

Projet Série Temporelle

Code ▼

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Utilisation des librairies nécessaires

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```
library("readxl")  
library("forecast")  
library("fpp2")  
library("ggplot2")  
library("dplyr")  
library("xlsx")
```

Importation des données

Hide

```
data = read_excel("Elec-train.xlsx")
```

La fréquence est de 96 car les données ont été mesuré toutes les 15min.
 $1\text{jour} = 96 * 15\text{min}$

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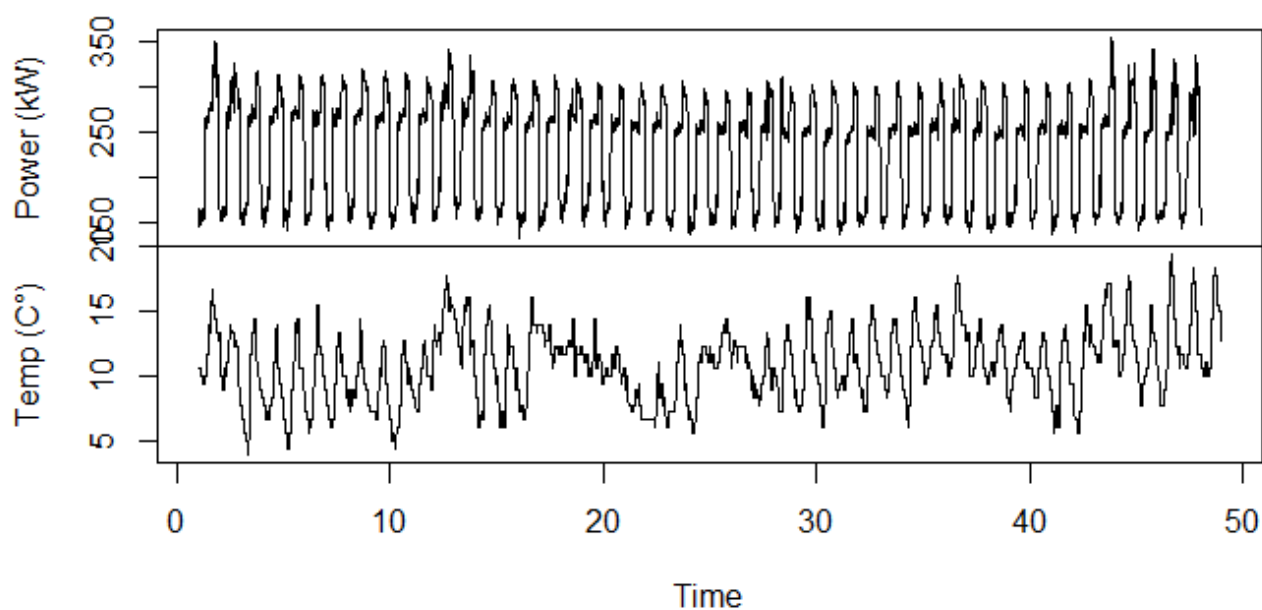
```
data=mutate(data, Timestamp = as.POSIXct(Timestamp,format = "%m/%d/%Y %H:%M"))  
elec<- ts(data[,2], start = c(1,6), end = c(47,96),frequency = 96)  
elecTemperature=ts(data[,2:3], start = c(1,6), end = c(48,96),frequency = 96)
```

Analyse des données

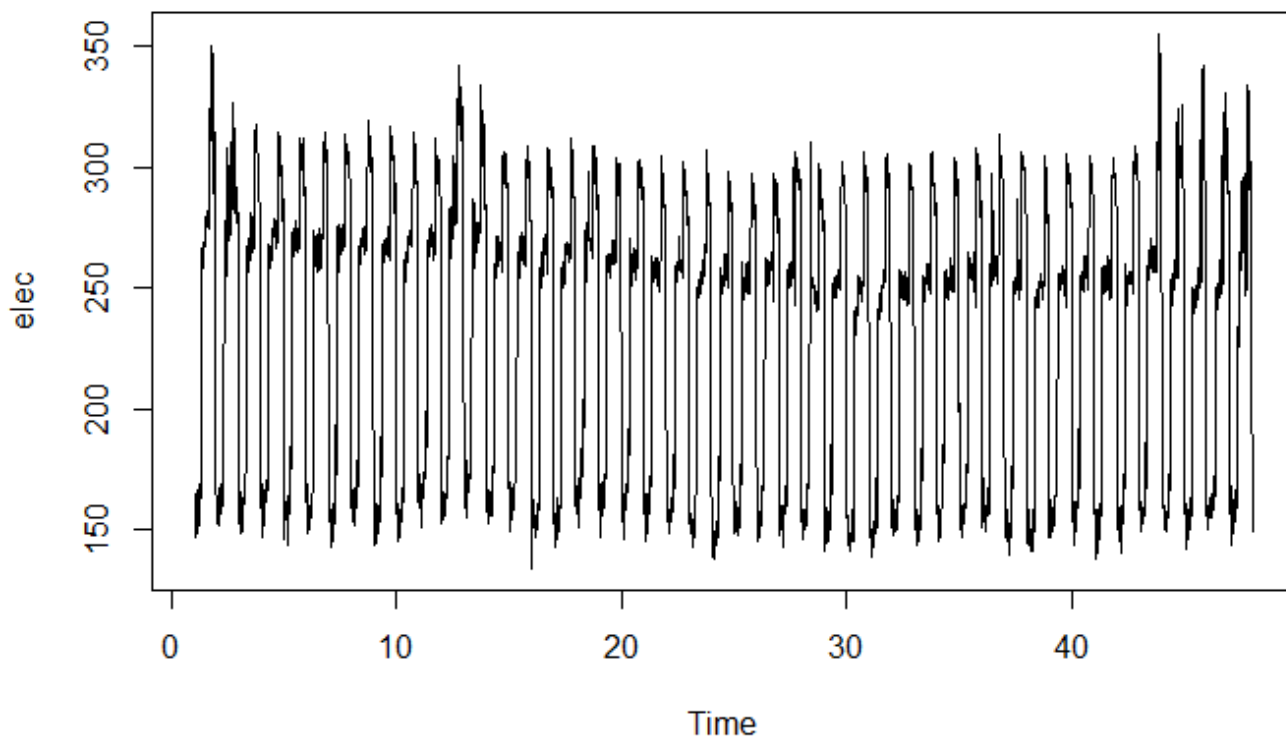
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```
plot(elecTemperature)
```

elecTemperature

[Hide](#)

```
plot(elec)
```



Il semble avoir une saisonnalité dans la consommation électrique, Mais il ne semble pas qu'il existe une tendance, car la consommation électrique ne semble ni augmenter ni diminuer.

Division des données en échantillons d'apprentissage et de test.

L'échantillon de test représente le dernier jour de consommation.

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```
elec_train = window(elec, start=c(1,6), end=c(46,96))
elec_test = window(elec, start=c(47,1), end=c(47,96))
elec_prev = window(elec, start=c(1,6))

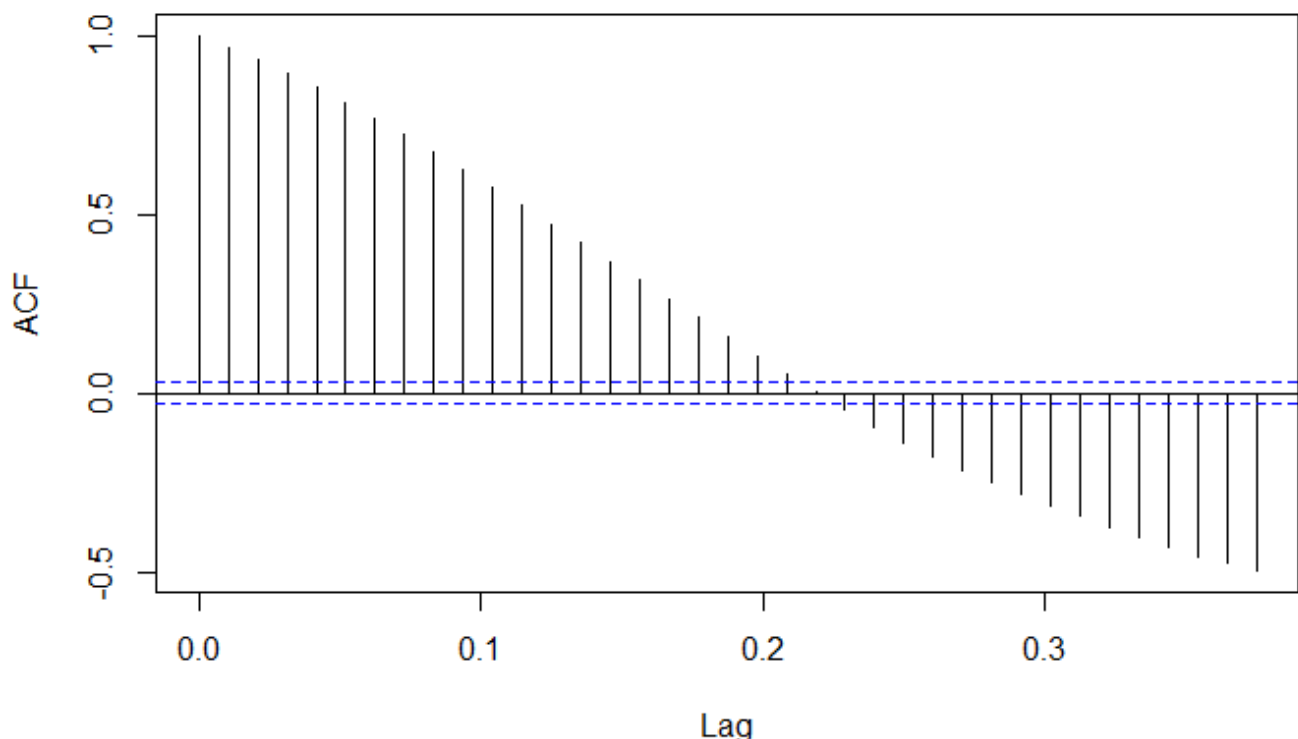
elecTemperature_train = window(elecTemperature, start=c(1,6), end=c(46,96))
elecTemperature_test = window(elecTemperature, start=c(47,1), end=c(47,96))
elecTemperature_prev = window(elecTemperature, start=c(1,6))
```

On commence la série à partir de 6 car la première valeur a été prise à 1h15. (6ième quarts-heure de la journée)

Sans Utilisation de la variable Temperature

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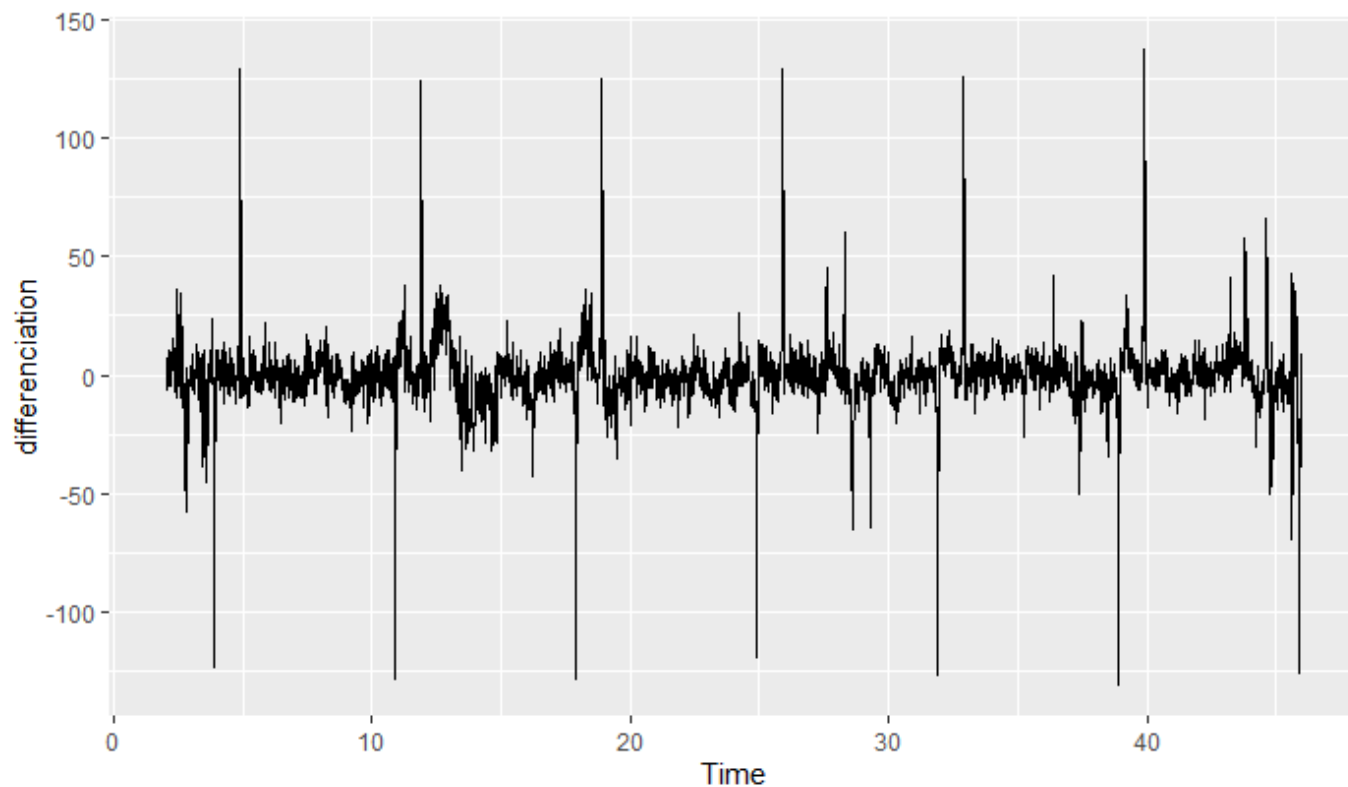
```
tmp=acf(elec_train,type="cor",plot = FALSE)
plot(tmp)
```



Grâce à notre ACF, je suis sûr que la serie a une Saisonnalité, car la fonction décroît exponentiellement

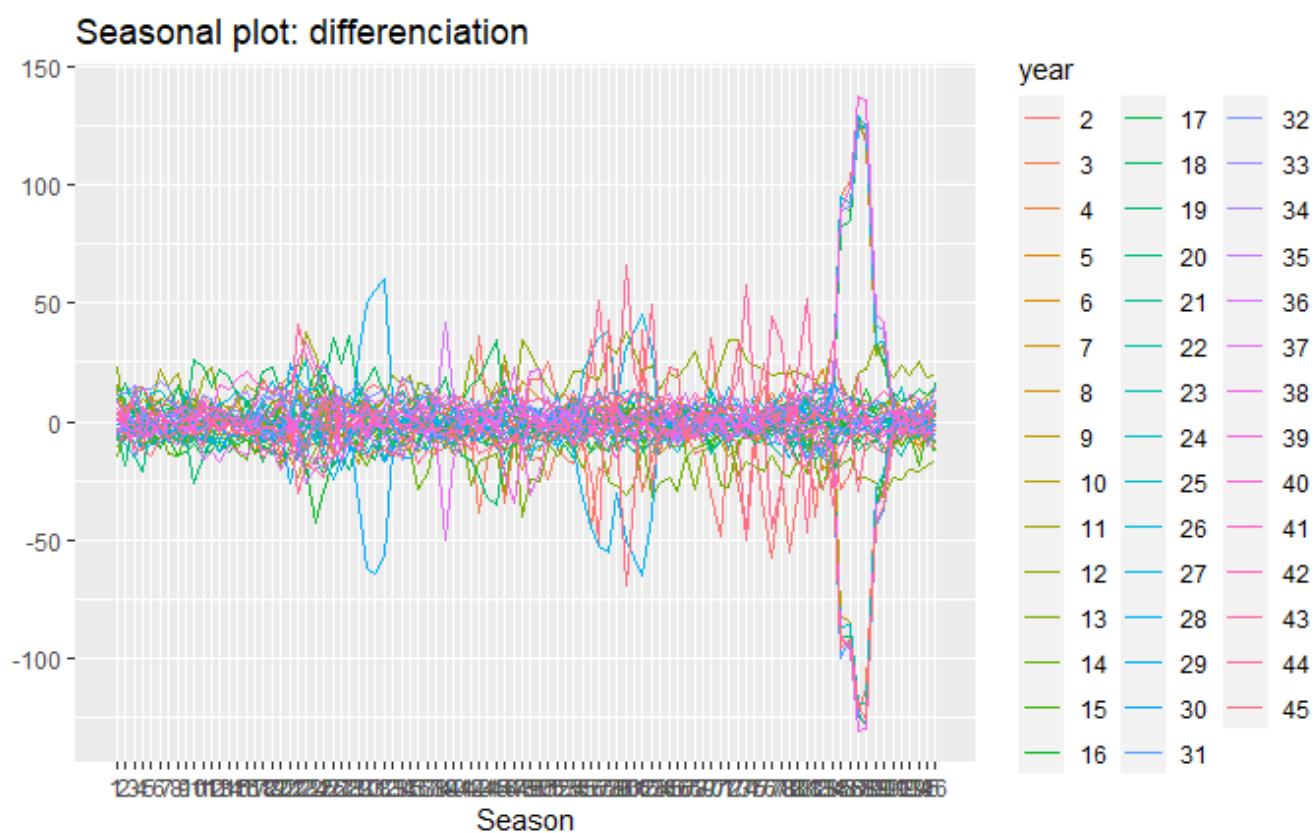
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```
differenciation=diff(elec_train,lag=96)
autoplot(differenciation)
```



