

Laborator Proiectare Logică 5

Sîrghe Matei

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Optimizarea funcțiilor logice

Optimizarea-reducerea numărului de operații

Website: lg.ccpr.ro

Exerciții

Exercițiul 1:

$$y : 2^3 \rightarrow 2^1; y = \sum(1, 2, 3, 5, 6) = FCD_y$$

$$y = \Pi(0, 4, 7) = FCC_y$$

$$FCD_y = \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}C + ABC\bar{C}$$

21 operații logice \uparrow

$$FCC_y = (A + B + C)(\bar{A} + B + C)(\bar{A} + \bar{B} + \bar{C})$$

12 operații logice \uparrow

Rezolvare: $FCD_y = \sum(2, 3) = n(2, 3) = A\bar{B} + AB$

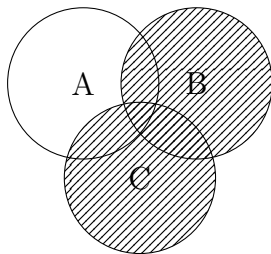
$$FCC_y = \Pi(0, 1) = m(0, 1) = (A + B)(A + \bar{B})$$

$$y = A\bar{B} + AB = A(\bar{B} + B) = A \times 1 = A$$

$$y = (A + B)(A + \bar{B}) = A^2 + A\bar{B} + BA + B\bar{B}$$

$$= A + A\bar{B} + AB + 0 = A(1 + B + \bar{B}) = A$$

A	B	C	y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0



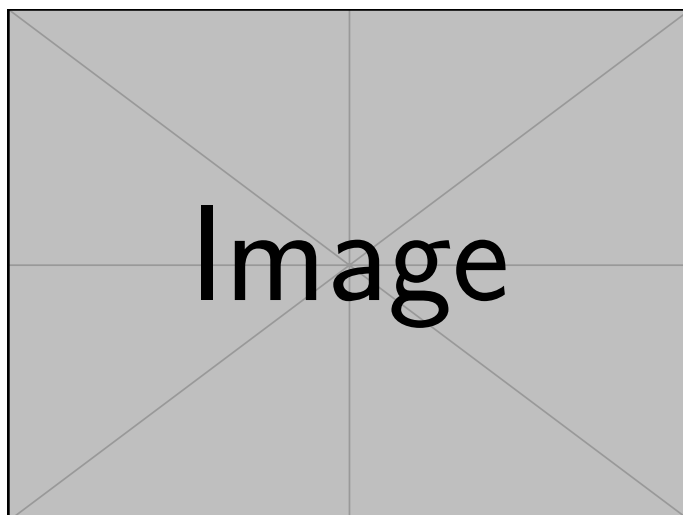
	\bar{A}	\bar{A}	A	A
\bar{C}	0	1	1	0
C	1	1	0	1
	\bar{B}	B	B	\bar{B}

$$\begin{aligned} & \bar{A}(\bar{B}C + B\bar{C}) + A(\bar{B}C + B\bar{C}) + \bar{A}(BC) \\ &= (\bar{A} + A)(\bar{B}C + B\bar{C}) + \bar{A}BC \\ &= \bar{B}C + B\bar{C} + \bar{A}BC \\ &= B \oplus C + \bar{A}BC \end{aligned}$$

Exercițiul 2:

Faceți schema pentru funcția:

$$y = B\bar{C} + \bar{A}B + C\bar{B}$$

**Exercițiul 3:**

Simplificați funcția dată prin tabela de adevăr:

Rezolvare:

$$y = \sum(0, 2, 3, 4, 5, 6, 8, 9, 10, 12)$$

$$= \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D}$$

$$y = \Pi(1, 7, 11, 13, 14, 15)$$

$$= (A + B + C + \bar{D})(A + \bar{B} + \bar{C} + \bar{D})(\bar{A} + B + \bar{C} + \bar{D})$$

$$(\bar{A} + \bar{B} + C + \bar{D})(\bar{A} + \bar{B} + \bar{C} + D)(\bar{A} + \bar{B} + \bar{C} + \bar{D})$$

A	B	C	D	y
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

	\bar{A}	\bar{A}	A	A	
\bar{C}	1	1	1	1	\bar{D}
\bar{C}	0	1	0	1	D
C	1	0	0	0	D
C	1	1	0	1	\bar{D}
	\bar{B}	B	B	\bar{B}	

$$y = \bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}\bar{B}C + \bar{A}\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D}$$