

Fixed Income Securities

INDIVIDUAL PROJECT ASSIGNMENT, 2020-21

1. Consider a government **inflation linked bond** with the following term sheet:

Notional amount	1000
Coupon Type	Fixed
Coupon rate	3.75%
Coupon frequency	Semi-annual
Currency	USD
Issue Date	31/7/2015
Maturity Date	15/7/2025
Trade Date	24/10/2015
Settlement Lag	T+1
Day Count	Act/Act
Inflation Reference Index	CONSUMER PRICE INDEX US
Inflation Reference Index Level at issue	237.14365
Inflation Reference Index Level at Settlement	237.46721

Assume the CPI index I_t follows a log-normal model (geometric Brownian motion), i.e.,

$$\frac{dI_t}{I_t} = \mu dt + \sigma dW_t,$$

where W_t is a Wiener process, μ the constant drift, and $\sigma > 0$ is the diffusion coefficient with estimates $\hat{\mu} = 0.03513$ and $\hat{\sigma} = 0.022439$.

Assume the issuers yield curve on the valuation date is given by the Nelson–Siegel–Svensson zero-coupon rate function parameters,

β_0	β_1	β_2	β_3	τ_1	τ_2
5.9%	-1.6%	-0.5%	1%	5	0.5

Tasks:

- Compute the accrued interest.
- Simulate 1000 scenarios for the inflation rate curve and CPI index
- For each scenario, compute the inflation linked bond cash flows and estimate the fair value.
- Summarise and analyse the inflation linked bond price distribution, including risk measures

PROJECT MILESTONES/REPORTS

A single individual written printed report must be submitted no later than **November 7, 2020** (use the Professor Mail box N.º 16 at NOVA IMS, 2nd floor). Additionally, you are asked to send the Word & EXCEL & RScript / Python files by email: jbravo@novaims.unl.pt