

Python: Functions

Functions

- write reusable pieces/chunks of code, called **functions**
- functions are not run in a program until they are “**called**” or “**invoked**” in a program
- function characteristics:
 - has a **name**
 - has **parameters** (0 or more)
 - has a **docstring** (optional but recommended)
 - has a **body**
 - **returns** something

Defining and invoking a function

```
def is_even( i ):
    """
    Input: i, a positive int
    Returns True if i is even, otherwise False
    """
    print("inside is_even")
    return i%2 == 0

is_even(3)
```

keyword

name

parameters or arguments

specification, docstring

body

later in the code, you call the function using its name and values for parameters

Defining and invoking a function

```
def is_even( i ):  
    """  
    Input: i, a positive int  
    Returns True if i is even, otherwise False  
    """
```

```
    print("inside is_even")
```

```
    return i%2 == 0
```

keyword

expression to
evaluate and return

run some
commands

Defining and invoking a function

Consider $f(x) = x^2$

```
def square(x):           #defining function
    return x*x
```

```
square(4)                #invoking function
```

```
16                        # output
```

Defining and invoking a function

Example: Functions may not have arguments, and return statement

```
def myprint():          #defining function  
    print ("Hello world")
```

```
myprint()              #invoking function
```

```
Hello world           # output
```

Defining and invoking a function

Example: Function calling another function

```
def repeatmyprint():
```

```
    myprint()
```

```
    myprint()
```

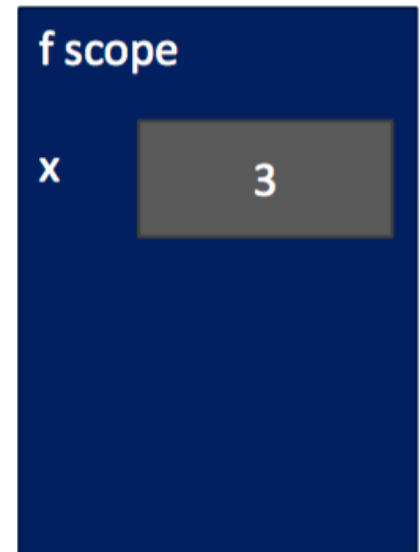
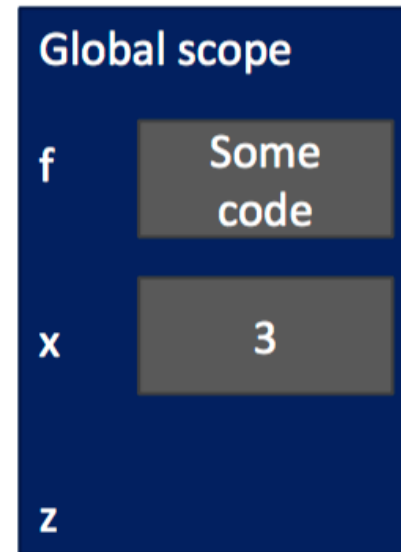
```
repeatmyprint()           #invoking function
```

```
Hello world              # output
```

```
Hello world
```

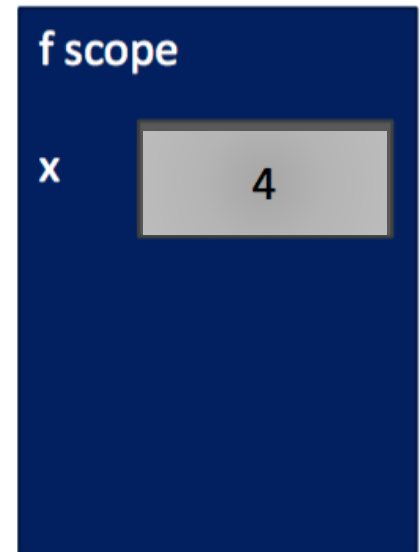
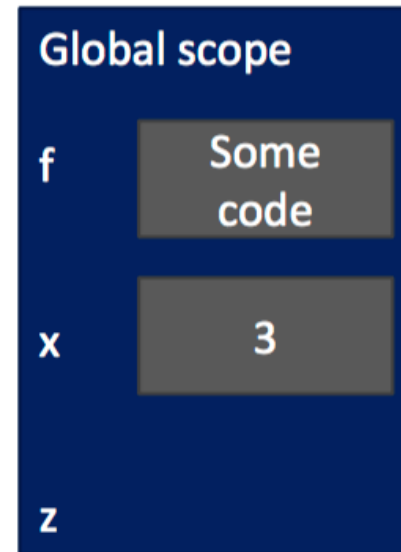
Scope of a Variable

```
def f( x ) :  
    x = x + 1  
    print('in f(x): x =', x)  
    return x  
  
x = 3  
z = f( x )
```



