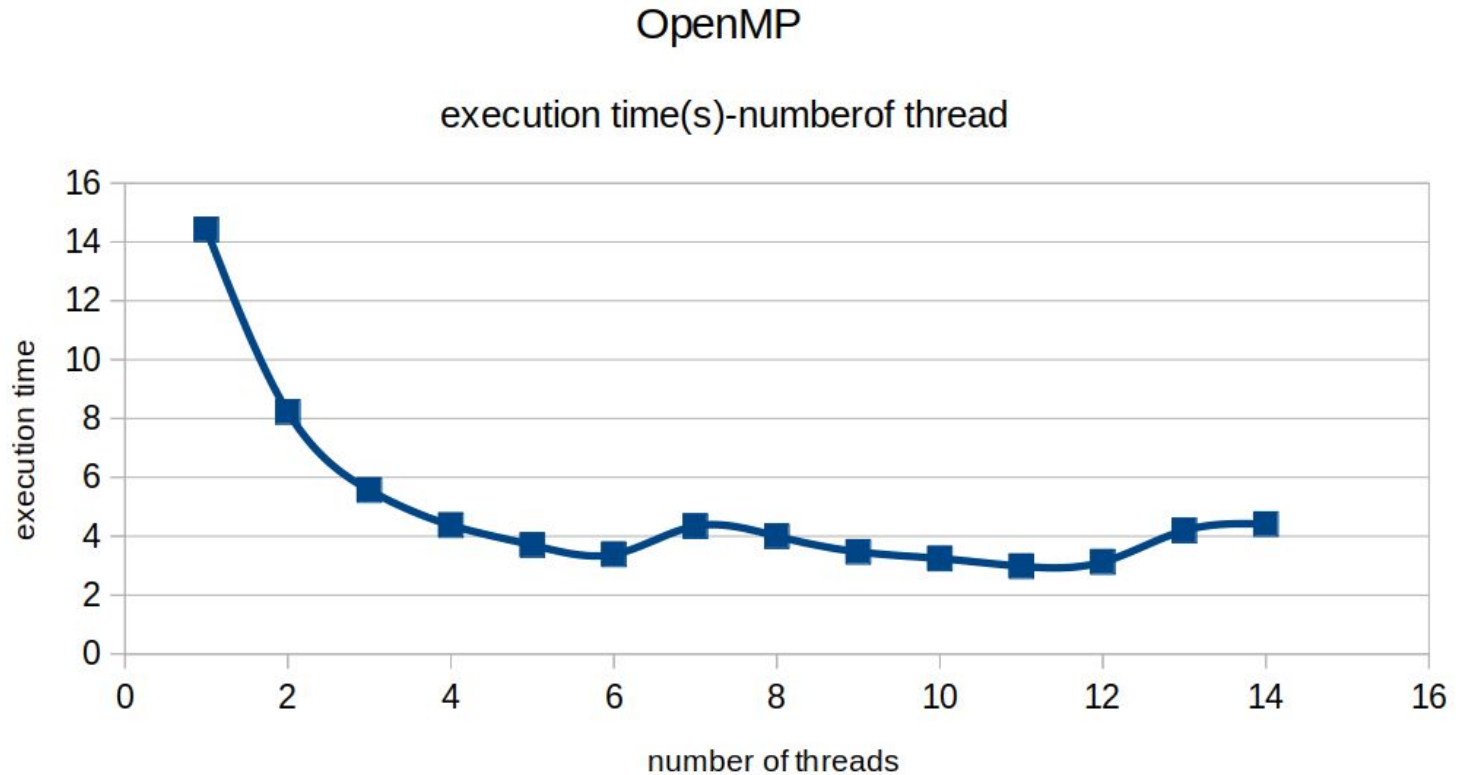


16384NumParticles: log10(Iterations) to time