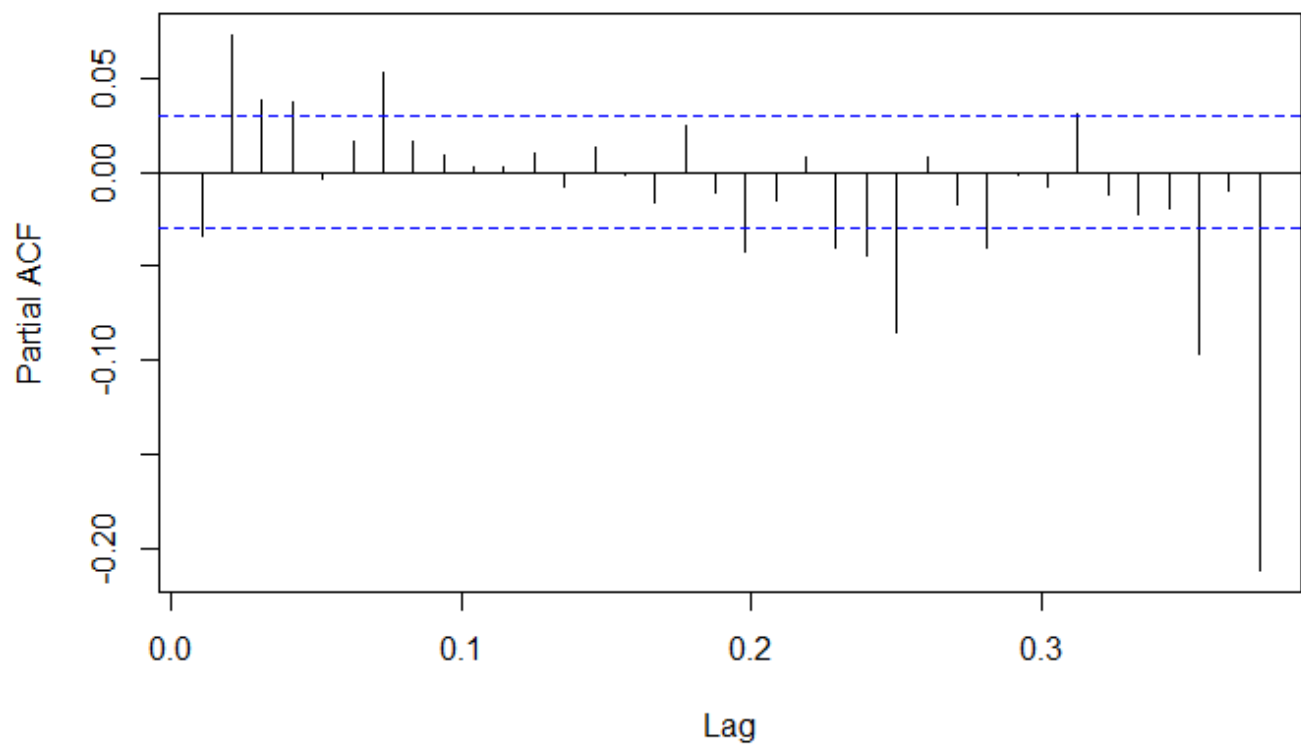
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```
ggseasonplot(differentiation)
```

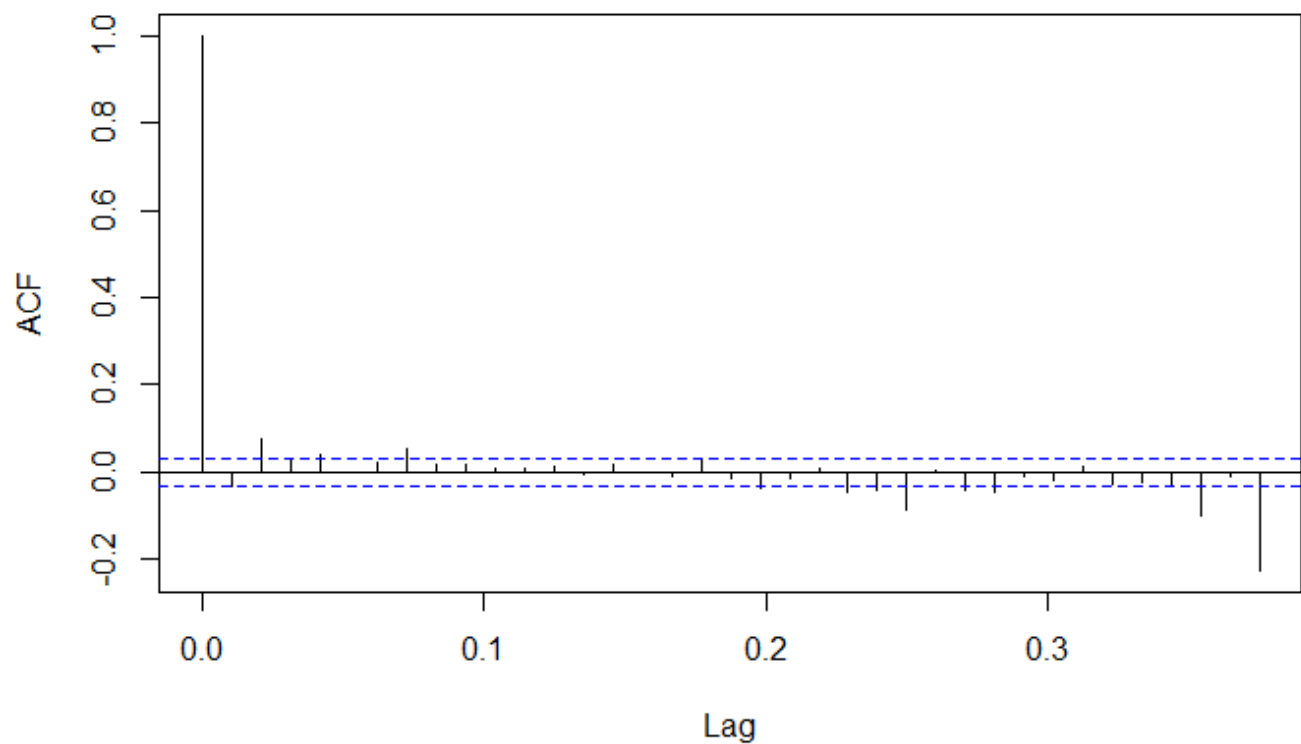


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```
diffpacf=pacf(diff(elec_train),type="cor",plot = FALSE)
plot(diffpacf)
```

[Hide](#)

```
diffacf=acf(diff(elec_train),type="cor",plot = FALSE)
plot(diffacf)
```



SARIMA

On va essayer d'utiliser les modèles auto-régressifs :

En consultant le PACF, on voit un pic sur le lag 2, On essaye le modèle suivant :