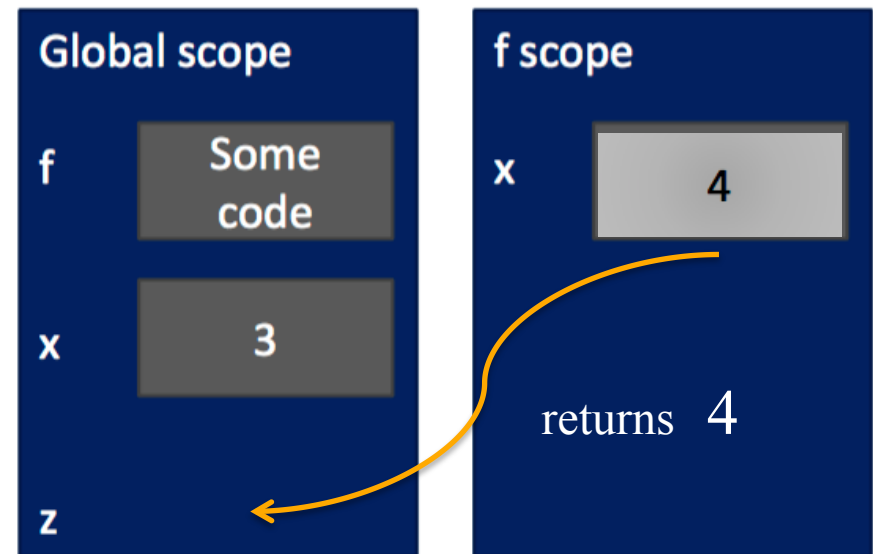
Scope of a Variable

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def f( x ) :  
    x = x + 1  
    print('in f(x): x =', x)  
    return x  
  
x = 3  
z = f( x )
```



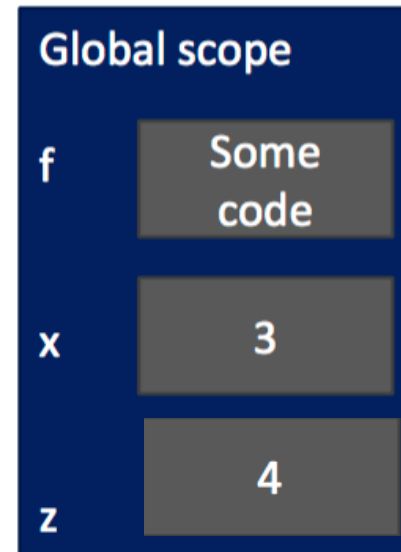
Scope of a Variable

```
def f( x ):  
    x = x + 1  
    print('in f(x): x =', x)  
    return x  
  
x = 3  
z = f( x )
```



Scope of a Variable

```
def f( x ) :  
    x = x + 1  
    print('in f(x): x =', x)  
    return x  
  
x = 3  
z = f( x )
```



Function: Scope

```
def f(y):  
    x=1  
    x+=1  
    print(x)
```

x is redefined locally

```
x=5  
f(x)  
print(x)
```

Output

2
5



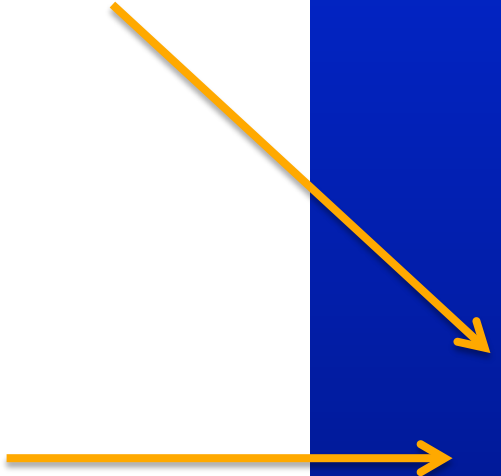
Function: Scope (Example)