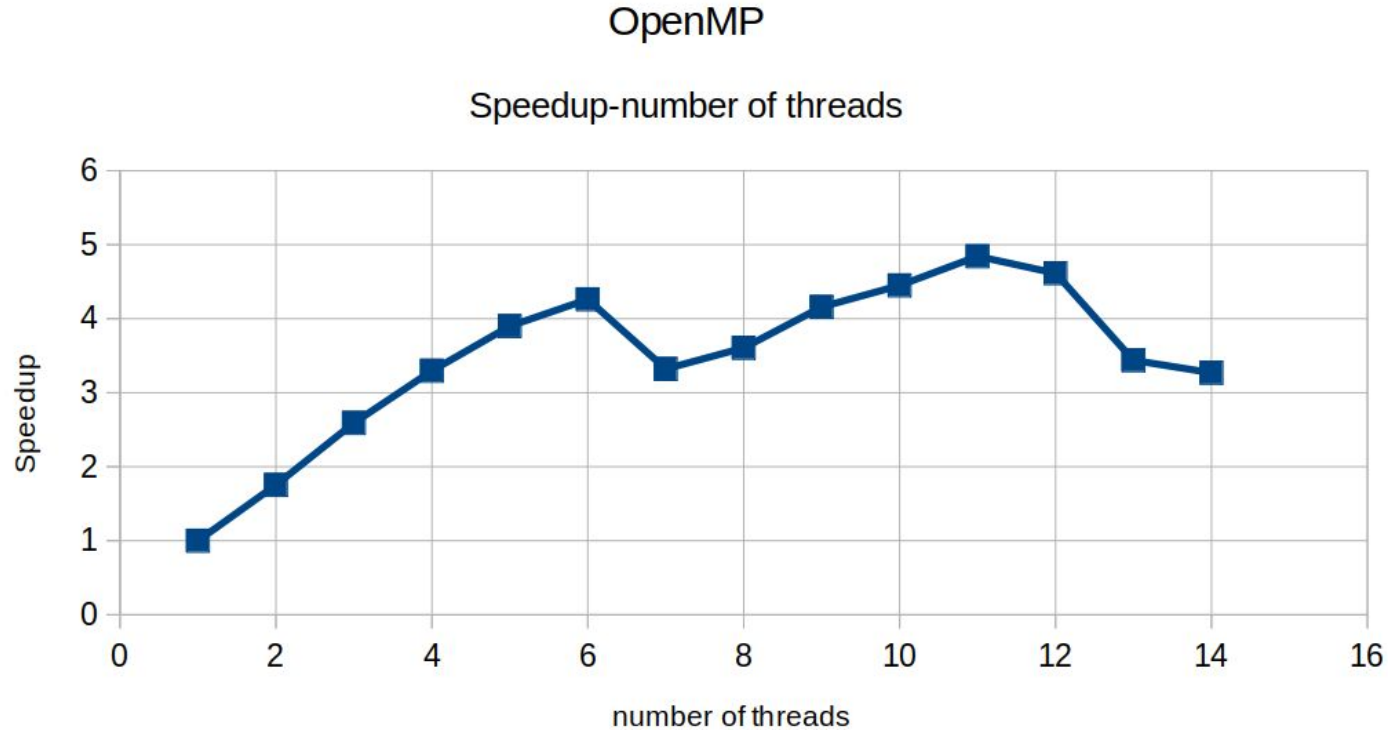
10000iteration: log2(NumParticles) to time

