Co.Al.A.R. Computational Algebraic Analysis Results

THIS PAGE IS DEVOTED TO SOME RESULTS IN **CLIFFORD ANALYSIS** and related topics

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==> NOETHERIAN OPERATORS [DSS]:

Some experiments performed using different algorithms, includes CPU times

| variables | multiplicity | IDEAL | CPU TIME (CoCoA 4.5 on Toshiba Sat. 2455) | OPERATORS |
|-----------|--------------|--------------------------|--|---------------------------------------|
| | | | - 3.4 from [DSS], following an idea of [MMM] | |
| | | | - (40) from [Ob96], using linear algebra | |
| | | | - 3.8 from [DSS], using forward reduction | |
| | | | - 3.17 from [DSS], using backward reduction | |
| 2 | 4 | (x^2-y ,y^2) | 0.75" | 1 , |
| | | | 0.14" | dx , dx^2+dy , dx^3+dxdy |
| | | | 0.37" | |
| | | | 0.08" | |
| 2 | 8 | (x^4-xy-y, y^2) | 8.31" | 1, |
| | | | 0.90" | dx , dx^2 , |
| | | | 0.28 " | dx^3 , dx^4+dy , |
| | | | 0.15" | dx^5+dx^4+dxdy , |
| | | | 0.13 | dx^6+dx^5+dx^2dy, dx^7+dx^6+dx^3dy |
| 2 | 9 | (x^3-y, y^3) | 2' 9" | 1, |
| | | | 1.53" | dx , dx^2 , |
| | | | 0.34" | dx^3+dy, dx^4+dxdy, |
| | | | 0.22" | dx^5+dx^2dy , $dx^6+dx^3dy+dy^2$, |
| | | | | $dx^7+dx^4dy+dxdy^2$ |
| 3 | 8 | (v\) = v\) = =\(\alpha\) | 12' | $dx^8+dx^5dy+dx^2dy^4$ |
| 3 | O | (x^2-z, y^2-z, z^2) | | 1 , dy , |
| | | | 9.18" | dx , dxdy , |
| | | | 0.99" | dx^2+dy^2+dz , |
| | | | 0.19" | dx^2dy+dy^3+dydz , |

| | | | | dx^3+dxdy^2+dxdz, dx^3dy+dxdy^3+dxdydz |
|---|---|-------------------------|-------------------|--|
| 3 | 4 | (x^2-ty ,y^2) | dim(I)>0 | 1 , |
| | | | dim(I)>0 | dx , tdx^2+dy , |
| | | | 0.64" | tdx^3+dxdy |
| | | | not yet available | |
| 4 | 8 | (x^4-txy-sy, y^2) | dim(I)>0 | 1, |
| | | | dim(I)>0 | dx , dx^2 , |
| | | | 2.61" | dx^3 , sdx^4+dy , |
| | | | not yet available | sdx^5+tdx^4+dxdy, sdx^6+tdx^5+dx^2dy, sdx^7+tdx^6+dx^3dy |
| 5 | 8 | (x^2-tz, y^2-sz, z^2) | dim(I)>0 | 1, |
| | | | dim(I)>0 | dy, dx, |
| | | | 12.73" | dxdy, sdy^2+tdx^2+dz, |
| | | | not yet available | sdy^3+tdx^2dy+dydz, sdxdy^2+tdx^3+dxdz, sdxdy^3+tdx^3dy+dxdydz |

REFERENCES: (click on [XXX] to get the AMS reference #)

[DSS] A. Damiano, I. Sabadini, D. Struppa, Computational Methods for the Construction of a Class of Noetherian Operators, Submitted

[Ob96] U. Oberst, Finite-dimensional systems of partial differential or difference equations. Adv. in Appl. Math. 17 (1996), no. 3, 337--356.

[MMM] Marinari, M. G.; Möller, H. M.; Mora, T. On multiplicities in polynomial system solving. Trans. Amer. Math. Soc. 348 (1996), no. 8, 3283-3321.