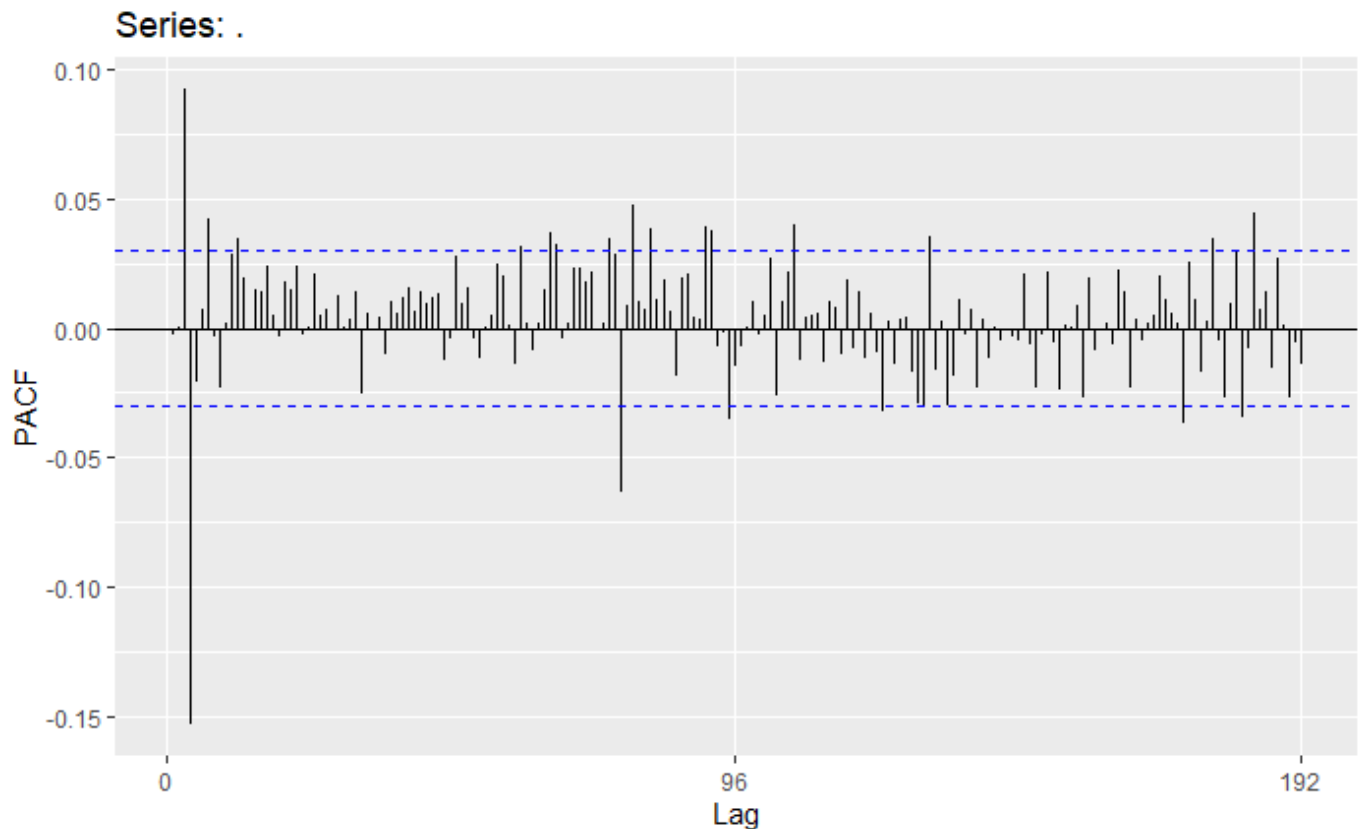
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```
prev= forecast(fitAuto)
cat("RMSE", sqrt(mean(elec_test-prev$mean)^2))
```

RMSE 9.129775

[Hide](#)

```
fit200 %>% residuals() %>% ggPacf()
```



On voit un pic sur le lag 3, on va essayer d'améliorer les performances de notre modèle :

[Hide](#)

```
fit300=Arima(elec_train, order=c(3,0,0), seasonal=c(0,1,1))#96
summary(fit300)
```

Series: elec_train
ARIMA(3,0,0)(0,1,1)[96]

Coefficients:

	ar1	ar2	ar3	sma1
	0.7070	0.0758	0.0107	-0.8665
s.e.	0.0154	0.0188	0.0154	0.0085

sigma^2 = 63.43: log likelihood = -14805.9

AIC=29621.8 AICc=29621.81 BIC=29653.54

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.3655502	7.871433	4.692265	-0.2530029	2.144352	0.5750232	-0.0006245872

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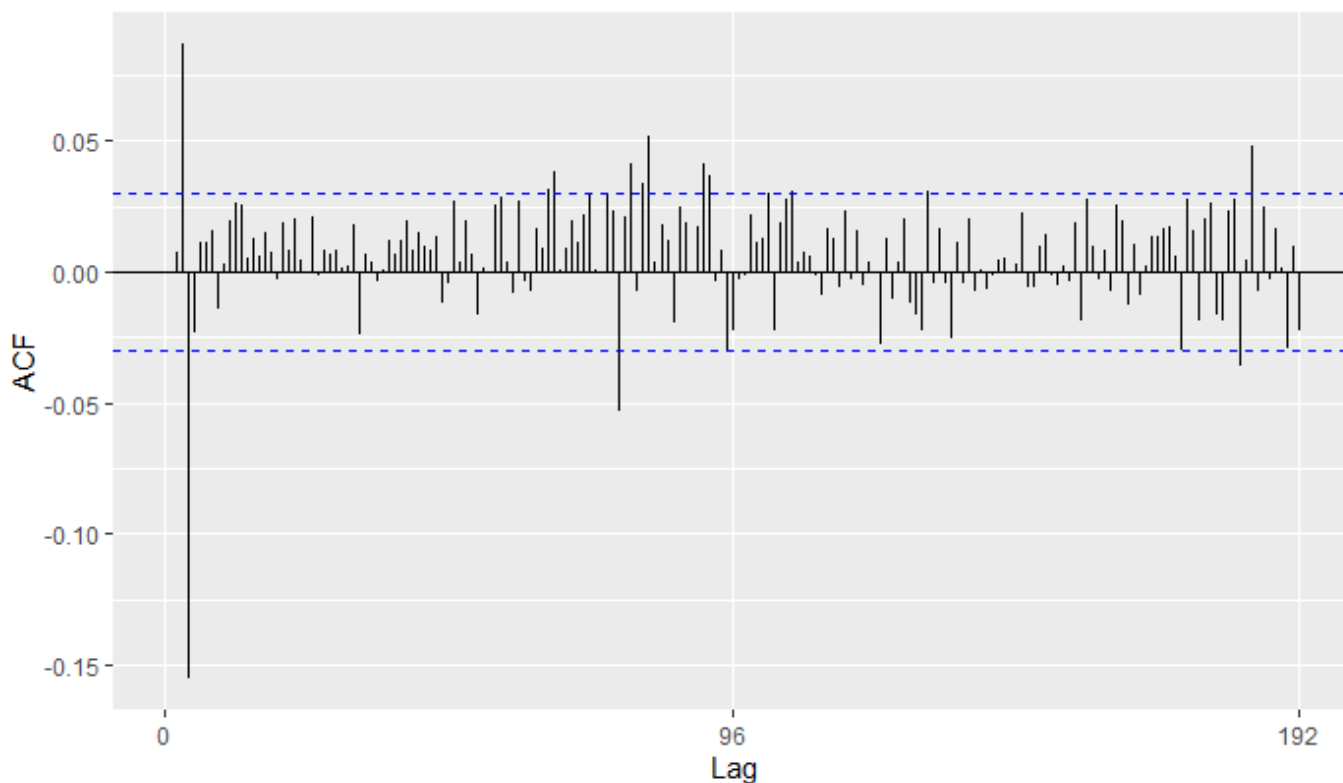
```
prevfit300= forecast(fit300)
cat("RMSE", sqrt(mean(elec_test-prevfit300$mean)^2))
```

RMSE 4.005757

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```
fit300 %>% residuals() %>% ggAcf()
```

Series: .



On voit un pic sur le ACF, sur le lag 3 :

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```
fit303=Arima(elec_train, order=c(3,0,3), seasonal=c(0,1,1))#96
prevfit303 = forecast(fit303)
cat("RMSE", sqrt(mean(elec_test-prevfit303$mean)^2))
```

RMSE 3.982057

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```
checkresiduals(fit303)
```

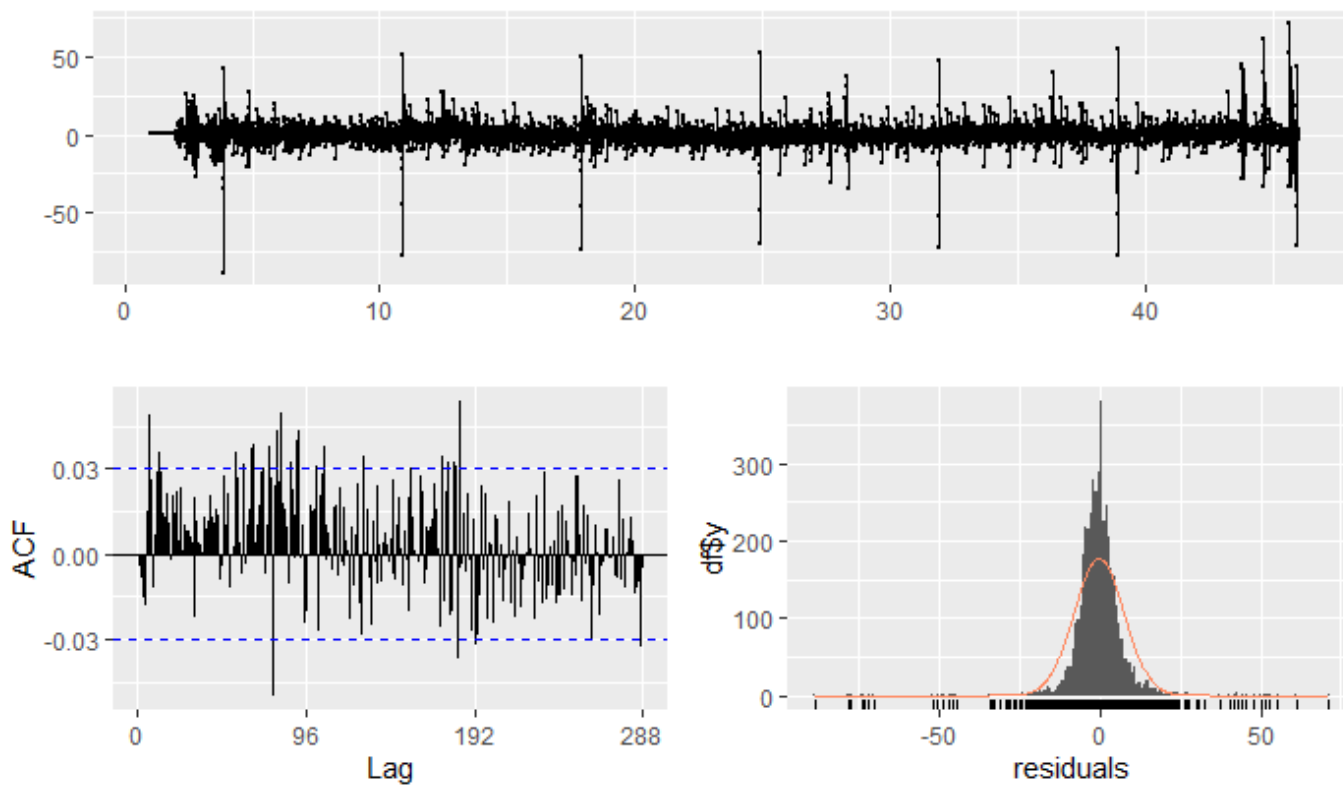
Ljung-Box test

data: Residuals from ARIMA(3,0,3)(0,1,1)[96]

$Q^* = 318.64$, $df = 185$, $p\text{-value} = 3.682e-09$

Model df: 7. Total lags used: 192

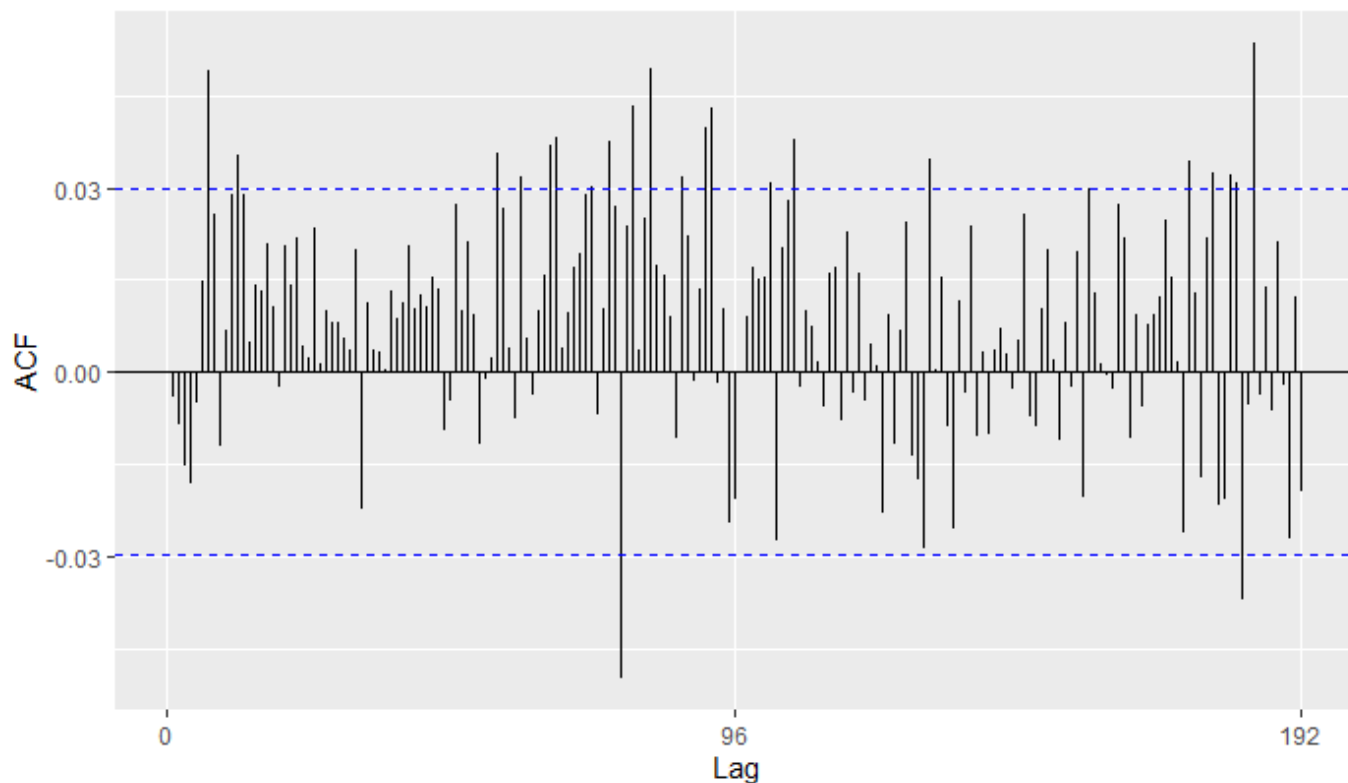
Residuals from ARIMA(3,0,3)(0,1,1)[96]



Hide

```
fit303 %>% residuals() %>% ggAcf()
```


Series: .