# Experiment--OpenMP

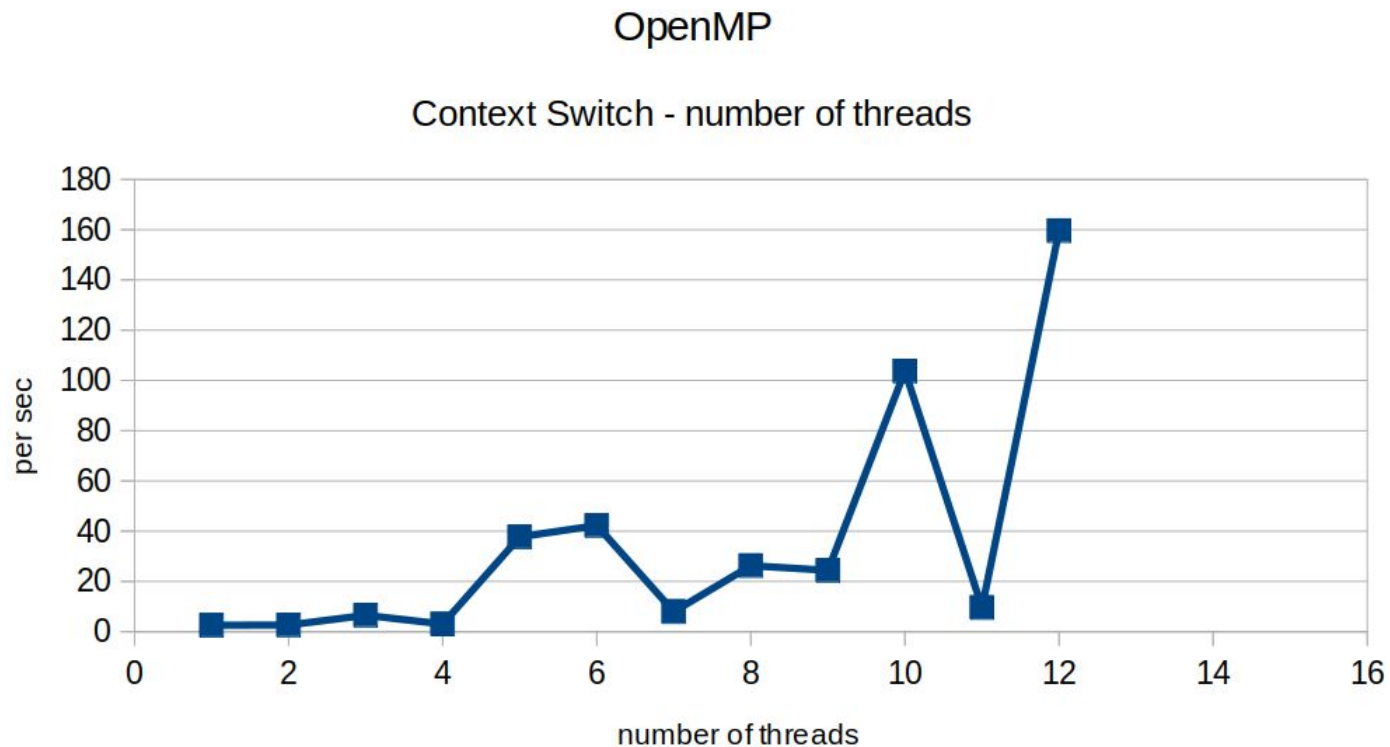




# Experiment--OpenMP



# Experiment--OpenMP

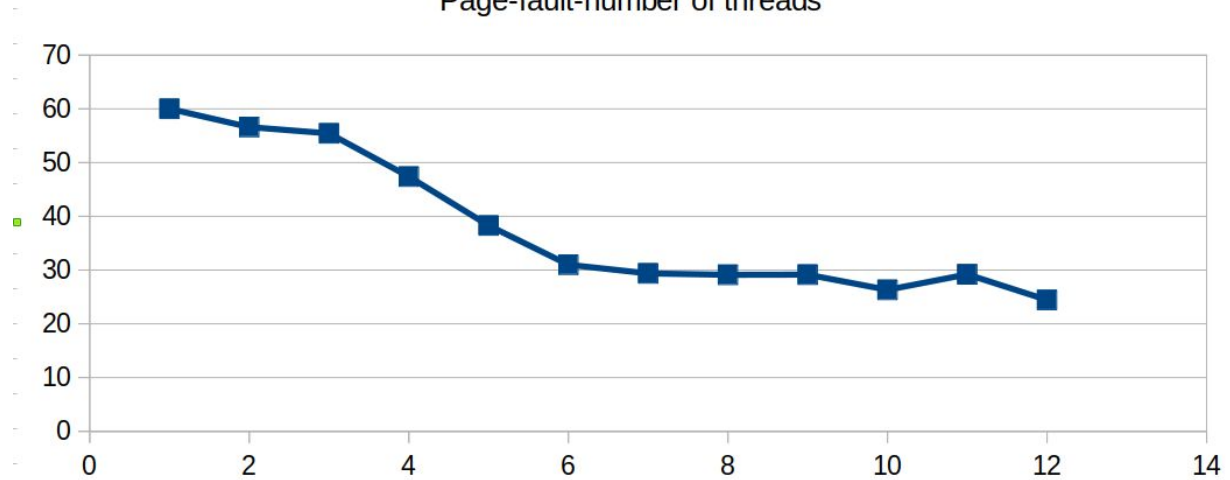


# Experiment--OpenMP

4 Threads

OpenMP

Page-fault-number of threads

