

(A) $\frac{\partial L}{\partial a_j^{l+1}} \propto \frac{\partial L}{\partial a_i^l}$ where $a_j^{l+1} = \sigma(z_j^l)$

computing $\sigma(\cdot)$ in
 $\frac{\partial L}{\partial z_j^l}$ signal for j^{th} node of layer l

$$\frac{\partial L}{\partial a_i^l} = \sum_{\forall a_j^{l+1}} \frac{\partial L}{\partial a_j^{l+1}} \cdot \frac{\partial a_j^{l+1}}{\partial z_j^l} \cdot \frac{\partial z_j^l}{\partial a_i^l}$$

(B) $\frac{\partial L}{\partial z_j^l} = \frac{\partial L}{\partial a_j^{l+1}} \cdot \frac{\partial a_j^{l+1}}{\partial z_j^l}$ (the first two terms of A.)

(C) $\frac{\partial L}{\partial w_{ij}^l} = \frac{\partial L}{\partial z_j^l} \cdot \frac{\partial z_j^l}{\partial w_{ij}^l}$

$$\frac{\partial L}{\partial b_j^l} = \frac{\partial L}{\partial z_j^l} \cdot \frac{\partial z_j^l}{\partial b_j^l}$$

$$\frac{\partial L}{\partial z_j^{l+1}} \cdot \frac{\partial z_j^{l+1}}{\partial a_j^{l+1}} \cdot \frac{\partial a_j^{l+1}}{\partial z_j^l}$$

$$\frac{\partial L}{\partial z_j^{l+1}} w_{ij}^{l+1} \cdot \sigma'(z_j^l)$$