On voit un pic sur le lag 7, on va encore améliorer notre modèle :

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```
fit307=Arima(elec_train, order=c(3,0,7), seasonal=c(0,1,1))#96
summary(fit307)
```

Series: elec_train
ARIMA(3,0,7)(0,1,1)[96]

Coefficients:

	ar1	ar2	ar3	ma1	ma2	ma3	ma4	ma5	ma6	ma7
sma1	0.0680	0.1428	0.6068	0.6467	0.4033	-0.1743	-0.2658	-0.2454	-0.2176	-0.0490
0.8628										
s.e.	0.7076	0.5576	0.6702	0.7075	0.6475	0.1823	0.0481	0.1560	0.1898	0.0353
0.0087										

sigma^2 = 61.19: log likelihood = -14725.52
AIC=29475.03 AICc=29475.11 BIC=29551.2

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.2898195	7.724954	4.695657	-0.218786	2.144737	0.5754388	-0.001255298

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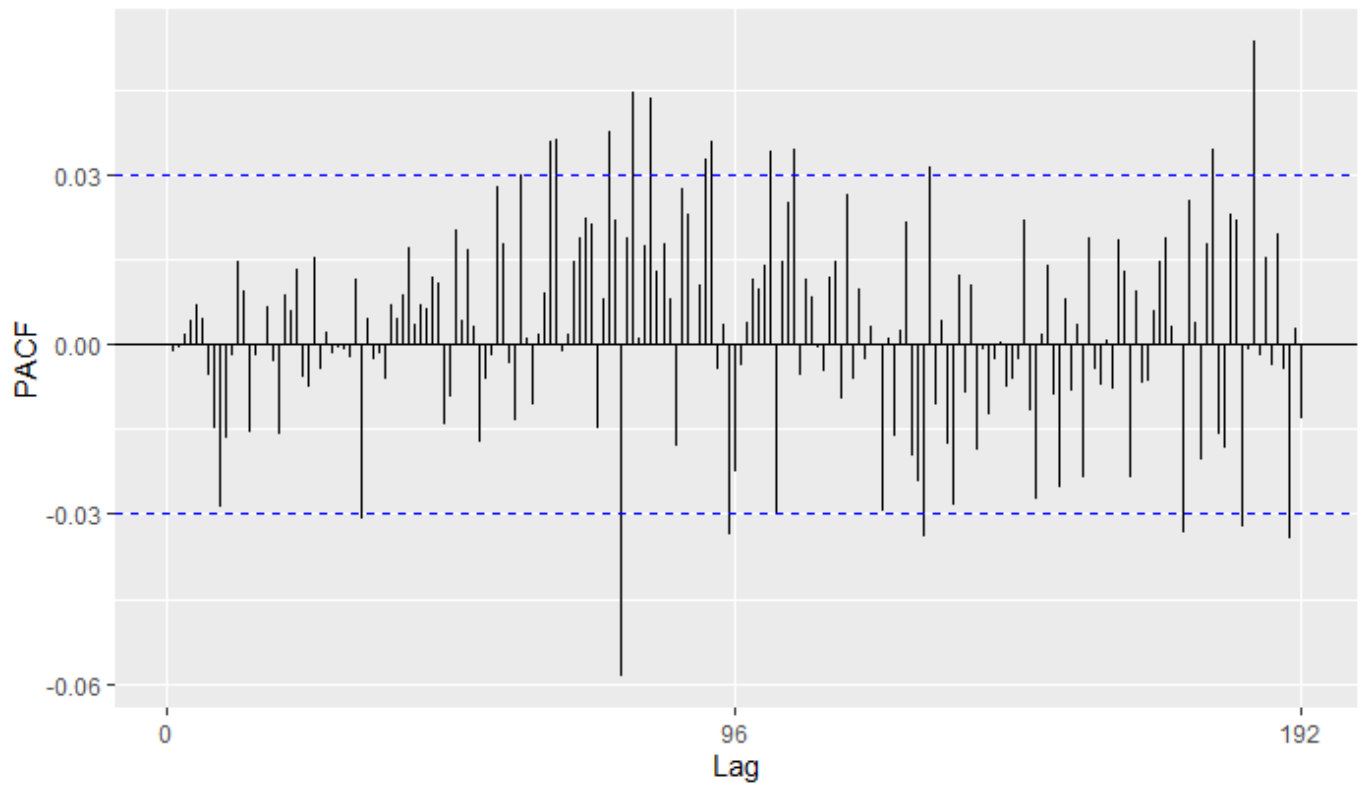
```
prevfit307 = forecast(fit307)
cat("RMSE", sqrt(mean(elec_test-prevfit307$mean)^2))
```

```
RMSE 5.081641
```

[Hide](#)

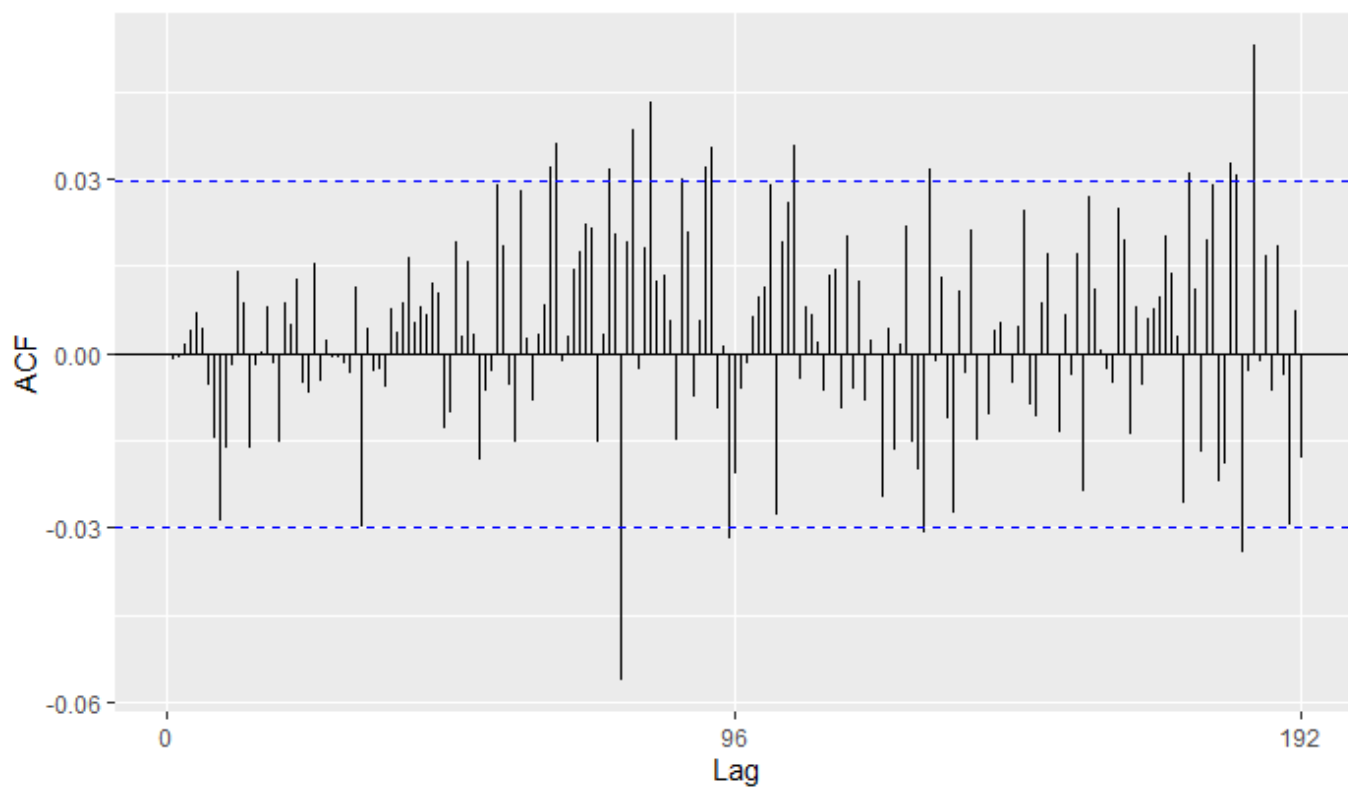
```
fit307 %>% residuals() %>% ggPacf()
```

Series: .

[Hide](#)

```
fit307 %>% residuals() %>% ggAcf()
```

Series: .

[Hide](#)

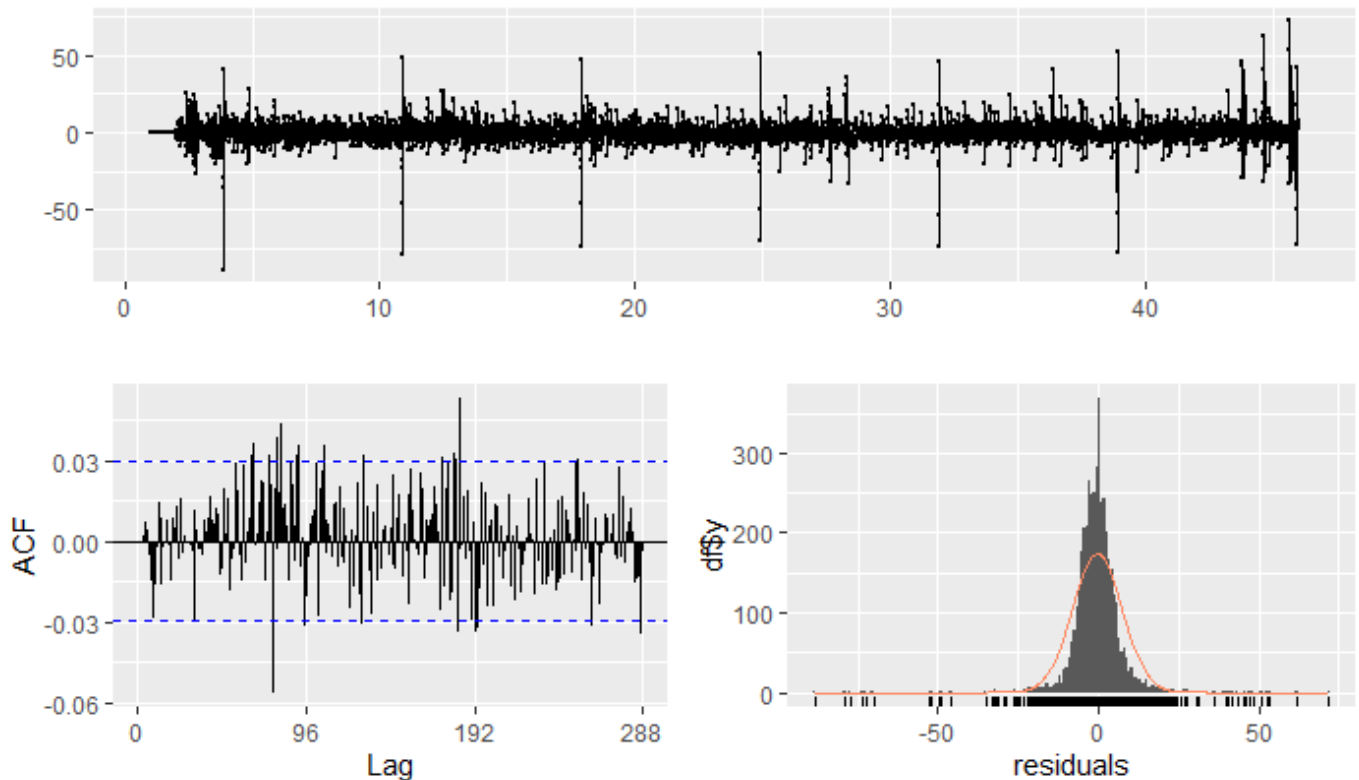
```
checkresiduals(fit307)
```

Ljung-Box test

