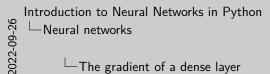
Introduction to Neural Networks in Python Neural networks

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- Biological motivation
- A Human brain contains approximately 86 billion neurons.
- 10¹⁴ to 10¹⁵ synapses connect these neurons.
- Neurons recieve inputs from dentrites.
- and can produce outputs signals along its axon.
- Axons are connect neurons, modelled by weighting inputs wx.
- Neuron inputs can be inhibitive (negative weight) or
- excitory (positive weight).
- If enough inputs exite a neuron it fires.
- The activation function aims to mimic this behaviour.
- Even though neural networks started out as biologically motivated,
- engineering efforts have since diverged from biology.



where \odot is the element-wise product. δ denotes the cost function gradient for the value following it [Gre+16]. Modern libraries will take care of these computations for you! You can choose to verify these equations yourself by completing the optional deep learning project

The chain rule tells us the gradients for the dense layer [Nie15]

The gradient of a dense layer

☐ The gradient of a dense layer

On the board, derive: Recall the chain rule $(g(h(x)))' = g'(h(x)) \cdot h'(x)$. For the activation function, we have,

$$\bar{\mathbf{h}} = f(\bar{\mathbf{h}}) \tag{7}$$

$$\Rightarrow \delta \bar{\mathbf{h}} = f'(\bar{\mathbf{h}}) \odot \triangle \tag{8}$$

For the weight matrix,

$$\bar{\mathbf{h}} = \mathbf{W}\mathbf{x} + \mathbf{b}$$
 (9)

$$\Rightarrow \delta \mathbf{W} = \delta \bar{\mathbf{h}} \mathbf{x}^T = [f'(\bar{\mathbf{h}}) \odot \triangle]^T \mathbf{x}$$
 (10)

For the bias.

$$\bar{\mathbf{h}} = \mathbf{W}\mathbf{x} + \mathbf{b} \tag{11}$$

$$\Rightarrow \delta \mathbf{b} = 1 \odot \delta \bar{\mathbf{h}} = [f'(\bar{\mathbf{h}}) \odot \triangle]$$
 (12)

Following [Nie15], substitute $\sigma(\mathbf{o})$ into eq 12.

If a sigmoidal activation function produced ${\bf e}$ the gradients can be computed using [NealS, Bla06] $\frac{\partial C_{\omega}}{\partial {\bf h}} = \sigma({\bf e}) - {\bf y} = \triangle_{\omega} \eqno(19)$

Gradients and cross-entropy