## SEM I -

## Lista ex

b) 
$$\Delta = 0 \iff a+b+c=0 \text{ sau } a=b=c$$

Calculati det (A) = V(a,b,c)

3) Fie 
$$A = \begin{pmatrix} 1+a^2 & ba & ca \\ ba & 1+b^2 & cb \end{pmatrix} \in \mathcal{M}_3(\mathbb{R})$$

Calculate  $\det(A^*)$ 

4) Fie 
$$tau = \begin{pmatrix} 2 & -1 & 3m+4 \\ 1 & m & 1 \\ -1 & -1 & 0 \end{pmatrix} \in \mathcal{U}_3(\mathbb{Z})$$

a) Determinati m ai A'∈ M3(Z)

b) It m=0, calculate A-1 Precipati mai multe metode

5 Fix  $A \in \mathcal{U}_2(\mathbb{C})$ Saca  $\exists k \in \mathbb{N}_1 k / 2 \text{ ai } A^k = \mathcal{O}_{2,1} \text{ at } A^k = \mathcal{O}_{2}$ .

(6) Fie f: Mom(R) -> R, f(X) = det X Precipate daca f este inj, resp. surjectiva

- (8) Fie  $A \in \mathcal{U}_n(\mathbb{R})$ a) Daca  $A = O_n$ , at  $J_n - A$ ,  $J_n + A$  sunt inversable b) Daca  $A^3 = O_n$ , at  $J_n - A$ ,  $J_n + A - II - III$
- 9 Fie  $A = (a_{ij})_{ij} = \overline{l_{in}}$ ,  $a_{ij} = \min_{i \neq j} \{i \neq i, j \leq n\}$ Sa se arale ca  $\Delta_n = \det A = 1$
- To Fig A =  $\begin{pmatrix} a & 1 & 2 \\ 1 & 1 & 1 \\ -1 & 1 & 1-a \end{pmatrix} \in \mathcal{M}_3(\mathbb{R})$  tg A = ? Disentie
- (12) Fix  $A \in M_3(\mathbb{R})$ ,  $A^{2023} 2023 A J_3 = 0_3$ a) tg A = ?b)  $tg (2023 A + J_3) = ?$

Ind AAT