



Machine learning for glacier modelling

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Overview

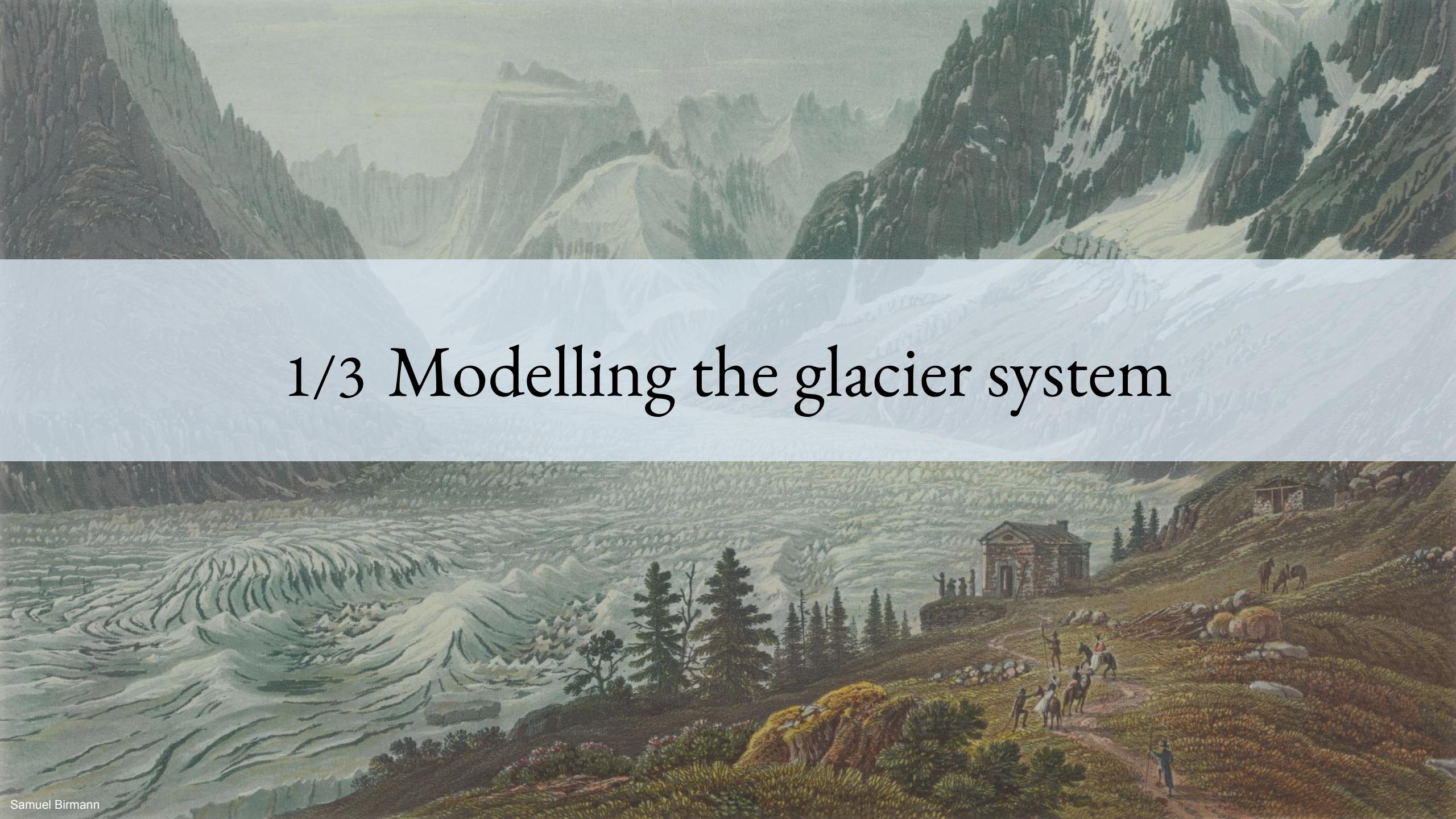
1. Modelling the glacier system

- What is a glacier and how do we model them?

