

The key is the distribution of links within social networks

Some acquaintances are relatively isolated
Some have wide ranging connections
Play a critical role in bringing network closer together
Milgram experiment
for the successful chains passed through a local storekeeper

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The Hollywood Network:

Here we organize all actors in a graph
If they have co-starred with someone in a movie
They have a direct link to them (1 hop)
Some actors have more links than others because they have acted in so many movies
E.g. Kevin Bacon

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The Hollywood Network:
6 degrees of Kevin Bacon

John Carradine: 4000 links

Robert Mitchum: 2905 links

But acting in the most movies does not always translate into shortest hops to a random node in the network

Rankings:

Rod Steiger: 2.53

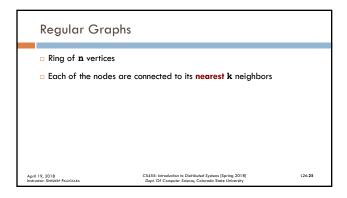
Donald Pleasence: 2.54

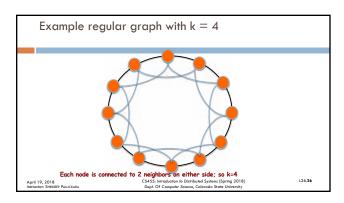
Martin Sheen, Christopher Lee, Robert Mitchum, Charlton Heston

Kevin Bacon? 2.79 pathlength and ranked 876th

Turns out even a small number of bridges can dramatically reduce pathlengths

Duncan Watts and Steven Strogatz (1998), "Collective Dynamics of 'Small-World' Networks," Nature 393, p 440.





Pathlength in a graph

Average number of hops to reach any node in the system
For each pair of vertices, compute shortest path
Take the average over all pairs
Gives a sense of how far apart points are in the network

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Clustering coefficients are a measure of the level of clustering

• For  ${\bf k}$  neighbors of a vertex, the number of possible connections between them is  $C_2^k = \frac{k(k-1)}{2}$ • Clustering coefficient of a vertex
- Proportion (0  $\sim$  1) of possible links actually present in graph

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Pathlength in Regular graphs

Approximately n/2k

If n=4096 and k=8

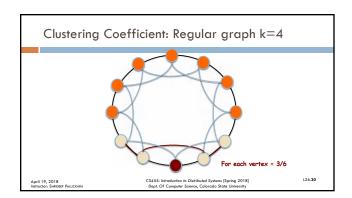
Pathlength = n/2k = 256

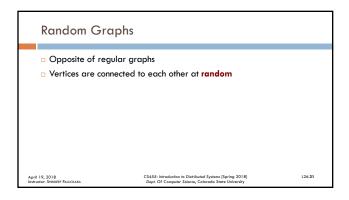
Very large!

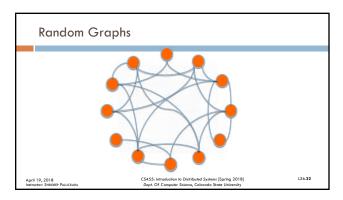
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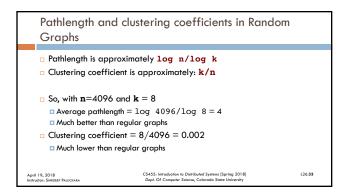
C5445: Introduction to Distributed Systems (Spring 2018)

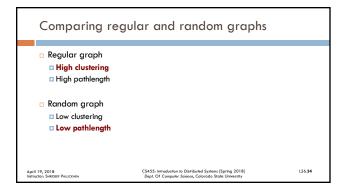
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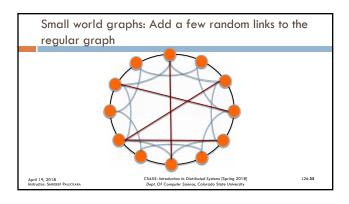