```
data: Residuals from ARIMA(3,0,7)(0,1,1)[96]  
Q* = 248.16, df = 181, p-value = 0.0006805
```

```
Model df: 11. Total lags used: 192
```

Residuals from ARIMA(3,0,7)(0,1,1)[96]



Il reste des corrections pour capturer toutes les informations elles nécessitent une trop grande puissance de calcul pour que l'on puisse continuer.

Cependant avec une p-value 0.0006805, les bruits blanc ne sont pas pris en compte.

SARIMA Auto

On va essayer de voir ce qu'on peut obtenir avec un SARIMA automatique :

[Hide](#)

```
fitAuto=auto.arima(elec_train,lambda = "auto")
summary(fitAuto)
```

```
Series: elec_train
ARIMA(5,0,1)(0,1,0)[96]
Box Cox transformation: lambda= 0.443743

Coefficients:
      ar1      ar2      ar3      ar4      ar5      ma1
    0.9335  -0.0531  0.0256  -0.2543  0.1586  -0.1900
s.e.  0.0996   0.0747  0.0223   0.0208  0.0195   0.1007
```

```
sigma^2 = 0.2459: log likelihood = -3024.7
AIC=6063.4  AICc=6063.43  BIC=6107.83
```

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.0871035	10.08052	5.942022	-0.1357493	2.701743	0.7281771	0.0007368769

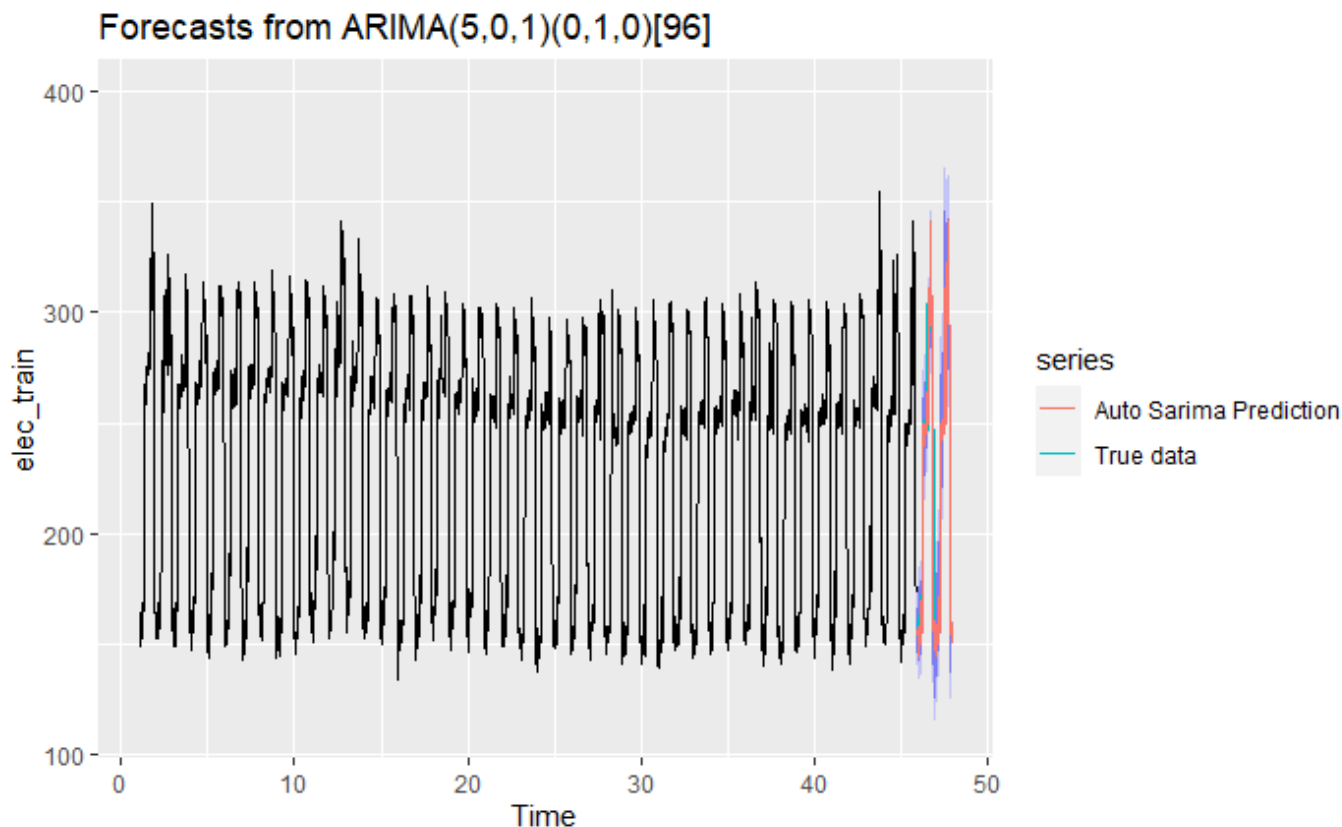
[Hide](#)

```
prev= forecast(fitAuto)
cat("RMSE", sqrt(mean(elec_test-prev$mean)^2))
```

RMSE 9.129775

[Hide](#)

```
autoplot(prev) + autolayer(elec_test, series="True data")+ autolayer(prev$mean, series="Auto
Sarima Prediction")
```



Les résultats de ce modèle sont inférieure à ce que l'on a trouvé auparavant

NEURAL NETWORK

On essaye de faire une prédiction avec un réseau de neurones

[Hide](#)

```
NNfit=nnetar(elec_train)
summary(NNfit)
```

	Length	Class	Mode
x	4315	ts	numeric
m	1	-none-	numeric
p	1	-none-	numeric
P	1	-none-	numeric
scalex	2	-none-	list
size	1	-none-	numeric
subset	4315	-none-	numeric
model	20	nnetarmodels	list
nnetargs	0	-none-	list
fitted	4315	ts	numeric
residuals	4315	ts	numeric
lags	12	-none-	numeric
series	1	-none-	character
method	1	-none-	character
call	2	-none-	call

Hide

```
prevNNfit= forecast(NNfit)
cat("RMSE", sqrt(mean(elec_test-prevNNfit$mean)^2))
```

RMSE 8.360124

Le résultat n'est pas assez performant, comparé aux RMSE du SARIMA

Holt-Winters

On essaye de faire une prédiction avec un Holt-Winters.

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```
fitHW= HoltWinters(elec_train)
summary(fitHW)
```

	Length	Class	Mode
fitted	16876	mts	numeric
x	4315	ts	numeric
alpha	1	-none-	numeric
beta	1	-none-	numeric
gamma	1	-none-	numeric
coefficients	98	-none-	numeric
seasonal	1	-none-	character
SSE	1	-none-	numeric
call	2	-none-	call

Hide

```
prevfitHW= forecast(fitHW)
cat("RMSE", sqrt(mean(elec_test-prevfitHW$mean)^2))
```

RMSE 9.046928

De même pour cette méthode, le résultat n'est pas assez performant

Choix Modèle

Même si le modèle SARIMA(3,0,3)(0,1,1)[96] n'est pas le modèle qui a capté le plus d'informations.

C'est le modèle avec le RMSE le plus bas : 3.982057

Son bruit blanc n'est pas pris en compte avec une p-value = 3.682e-09

Export des prédictions

Pour la prévision sans l'utilisation de la température extérieure

[Hide](#)

```
fit303F=Arima(elec_prev, order=c(3,0,3), seasonal=c(0,1,1))#96
prevFinal = forecast(fit303F, h=96)
```

[Hide](#)

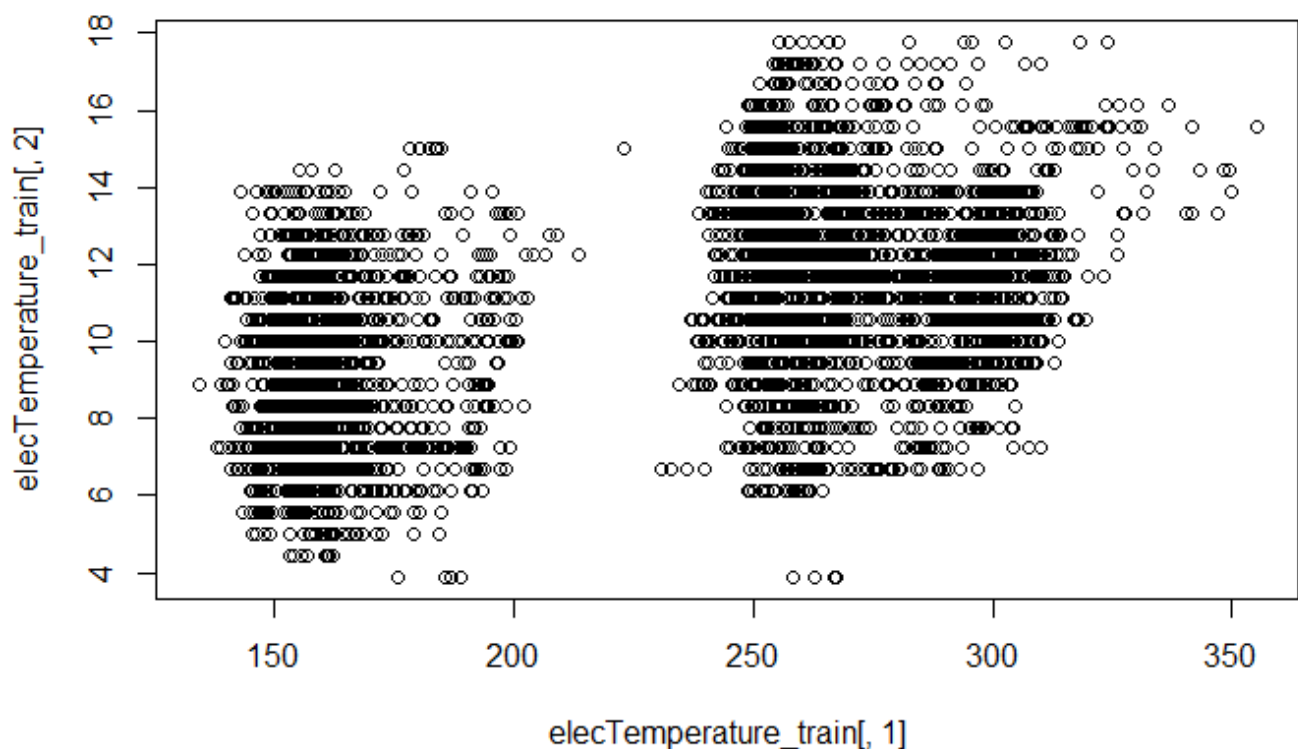
```
write.xlsx(as.data.frame(prevFinal$mean), "exportPower.xlsx")
```

Utilisation de la variable Temperature

On va d'abord essayer de voir si il y a correlation entre les variables Temperature et Power

[Hide](#)

```
plot(elecTemperature_train[,1], y=elecTemperature_train[,2])
```

[Hide](#)

```
cor(elecTemperature_train)
```

	Power (kW)	Temp (C°)
Power (kW)	1.0000000	0.4722473
Temp (C°)	0.4722473	1.0000000