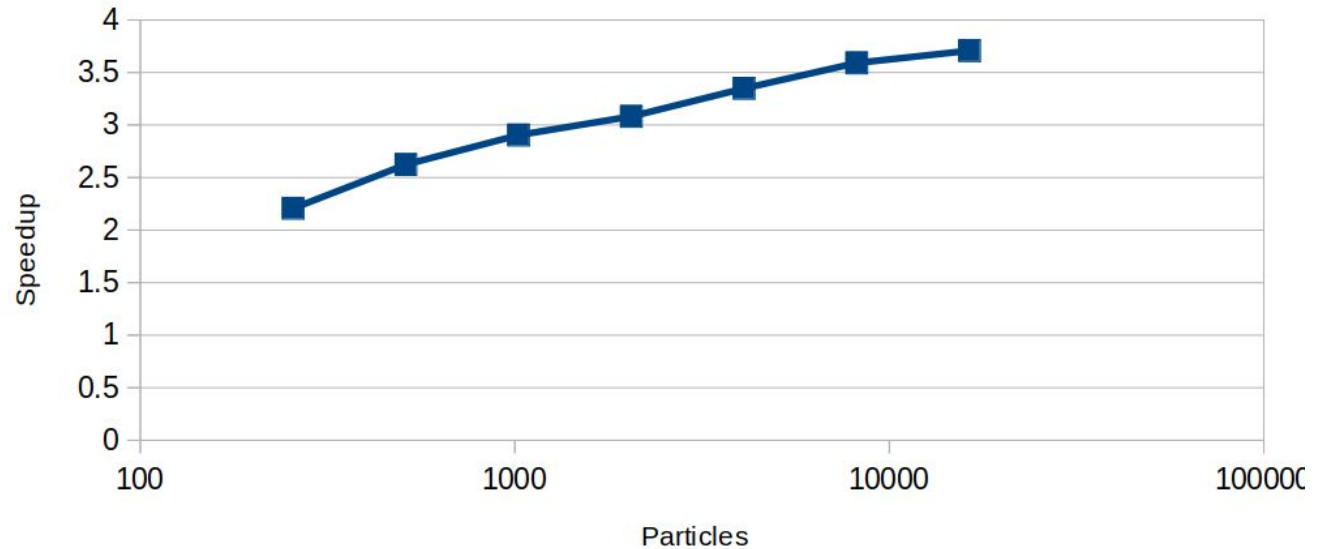


# Experiment--OpenMP

4 Threads

OpenMP

Speedup-number of Particles



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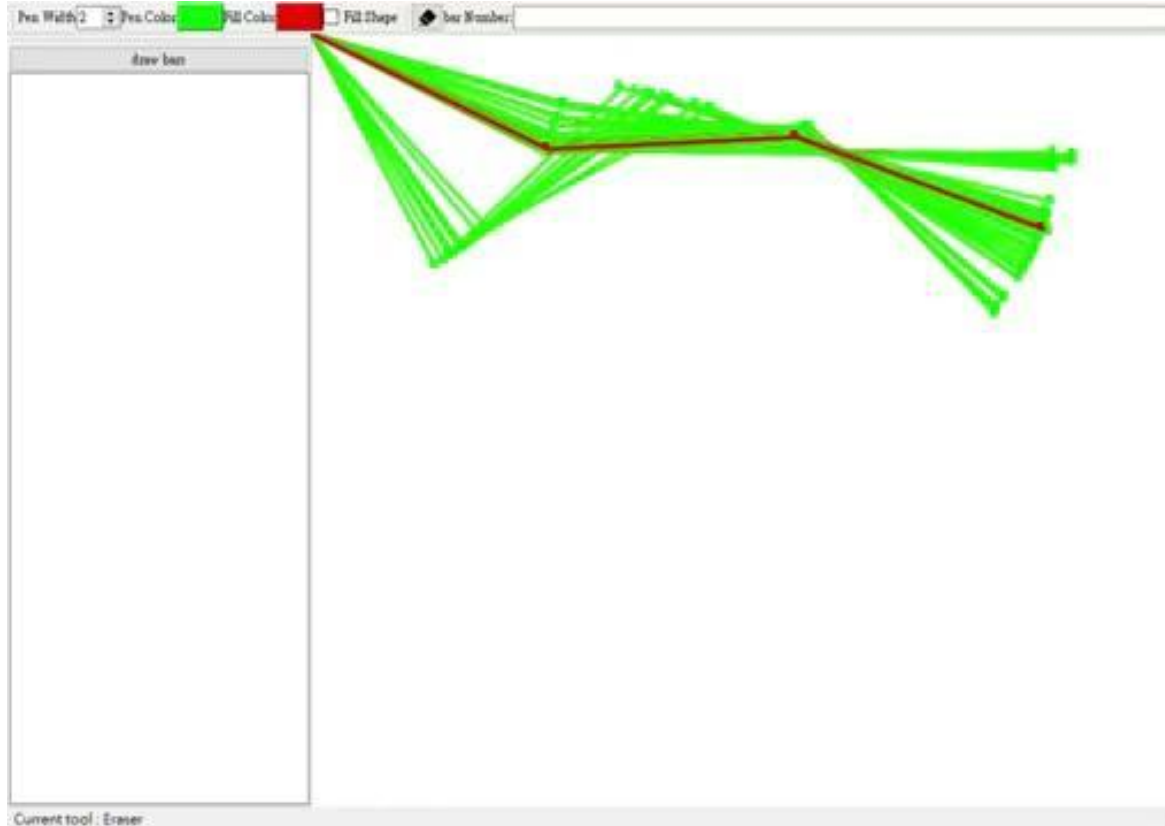
Experiment