```
def g(x):  
    def h():  
        x = 'abc'  
    x = x + 1  
    print('g: x =', x)  
    h()  
    return x
```

```
x = 3  
z = g(x)  
print(z)
```

Output

g: x=4
4



Python: Recursive Functions

Recursive Functions

Recall factorial function:

```
def factorial(n):  
    i=0  
    fact=1  
    while (i<n):  
        i=i+1  
        fact=fact*i  
    return fact
```

Iterative Algorithm

Loop construct (while)

can capture computation in a set of **state variables** that update on each iteration through loop

Recursive Functions

Alternatively:

Consider

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

can be re-written as $5! = 5 \times 4!$

In general $n! = n \times (n-1)!$

$$\text{factorial}(n) = n * \text{factorial}(n-1)$$

Recursive Functions

Alternatively:

Consider

$$5! = 5 \times 4 \times 3 \times 2 \times 1$$

can be re-written as $5! = 5 \times 4!$

Recursive Algorithm

function calling itself

In general $n! = n \times (n-1)!$

$$\text{factorial}(n) = n * \text{factorial}(n-1)$$



Recursive Functions

```
def factorial( n):
```

```
    if (n == 0):
```

```
        return 1
```

```
    else:
```

```
        return n * factorial(n - 1)
```

Base case

Recursive step

GCD Algorithm

$$\text{gcd}(a, b) = \begin{cases} b & \text{if } a \bmod b = 0 \\ \text{gcd}(b, a \bmod b) & \text{otherwise} \end{cases}$$

```
def gcd(a,b):  
    r=a%b  
    while (r !=0 ):  
        a=b  
        b=r  
        r=a%b  
    return b
```

Iterative
Algorithm

```
def gcd(a,b):  
    if (a%b == 0):  
        return b  
    else:  
        return gcd(b,a%b)
```

Recursive Algorithm

GCD Algorithm

$$\text{gcd}(a, b) = \begin{cases} b & \text{if } a \bmod b = 0 \\ \text{gcd}(b, a \bmod b) & \text{otherwise} \end{cases}$$

```
def gcd(a,b):  
    if (a%b == 0):  
        return b  
    else:  
        return gcd(b,a%b)
```

```
gcd(6, 10)  
gcd(10, 6)  
gcd(6, 4)  
gcd(4, 2)  
2  
2  
2  
2
```

Selecting Characters from a String

- A string is (still) an ordered collection of characters. The character positions in a Python string are, as in most computer languages, identified by an *index* beginning at 0.
- For example, if `s` is initialized as

```
s = "hello, world"
```

the characters in `s` are arranged like this:

h	e	l	l	o	,		w	o	r	l	d
0	1	2	3	4	5	6	7	8	9	10	11

- You can select an individual character using the syntax `str[k]`, where *k* is the index of the desired character. The expression

```
s[7]
```

returns the one-character string `"w"` that appears at index 7.

Negative Indexing

- Unlike JavaScript, Python allows you to specify a character position in a string by using negative index numbers, which count backwards from the end of the string. The characters in the **"hello, world"** string on the previous slide can therefore be numbered using the following indices:

h	e	l	l	o	,		w	o	r	l	d
-12	-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1

- You can select the **"w"** toward the end of this string using the expression

s[-5]

which is shorthand for the positive indexing expression

s[len(s) - 5]

Concatenation

- One of the more familiar operations available to Python strings is *concatenation*, which consists of combining two strings end to end with no intervening characters.
- Concatenation is built into Python in the form of the + operator. This is consistent with how JavaScript and most other languages support concatenation.
- Noteworthy difference between Python and JavaScript: Python interprets the + operator as concatenation only if **both** operands are strings. If one of the operands is something other than a string, then string concatenation isn't applied. Restated, Python doesn't automatically convert numbers to strings as JavaScript does.

Repetition

- In much the same way that Python redefines the `+` operator to indicate string concatenation, it also redefines the `*` operator for strings to indicate repetition, so that the expression `s * n` indicates `n` copies of the string `s` concatenated together.
- The expression `"1a" * 3` therefore returns `"1a1a1a"`, which is three copies of the string `"1a"` concatenated together.
- Note that this interpretation is consistent with the idea that multiplication is repeated addition:

`"1a" * 3` \rightarrow `"1a" + "1a" + "1a"`

- You can use this feature, for example, to print a line of 80 hyphens like this:

```
print("-" * 80)
```


Slicing

- Python allows you to extract a substring by specifying a range of index positions inside the square brackets. This operation is known as *slicing*.
- The simplest specification of a slice is `[start:stop]`, where *start* is the index at which the slice begins, and *stop* is the past-the-end index where the slice ends.
- The *start* and *stop* components of a slice are optional, but the colon must be present. If *start* is missing, it defaults to 0, and if *stop* is missing, it defaults to the length of the string.
- A slice specification may also contain a third component called a *stride*, as with `[start:stop:stride]`. Strides indicate how many positions are omitted between selected characters.
- The *stride* component can be negative, in which case the selection occurs backwards from the end of the string.

Exercise: Slicing

- Suppose that you have initialized **ALPHABET** as

ALPHABET = "ABCDEFGHIJKLMNOPQRSTUVWXYZ"

so that the index numbers (in both directions) run like this:

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
-26	-25	-24	-23	-22	-21	-20	-19	-18	-17	-16	-15	-14	-13	-12	-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1

- What are the values of the following slice expressions?
 - (a) **ALPHABET**[7:9]
 - (b) **ALPHABET**[-3:-1]
 - (c) **ALPHABET**[:3]
 - (d) **ALPHABET**[-1:]
 - (e) **ALPHABET**[14:-12]
 - (f) **ALPHABET**[1:-1]
 - (g) **ALPHABET**[0:5:2]
 - (h) **ALPHABET**[::-1]
 - (i) **ALPHABET**[5:2:-1]
 - (j) **ALPHABET**[14:2:-3]

Methods for Finding Patterns

str.find(pattern)

Returns the first index of *pattern* in *str*, or -1 if it does not appear.

str.find(pattern, k)

Same as the one-argument version but starts searching from index *k*.

str.rfind(pattern)

Returns the last index of *pattern* in *str*, or -1 if it does not appear.

str.rfind(pattern, k)

Same as the one-argument version but searches backward from index *k*.

str.startswith(prefix)

Returns **True** if this string starts with *prefix*.

str.endswith(suffix)

Returns **True** if this string ends with *suffix*.

Methods for Transforming Strings

str.lower()

Returns a copy of *str* with all letters converted to lowercase.

str.upper()

Returns a copy of *str* with all letters converted to uppercase.

str.capitalize()

Capitalizes the first character in *str* and converts the rest to lowercase.

str.strip()

Removes whitespace characters from both ends of *str*.

str.replace(old, new)

Returns a copy of *str* with all instances of *old* replaced by *new*.

Methods for Classifying Characters

`ch.isalpha()`

Returns **True** if *ch* is a letter.

`ch.isdigit()`

Returns **True** if *ch* is a digit.

`ch.isalnum()`

Returns **True** if *ch* is a letter or a digit.

`ch.islower()`

Returns **True** if *ch* is a lowercase letter.

`ch.isupper()`

Returns **True** if *ch* is an uppercase letter.

`ch.isspace()`

Returns **True** if *ch* is a *whitespace character* (space, tab, or newline).

`str.isidentifier()`

Returns **True** if this string is a legal Python identifier.

Lists

- **ordered sequence** of information, accessible by index
- a list is denoted by **square brackets**, []
- a list contains **elements**
 - usually homogeneous (ie, all integers)
 - can contain mixed types (not common)
- list elements can be changed so a list is **mutable**

Lists