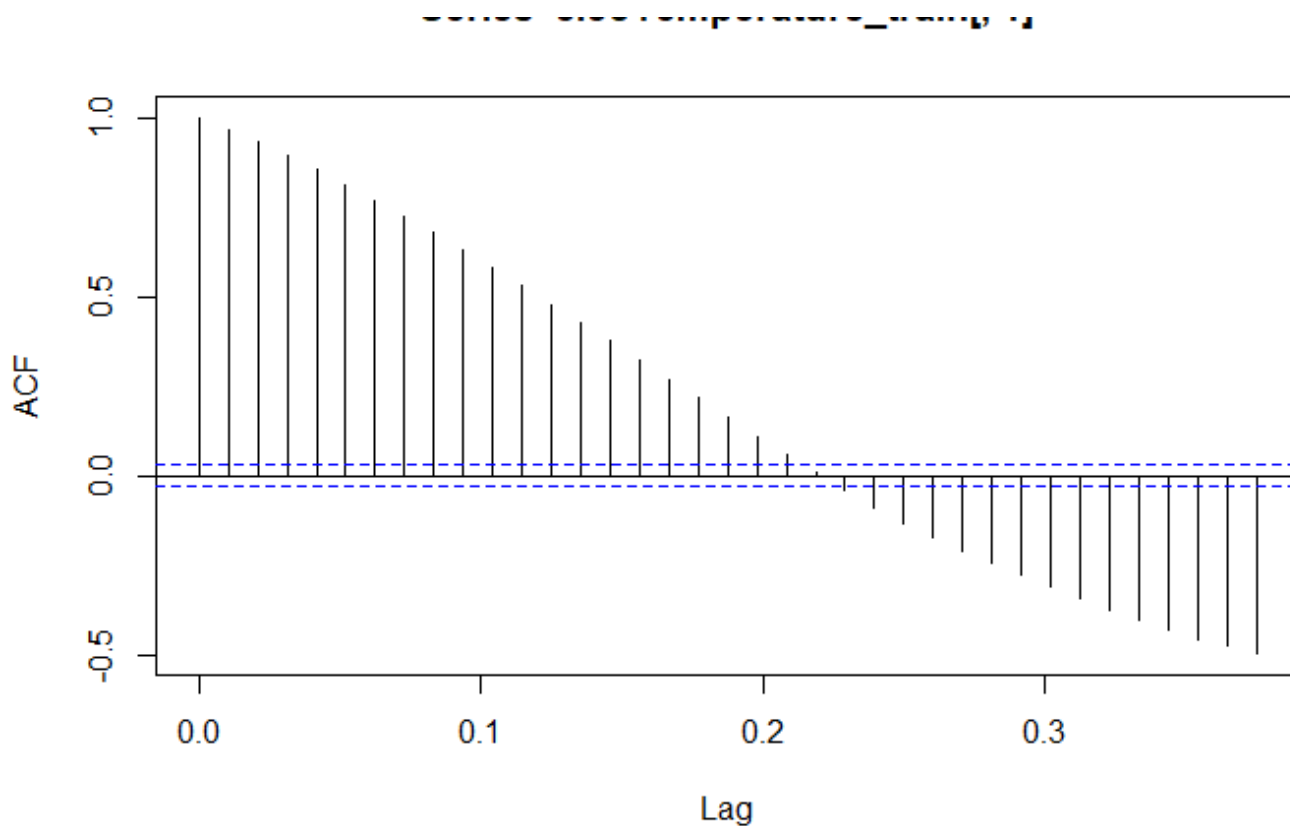
Nous obtenons une valeur de 0.472

Les variables ne semblent pas vraiment corrélées.

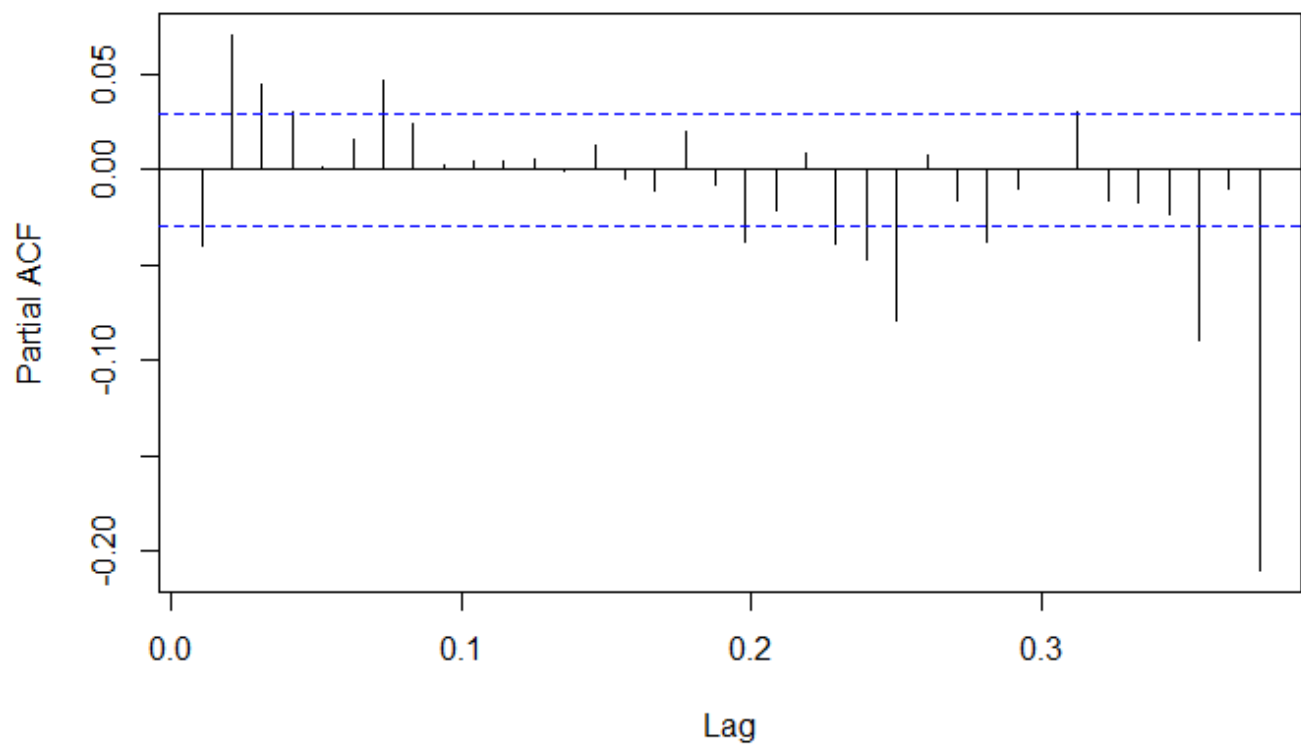
Prévisions

[Hide](#)

```
tmp=acf(elecTemperature_train[,1],type="cor",plot = FALSE)  
plot(tmp)
```

[Hide](#)

```
diffpacf=pacf(diff(elecTemperature_train[,1]),type="cor",plot = FALSE)  
plot(diffpacf)
```

On remarque à nouveau une saisonnalité et avec le PACF on a un pic du lag à 2

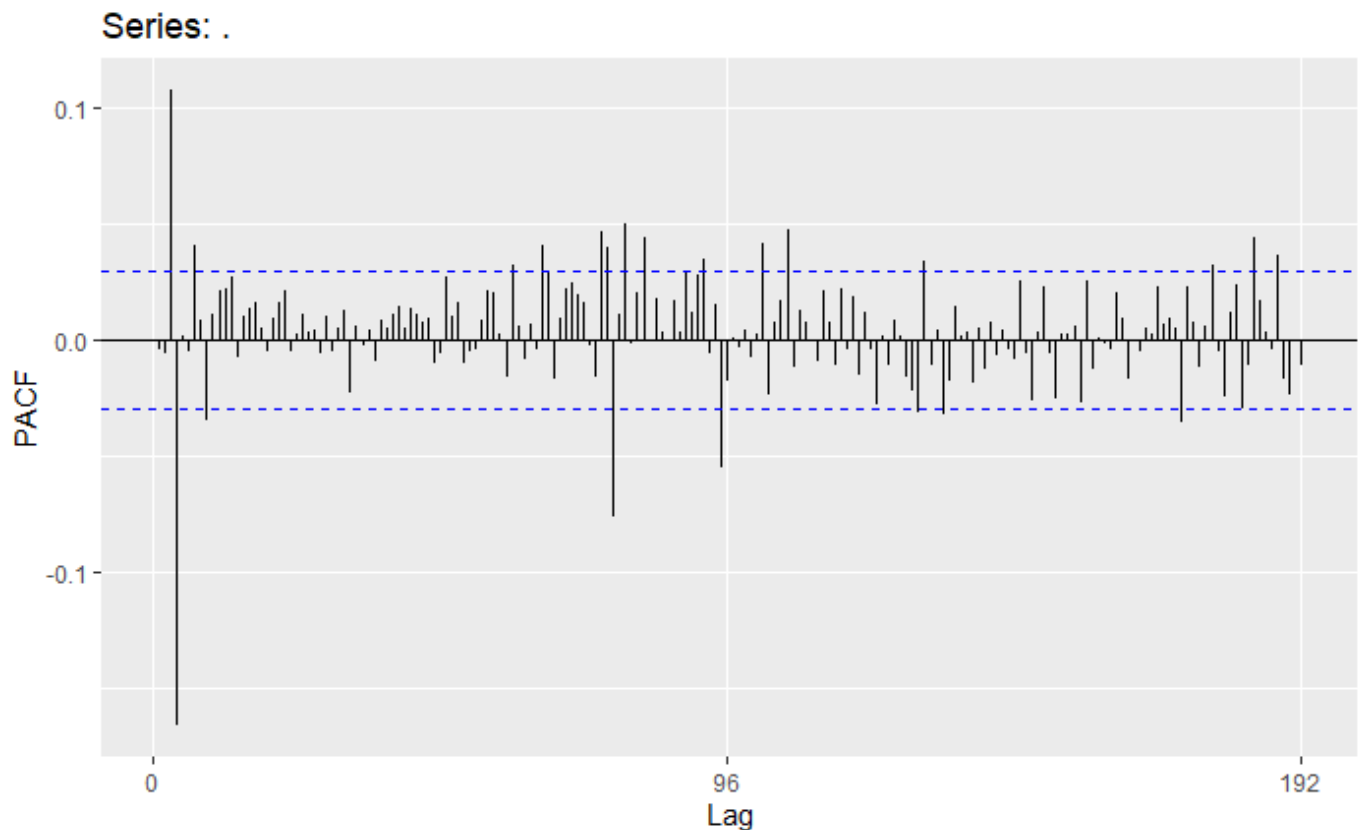
Hide

```
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevfit200Temp$mean)^2))
```

```
RMSE 3.261178
```

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```
fit200Temp %>% residuals() %>% ggPacf()
```



Grâce au PACF, on voit un pic au lag 3, on va améliorer le modèle

Hide

```
fit400Temp=Arima(elecTemperature_train[,1], order=c(4,0,0), seasonal=c(0,1,1), xreg = elecTem
perature_train[,2])#96
summary(fit400Temp)
```

Series: elecTemperature_train[, 1]
Regression with ARIMA(4,0,0)(0,1,1)[96] errors

Coefficients:

	ar1	ar2	ar3	ar4	sma1	xreg
	0.6792	0.0959	0.1244	-0.1493	-0.8631	0.7070
s.e.	0.0151	0.0182	0.0182	0.0152	0.0084	0.2005

sigma^2 = 64.55: log likelihood = -15176.92

AIC=30367.84 AICc=30367.87 BIC=30412.43

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.4237798	7.94078	4.791944	-0.2784618	2.180156	0.57578	0.01656161

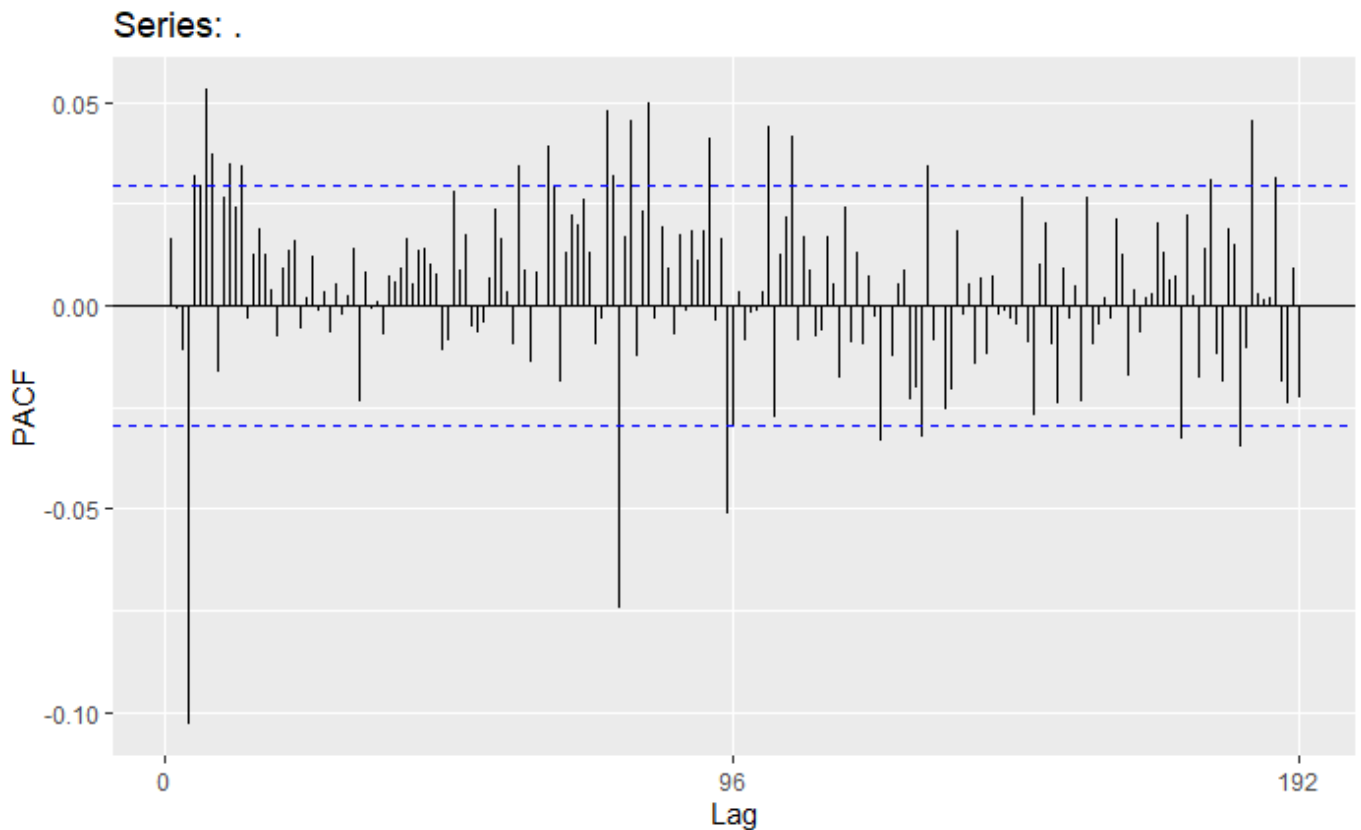
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```
prevfit400Temp= forecast(fit400Temp, xreg=elecTemperature_test[,2])
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevfit400Temp$mean)^2))
```