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# Demo--serialize 3000iter 15 times slow



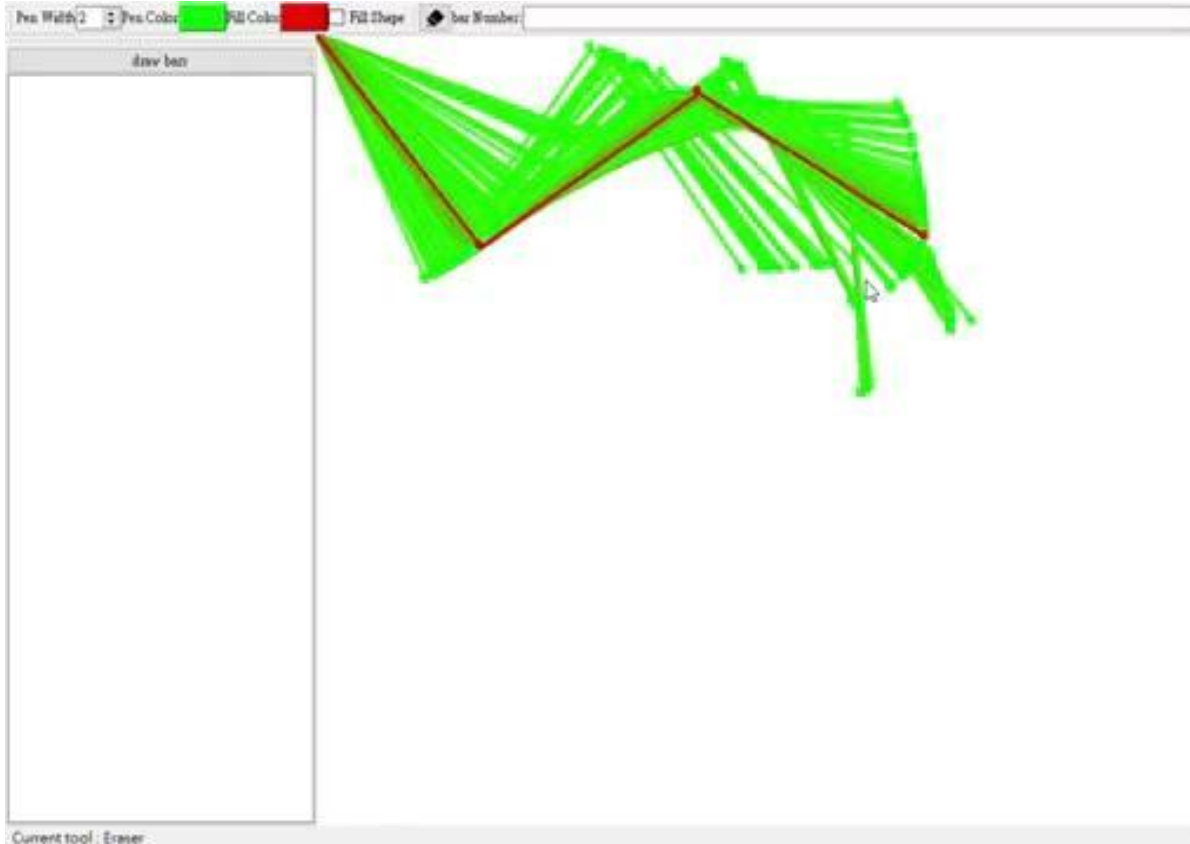
gBest is at: a1:0.453, a2:0.489,  
a3:0.357,d2: 4.791