```
a_list = [] empty list  
L = [2, 'a', 4, [1, 2]]  
len(L) → evaluates to 4  
L[0] → evaluates to 2  
L[2]+1 → evaluates to 5  
L[3] → evaluates to [1, 2], another list!  
L[4] → gives an error  
i = 2  
L[i-1] → evaluates to 'a' since L[1] = 'a'
```

Lists

- lists are **mutable**!
- assigning to an element at an index changes the value

```
L = [2, 1, 3]
```

```
L[1] = 5
```

- L is now [2, 5, 3], note this is the **same object** L

Lists

- compute the **sum of elements** of a list
- common pattern, iterate over list elements

```
total = 0
for i in range(len(L)):
    total += L[i]
print total
```

```
total = 0
for i in L:
    total += i
print total
```

like strings,
can iterate
over list
elements
directly

- notice
 - list elements are indexed 0 to $\text{len}(L) - 1$
 - `range(n)` goes from 0 to $n - 1$

Lists

- **add** elements to end of list with `L.append(element)`

- **mutates** the list!

```
L = [2, 1, 3]
```

```
L.append(5)    → L is now [2, 1, 3, 5]
```



- what is the dot?
 - lists are Python objects, everything in Python is an object
 - objects have data
 - objects have methods and functions
 - access this information by `object_name.do_something()`
 - will learn more about these later

Lists

- to combine lists together use **concatenation**, + operator, to give you a new list
- **mutate** list with `L.extend(some_list)`

```
L1 = [2, 1, 3]
```

```
L2 = [4, 5, 6]
```

```
L3 = L1 + L2
```

→ L3 is [2, 1, 3, 4, 5, 6]
L1, L2 unchanged

```
L1.extend([0, 6])
```

→ mutated L1 to [2, 1, 3, 0, 6]

Lists

- delete element at a **specific index** with `del (L[index])`
- remove element at **end of list** with `L.pop()`, returns the removed element
- remove a **specific element** with `L.remove(element)`
 - looks for the element and removes it
 - if element occurs multiple times, removes first occurrence
 - if element not in list, gives an error

all these
operations
mutate
the list

```
L = [2, 1, 3, 6, 3, 7, 0] # do below in order
L.remove(2) → mutates L = [1, 3, 6, 3, 7, 0]
L.remove(3) → mutates L = [1, 6, 3, 7, 0]
del(L[1])   → mutates L = [1, 3, 7, 0]
L.pop()     → returns 0 and mutates L = [1, 3, 7]
```

Lists to String

- convert **string to list** with `list(s)`, returns a list with every character from `s` as an element in `L`
- can use `s.split()`, to **split a string on a character** parameter, splits on spaces if called without a parameter
- use `' '.join(L)` to turn a **list of characters into a string**, can give a character in quotes to add char between every element

<code>s = "I<3 cs"</code>	→ <code>s</code> is a string
<code>list(s)</code>	→ returns <code>['I', '<', '3', ' ', 'c', 's']</code>
<code>s.split('<')</code>	→ returns <code>['I', '3 cs']</code>
<code>L = ['a', 'b', 'c']</code>	→ <code>L</code> is a list
<code>' '.join(L)</code>	→ returns <code>"abc"</code>
<code>'_'.join(L)</code>	→ returns <code>"a_b_c"</code>

Lists: Other Operations

- `sort()` and `sorted()`

- `reverse()`