RMSE 3.380815

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```
fit400Temp %>% residuals() %>% ggPacf()
```



On observe toujours un pic sur le lag 4 on va essayer d'en prendre un autre pic ici avec le lag 7

[Hide](#)

```
fit700Temp=Arima(elecTemperature_train[,1], order=c(7,0,0), seasonal=c(0,1,1), xreg = elecTem
perature_train[,2])#96
summary(fit700Temp)
```

Series: elecTemperature_train[, 1]
Regression with ARIMA(7,0,0)(0,1,1)[96] errors

Coefficients:

	ar1	ar2	ar3	ar4	ar5	ar6	ar7	sma1	xreg
	0.7136	0.0821	0.0913	-0.2222	0.0803	0.0347	0.0243	-0.8614	0.5014
s.e.	0.0154	0.0189	0.0189	0.0187	0.0191	0.0191	0.0157	0.0087	0.2253

sigma^2 = 61.29: log likelihood = -14729.48

AIC=29478.96 AICc=29479.01 BIC=29542.43

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.3477228	7.733109	4.693706	-0.2438774	2.143879	0.5753418	-0.001330753

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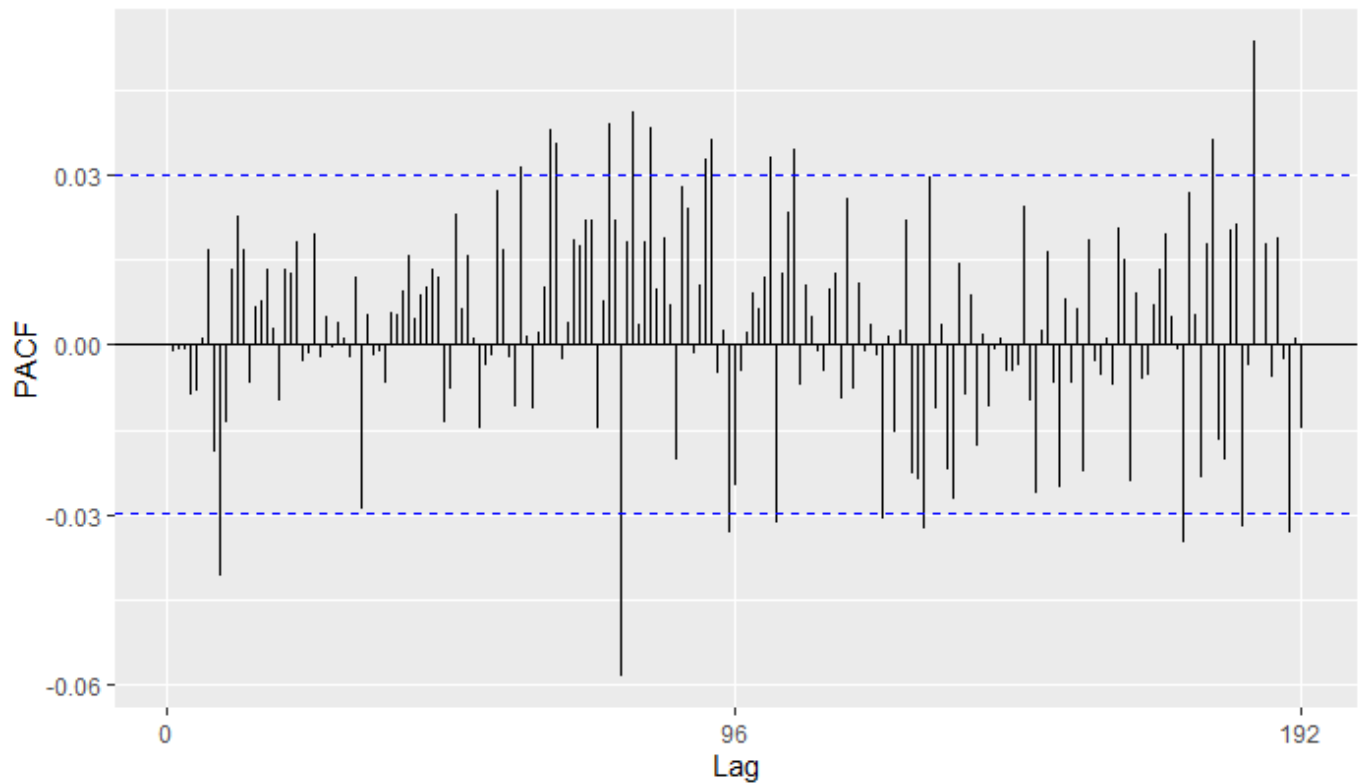
```
prevfit700Temp= forecast(fit700Temp, xreg=elecTemperature_test[,2])
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevfit700Temp$mean)^2))
```

RMSE 4.657614

Hide

```
fit700Temp %>% residuals() %>% ggPacf()
```

Series: .



On observe un pic sur le lag 9 on va essayer d'améliorer le modèle

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```
fit900Temp=Arima(elecTemperature_train[,1], order=c(9,0,0), seasonal=c(0,1,1), xreg = elecTem  
perature_train[,2])#96  
  
summary(fit900Temp)
```

Series: elecTemperature_train[, 1]
 Regression with ARIMA(9,0,0)(0,1,1)[96] errors

Coefficients:

	ar1	ar2	ar3	ar4	ar5	ar6	ar7	ar8	ar9	sma1	xr
eg	0.6944	0.0838	0.1185	-0.2455	0.105	0.0108	0.0452	-0.0136	-0.0066	-0.8659	0.60
58											
s.e.	0.0152	0.0186	0.0186	0.0187	0.019	0.0186	0.0186	0.0185	0.0153	0.0085	0.21
99											

sigma^2 = 63.38: log likelihood = -15136
 AIC=30296.01 AICc=30296.08 BIC=30372.45

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.3546927	7.864058	4.771477	-0.2482636	2.169055	0.5733208	-0.001483967

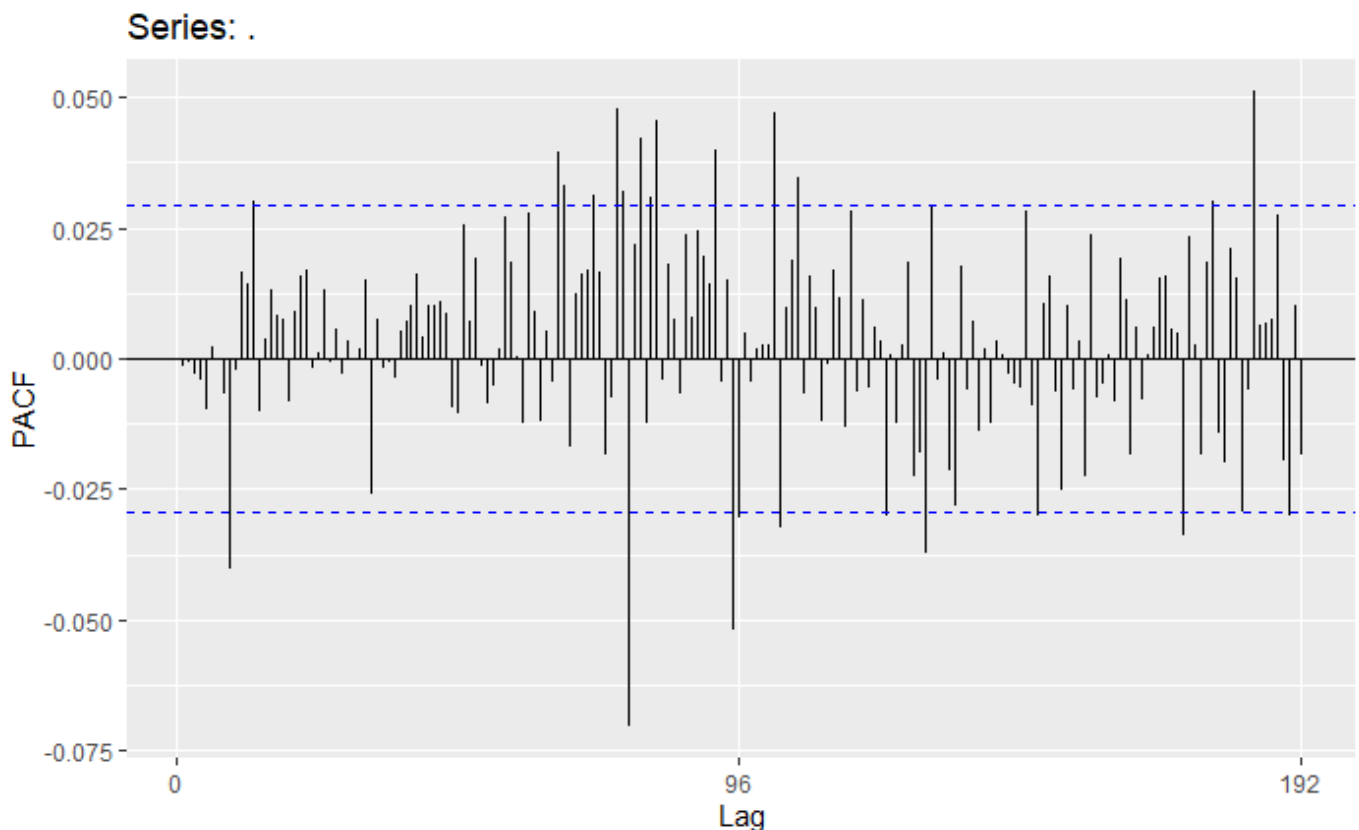
Hide

```
prevfit900Temp= forecast(fit900Temp, xreg=elecTemperature_test[,2])
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevfit900Temp$mean)^2))
```

RMSE 3.143429

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```
fit900Temp %>% residuals() %>% ggPacf()
```



On observe un pic sur le lag 8 on va essayer d'améliorer le modèle

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```
fit800Temp=Arima(elecTemperature_train[,1], order=c(8,0,0), seasonal=c(0,1,1), xreg = elecTem
perature_train[,2])#96
summary(fit800Temp)
```

Series: elecTemperature_train[, 1]
 Regression with ARIMA(8,0,0)(0,1,1)[96] errors

Coefficients:

	ar1	ar2	ar3	ar4	ar5	ar6	ar7	ar8	sma1	xreg
	0.6946	0.0835	0.1184	-0.2461	0.1066	0.0100	0.0447	-0.0181	-0.8660	0.5986
s.e.	0.0152	0.0185	0.0186	0.0186	0.0186	0.0186	0.0185	0.0153	0.0085	0.2200

sigma^2 = 63.37: log likelihood = -15136.1

AIC=30294.2 AICc=30294.26 BIC=30364.26

Training set error measures:

	ME	RMSE	MAE	MPE	MAPE	MASE	ACF1
Training set	-0.3522732	7.864132	4.770965	-0.2472987	2.168549	0.5732593	-0.00192004