arm position:(6.0000, 3.000)

time elapsed: 3.53499s

fitness: 0.505182

# Demo--openMP 3000iter 15 times slow



gBest is at: a1:0.894, a2:-0.599,  
a3:0.599,d2: 4.960

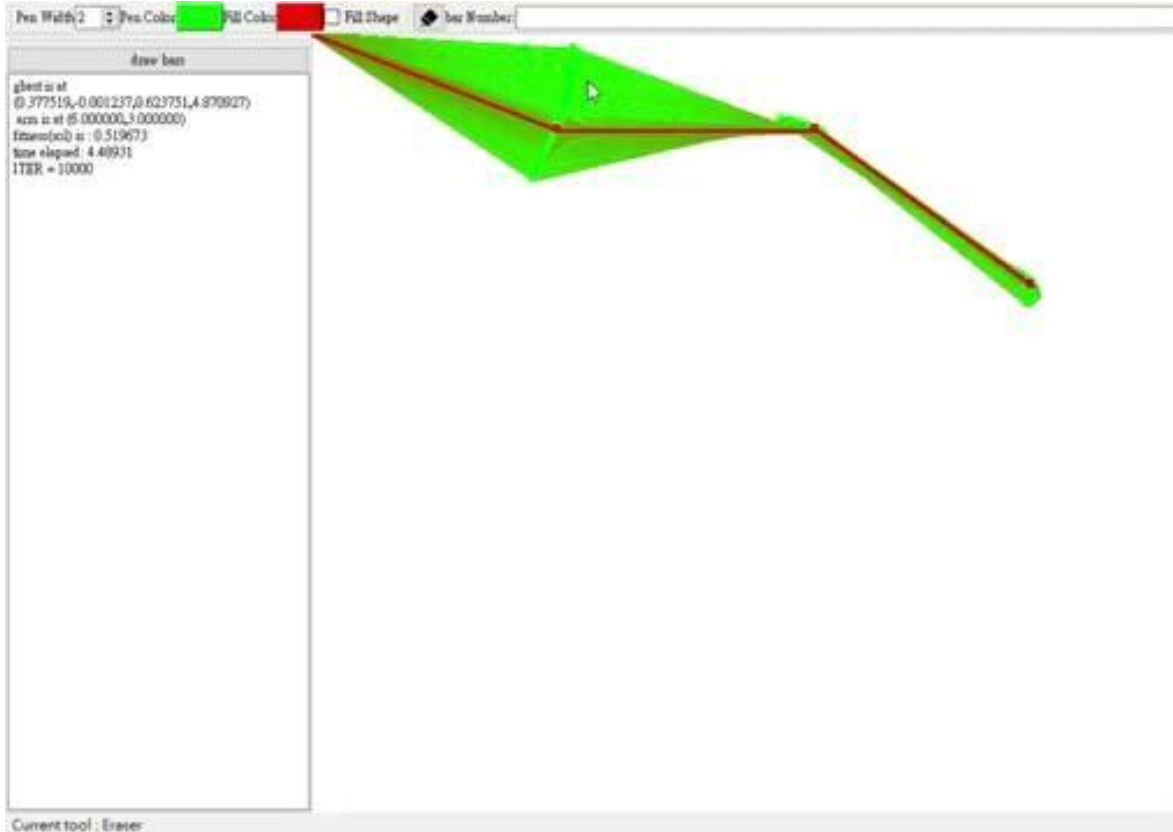
arm position:(6.0000, 3.000)

