

Informal Description:

(Initialize) The input of this Turing Machine is a binary string flanked by one x character on each edge, and the output is the binary string shifted right by one bit and also flanked by one x character on each edge. Assuming the input is correctly formatted and cannot be empty.

(Shift Binary String to the right by one bit) We start from state q_0 , scanning the tape from the leftmost, when we see an x, moving the head to right once to state q_1 . Continue scanning the tape, if it's not x move the head to the right until we see an x which means we reach the end of the input tape, moving the head to left once and getting into state q_2 , no matter what character the head is pointing at, moving the head to left once and getting into state q_3 . At state q_3 , we have three options:

(1) An x is met, moving the head to right once and getting into state q_4 , no matter what character the head is pointing at, change the character to 0 and move the head to left once (pointing at the leftmost x).

Therefore, it gets into q_{halt} , and we claim the shifting binary string to the right by one bit succeeds and the output has been accepted.

(2) A 0 is met, moving the head to right once and getting into state q_5 , no matter what character the head is pointing at, change the character to 0 and move the head to left once and get into state q_7 , no matter what character is met move the head to left once back to q_3 . There are three situations:

(a.) An x is met, moving the head to right once and getting into state q_4 , no matter what character the head is pointing at, change the character to 0 and move the head to left once (pointing at the leftmost x).

Therefore, it gets into q_{halt} , and we claim the shifting binary string to the right by one bit succeeds and the output has been accepted.

(b.) A 0 is met, follow the same steps (in (2)) above from states q_3 -- q_5 -- q_7 until we see an x, moving the head to right once and getting into state q_4 , no matter what character the head is pointing at, change the character to 0 and move the head to left once (pointing at the leftmost x). Therefore, it gets into q_{halt} , and we claim the shifting binary string to the right by one bit succeeds and the output has been accepted.

(c.) A 1 is met, moving the head to right once and getting into state q_6 , no matter what character we met, change it to 1 then move the head to the left once and get into state q_7 , no matter what character the head is pointing to, moving the head to left and getting into q_3 , we follow the same steps above from (2a) to (2c) until we see an x, then we follow the steps in (1)

(3) A 1 is met, moving the head to right once and getting into state q_6 , no matter what character we met, change it to 1 then move the head to the left once and get into state q_7 , no matter what character the head is pointing to, moving the head to left and getting into q_3 , then we follow the steps above from (2a) to (2c)

Result Discussion: Therefore, by the examples, edge cases, and how this Turing Machine went, we can conclude that this Turing Machine that implements the SHIFT instruction succeeds. The input is a binary string flanked by one x character on each edge, and the output is the binary string shifted right by one bit and also flanked by one x character on each edge.