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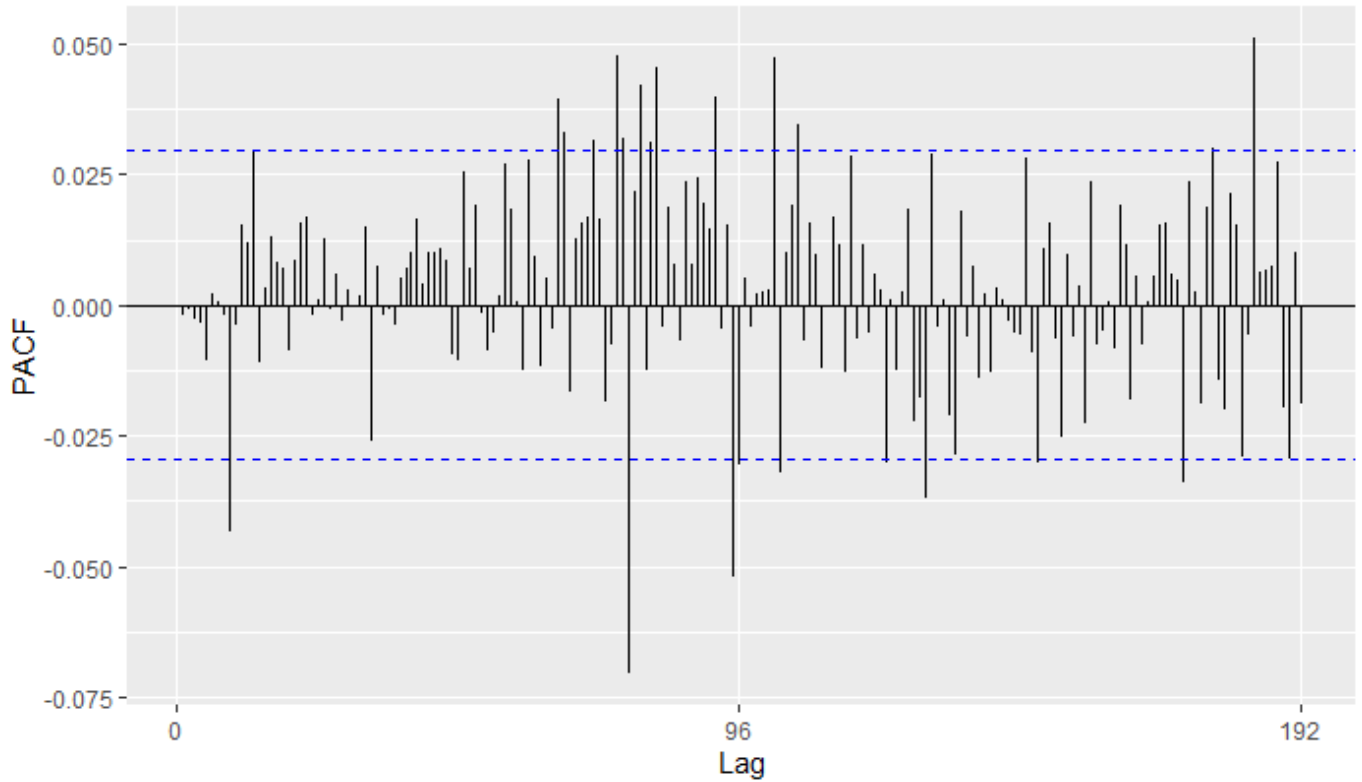
```
prevfit800Temp= forecast(fit800Temp, xreg=elecTemperature_test[,2])
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevfit800Temp$mean)^2))
```

RMSE 3.137962

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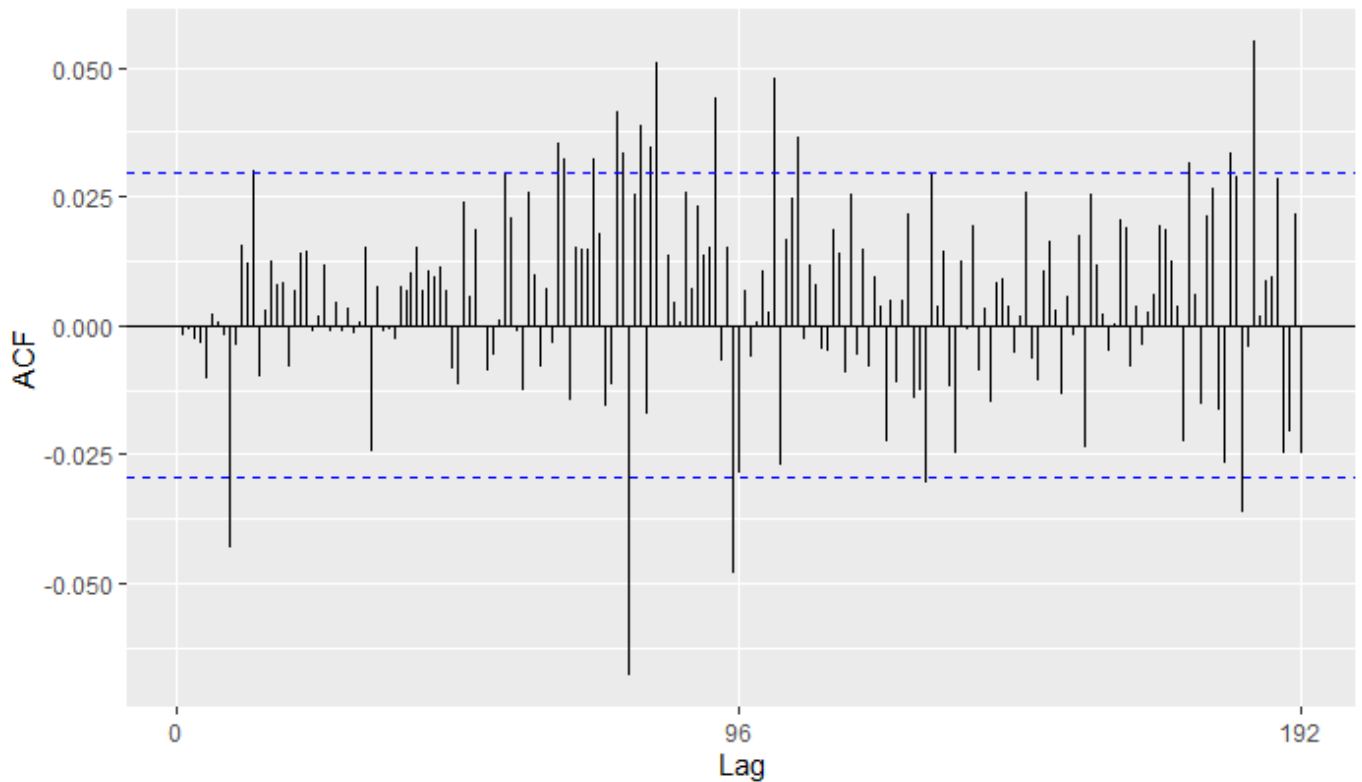
```
fit800Temp %>% residuals() %>% ggPacf()
```

Series: .

[Hide](#)

```
fit800Temp %>% residuals() %>% ggAcf()
```

Series: .



On arrive plus à stabiliser les pic des lag, cela nécessite trop de performances.

NEURAL NETWORK

On essaye de faire une prédiction avec un réseau de neurones.

[Hide](#)

```
NNfitTemp=nnetar(elecTemperature_train[,1], xreg = elecTemperature_train[,2])
summary(NNfitTemp)
```

	Length	Class	Mode
x	4411	ts	numeric
m	1	-none-	numeric
p	1	-none-	numeric
P	1	-none-	numeric
scalex	2	-none-	list
scalexreg	2	-none-	list
size	1	-none-	numeric
xreg	4411	-none-	numeric
subset	4411	-none-	numeric
model	20	nnetarmodels	list
nnetargs	0	-none-	list
fitted	4411	ts	numeric
residuals	4411	ts	numeric
lags	17	-none-	numeric
series	1	-none-	character
method	1	-none-	character
call	3	-none-	call

[Hide](#)

```
prevNNfitTemp= forecast(NNfitTemp, xreg=elecTemperature_test[,2])
cat("RMSE", sqrt(mean(elecTemperature_test[,1]-prevNNfitTemp$mean)^2))
```

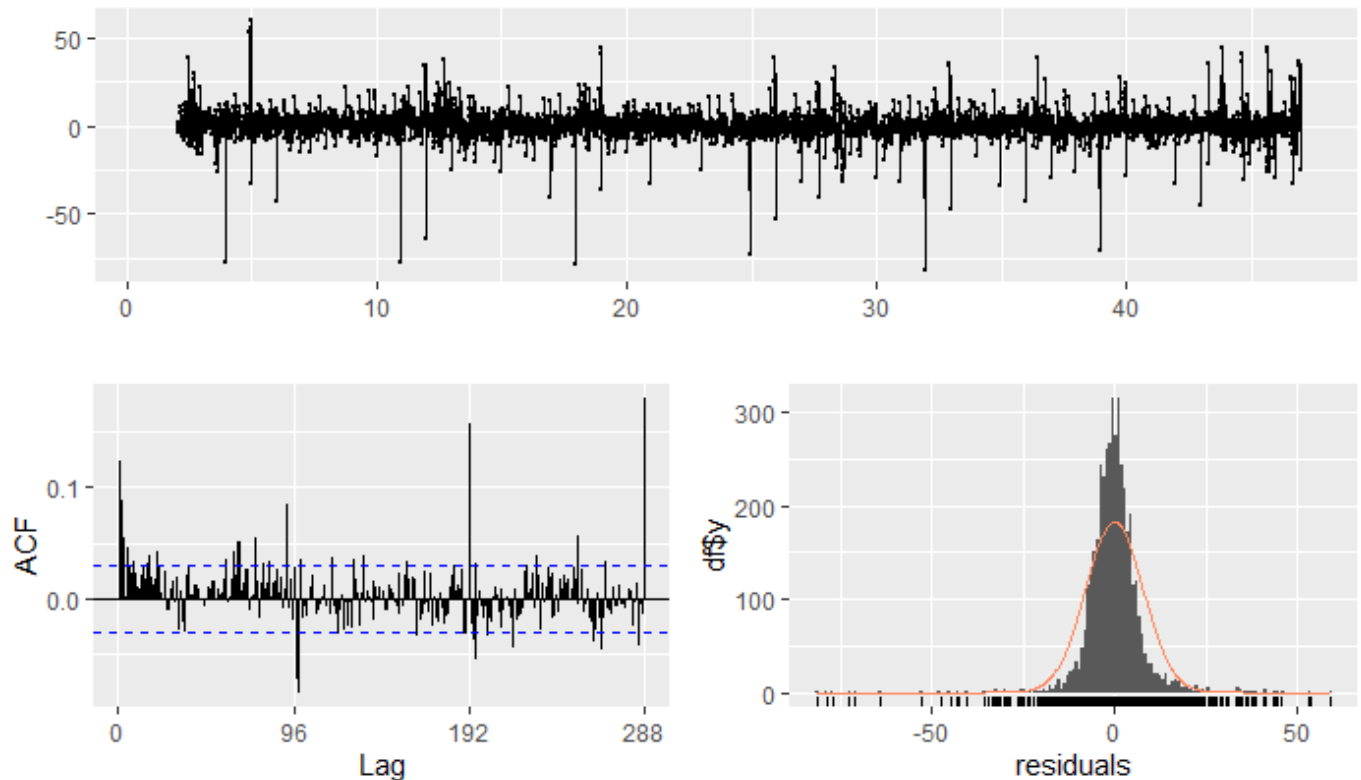
RMSE 1.208937

[Hide](#)

```
checkresiduals(NNfitTemp)
```

```
Warning in modeldf.default(object) :
  Could not find appropriate degrees of freedom for this model.
```


Residuals from NNAR(16,1,10)[96]



Le résultat est très satisfaisant comparé aux RMSE du SARIMA

Pour la prévision avec l'utilisation de la température extérieure

Les prédictions semblent vraiment similaires avec ou sans la variable température, on a aperçu une petite différence de performances entre les modèles.

Le modèle utilisant un réseau de neurone s'est démarqué avec un RMSE bizarrement bas de 1.208937.

Exportation des résultats

[Hide](#)

```
fitFinaltemp = nnetar(elecTemperature_prev[1:4507,1], xreg = elecTemperature_prev[1:4507,2])
prevFinalTemp= forecast(fitFinaltemp, xreg=elecTemperature_prev[4508:4603,2])
write.xlsx(as.data.frame(prevFinalTemp$mean), "exportPowerTemp.xlsx")
```

A noter que dans le fichier prédiction :

La première colonne contient les prédictions SANS la variable température.

La deuxième colonne contient les prédictions AVEC la variable température.