```
L=[9, 6, 0, 3]
```

```
sorted(L)      → returns sorted list, does not mutate L
```

```
L.sort()       → mutates L=[0, 3, 6, 9]
```

```
L.reverse()    → mutates L=[9, 6, 3, 0]
```

<https://docs.python.org/3/tutorial/datastructures.html>

Lists

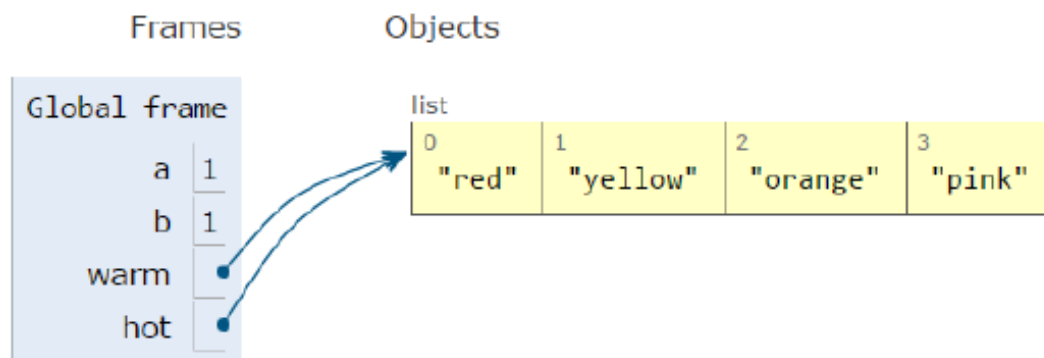
- lists are **mutable**
- behave differently than immutable types
- is an object in memory
- variable name points to object
- any variable pointing to that object is affected
- key phrase to keep in mind when working with lists is **side effects**

Lists: Aliasing

- `hot` is an **alias** for `warm` – changing one changes the other!
- `append()` has a side effect

```
1 a = 1
2 b = a
3 print(a)
4 print(b)
5
6 warm = ['red', 'yellow', 'orange']
7 hot = warm
8 hot.append('pink')
9 print(hot)
10 print(warm)
```

```
1
1
['red', 'yellow', 'orange', 'pink']
['red', 'yellow', 'orange', 'pink']
```

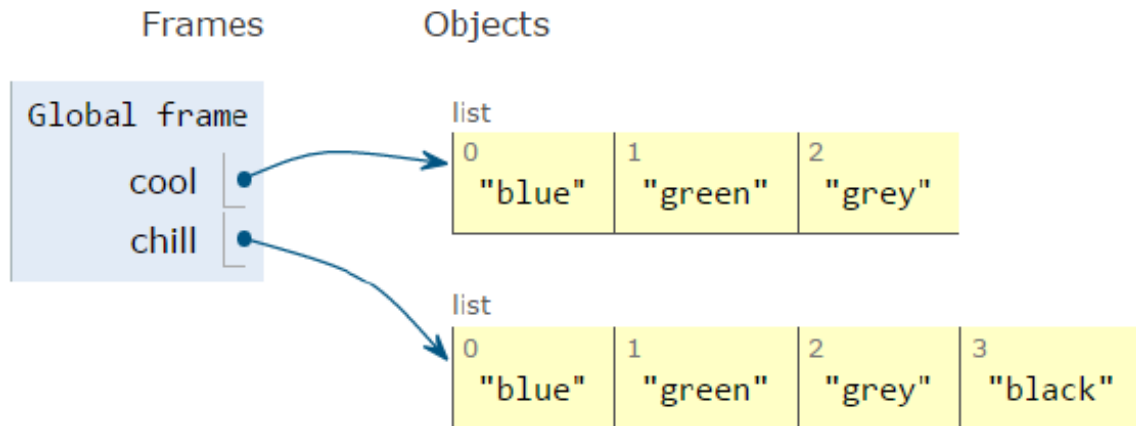


Lists: Cloning

- create a new list and **copy every element** using
`chill = cool[:]`

```
1 cool = ['blue', 'green', 'grey']  
2 chill = cool[:]  
3 chill.append('black')  
4 print(chill)  
5 print(cool)
```

```
['blue', 'green', 'grey', 'black']  
['blue', 'green', 'grey']
```



Lists: Sorting

- calling `sort()` **mutates** the list, returns nothing
- calling `sorted()` **does not mutate** list, must assign result to a variable

```
['orange', 'red', 'yellow']  
None  
['grey', 'green', 'blue']  
['blue', 'green', 'grey']
```

```
1 warm = ['red', 'yellow', 'orange']  
2 sortedwarm = warm.sort()  
3 print(warm)  
4 print(sortedwarm)  
5  
6 cool = ['grey', 'green', 'blue']  
7 sortedcool = sorted(cool)  
8 print(cool)  
9 print(sortedcool)
```