time elapsed: 0.6425s

fitness: 0.505182

6.99745X

# Demo--openMP 10000iter 15 times slow



gBest is at: a1:0.378, a2:-0.001,  
a3:0.624,d2: 4.871

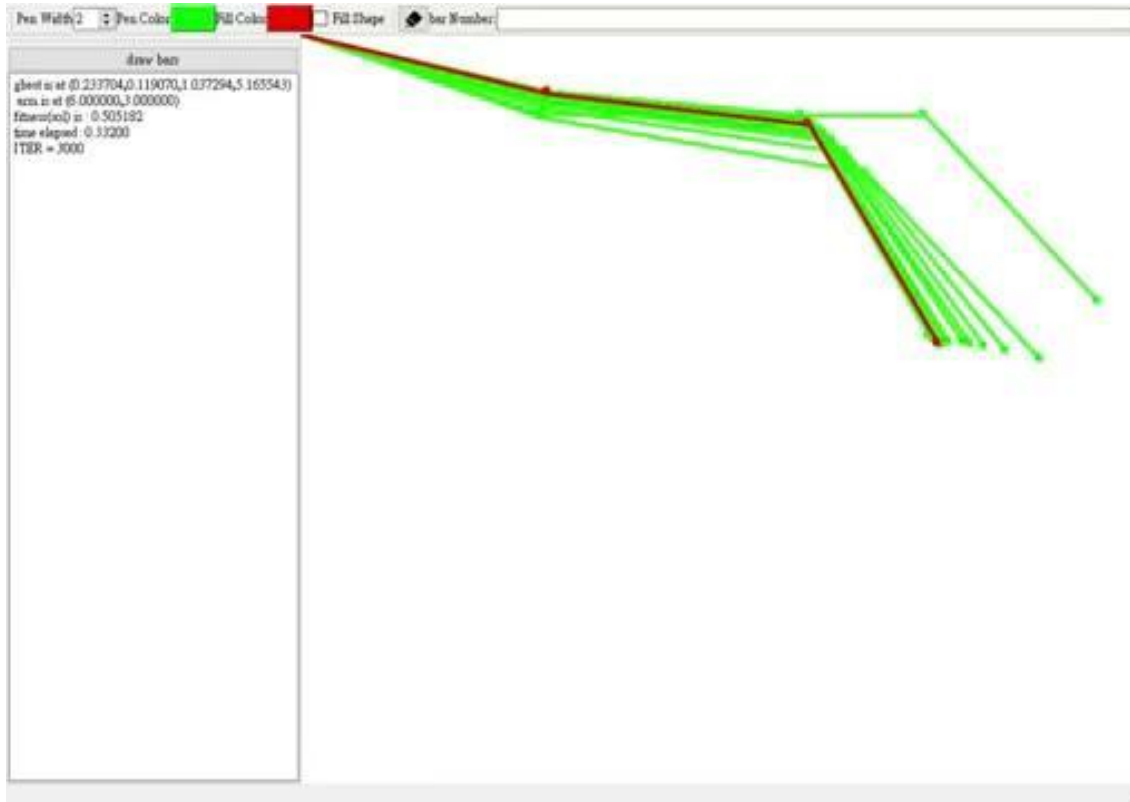
arm position:(6.0000, 3.000)

time elapsed: 4.409s

fitness: 0.519673



# Demo--cuda 3000 iter 15 times slow



gBest is at: a1:0.234, a2:0.119,  
a3:1.037,d2: 5.163

arm position:(6.0000, 3.000)

time elapsed: 0.332s

fitness: 0.505182

10.6468X

# Demo--cuda and openMP 3000iter normal speed



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## Conclusion and Future work

### Conclusion:

openMP and CUDA can significantly speedup PSO when solving Inverse Kinematics

CUDA done better when the problem size increases;

It is much more easier to parallelize PSO by openMP

### Future work:

Real time tracing Inverse Kinematics

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J. F. Schutte , J. A. Reinbolt., Parallel global optimization with the particle swarm algorithm, Int J Numer Methods Eng. 2004 December 7

Luca Musci,Stefano Cagn ,Particle swarm optimization within the CUDA architecture, ,Conference: Genetic and Evolutionary Computation Conference - GECCO 2009

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Bruno Seixas Gomes de Almeida and Victor Coppo Leite (2019),

Particle Swarm Optimization:A Powerful Technique for Solving Engineering Problems. IntechOpen.  
PySwarms (2021), Lj Miranda, <https://github.com/ljvmiranda921/pyswarms>.

Thank you for your attention