

## Contents

---

- [Forward Kinematics](#)
- [Jacobian](#)
- [Cartesian space velocity](#)
- [Desired Position in cartesian coordinate](#)

```
function [ dx ] = odeInverseDyn(t,x,system_params)
```

```
% note x is in the form of q_1, q_2,dot q_1, dot q_2

% Extracting the system params
I1=system_params(1); I2 = system_params(2); m1=system_params(3); r1=system_params(4); m
2=system_params(5); r2=system_params(6); l1=system_params(7); l2=system_params(8);
g=9.8;

a = I1+I2+m1*r1^2+ m2*(l1^2+ r2^2);
b = m2*l1*r2;
d = I2+ m2*r2^2;

% the actual dynamic model of the system:
Mmat = [a+2*b*cos(x(2)), d+b*cos(x(2)), d+b*cos(x(2)), d];
Cmat = [-b*sin(x(2))*x(4), -b*sin(x(2))*(x(3)+x(4)); b*sin(x(2))*x(3),0];
Gmat = [m1*g*r1*cos(x(1))+m2*g*(l1*cos(x(1))+r2*cos(x(1)+x(2)));
m2*g*r2*cos(x(1)+x(2))];
invM = inv(Mmat);
invMC = invM*Cmat;
```

Not enough input arguments.

Error in odeInverseDyn (line 5)

```
I1=system_params(1); I2 = system_params(2); m1=system_params(3); r1=system_params(4); m
2=system_params(5); r2=system_params(6); l1=system_params(7); l2=system_params(8);
```

## Forward Kinematics

---

```
q1=x(1);
q2=x(2);
q1_dot=x(3);
q2_dot=x(4);

X=l1*cos(q1)+l2*cos(q1+q2);
Y=l1*sin(q1)+l2*sin(q1+q2);
```

## Jacobian

```
J=[-l1*sin(q1)-l2*sin(q1+q2) -l2*sin(q1+q2);l1*cos(q1)+l2*cos(q1+q2) l2*cos(q1+q2)];  
  
Jdot = [-l1*cos(q1)*q1_dot-l2*cos(q1+q2)*(q1_dot+q2_dot) -l2*cos(q1+q2)*(q1_dot+q2_dot);  
...  
-l1*sin(q1)*q1_dot-l2*sin(q1+q2)*(q1_dot+q2_dot) -l2*sin(q1+q2)*(q1_dot+q2_dot)];
```

## Cartesian space velocity

```
xdot = J*[q1_dot;q2_dot];
```

## Desired Position in cartesian coordinate

```
r=0.5;  
x_d = [r*sin(t);r*cos(t)];  
dx_d = [r*cos(t);-r*sin(t)];  
ddx_d = [-r*sin(t);-r*cos(t)];  
dtheta = x(3:4,1);
```

```
% Inverse Dynamic controller controller  
  
% Initialize the gain matrix  
KP=50;  
KD=35;  
  
ddx = ddx_d - KP*([X;Y]-x_d) - KD*(xdot - dx_d);  
Torque = Mmat*(pinv(J)*(ddx) - Jdot*[x(3);x(4)])+ Cmat*dtheta +Gmat;  
dx = [x(3);x(4);invM*(Torque - Gmat) - invM*Cmat*dtheta];
```

```
end
```