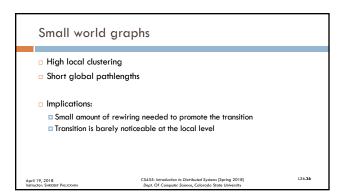


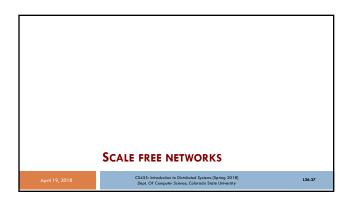


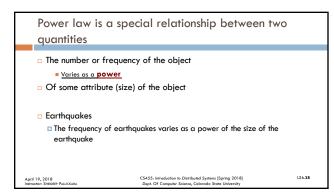












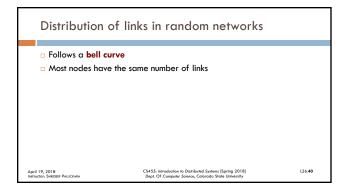
Power law and Random Networks:

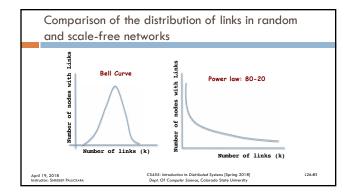
Real World examples

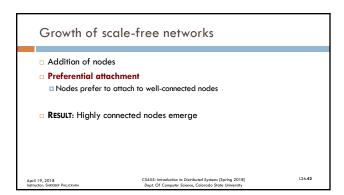
Random networks
Eisenhower National Highway System
Nodes=Cities, Links=Highways connecting them
Most cities served by roughly the same number of highways

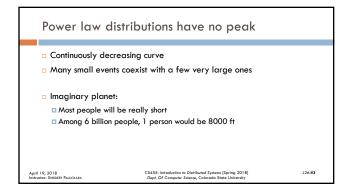
Scale-free networks
Airport system
Large number of small airports served by a few major hubs

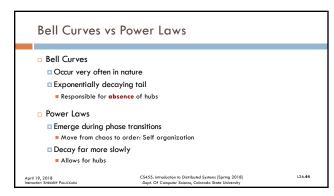
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Large number of small airports served by a few major hubs

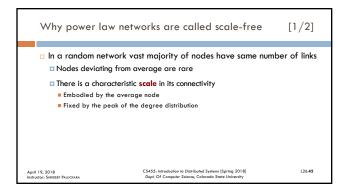


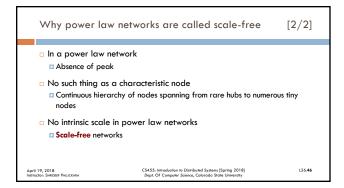












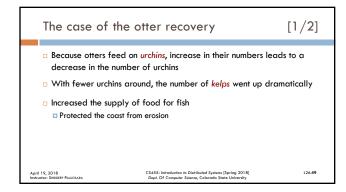
Achilles' heel in the power law network

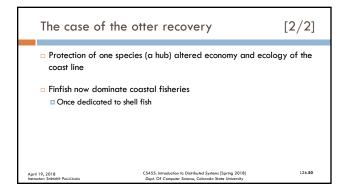
Power law networks are robust to random failures
Vulnerable to a targeted attack on hubs

Removal of hubs
Disintegrates these networks
Breaks them up into tiny non-communicating islands

Coexistence of robustness and vulnerability plays a role in complex systems

- Sea otters in California went nearly extinct because of excessive hunting for its pelts
- In 1911 federal regulators banned hunting them
- Otters made a dramatic comeback





The contents of this slide set are based on the following references

Peer-to-Peer: Harnessing the Power of Disruptive Technologies. Edited by Andy Oram. O'Reilly Publishing. ISBN: 0-596-00110-X. [Chapter 14 – Performance by Theodore Hong]

Linked: How Everything is Connected to Everything Else and What it Means for Business, Science, and Everydoy Life. Albert-László Barabásl. Plume. ISBN: 0452284392/978-0452284395. [Chapters 4,5,6, and 7]