2. Machine learning to model glacier physical processes

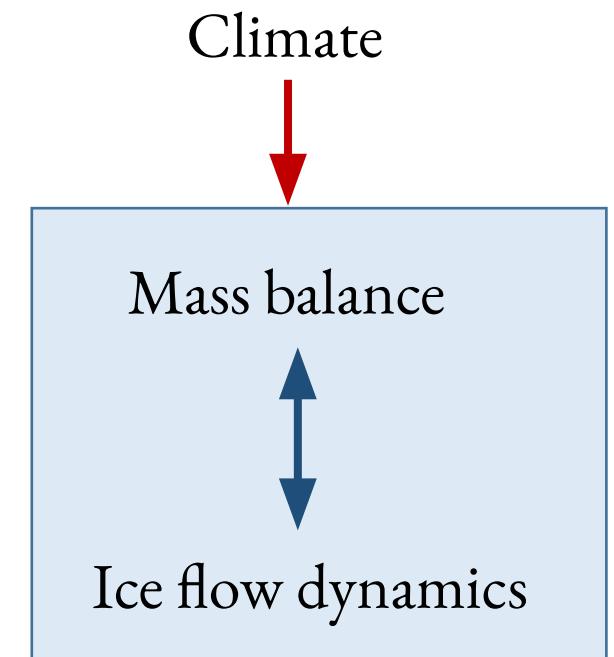
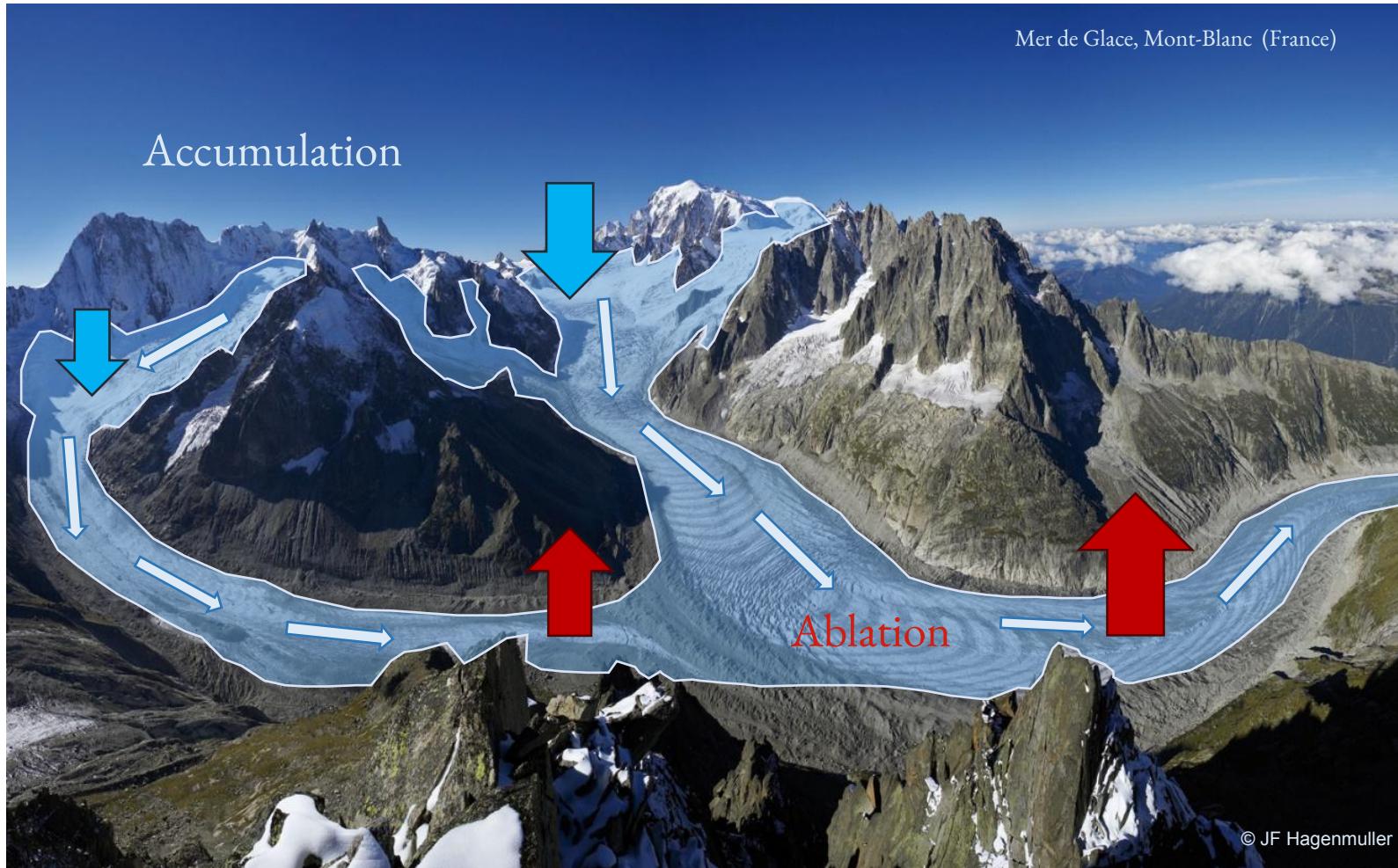
- What is machine learning for regression?
- How can it be useful in glacier modelling?
- How can we be sure that we are actually respecting physics?
- What are the main pitfalls and limitations when training ML models?

3. Project description



1/3 Modelling the glacier system

The glacier system



Glacier evolution models

Mass balance component

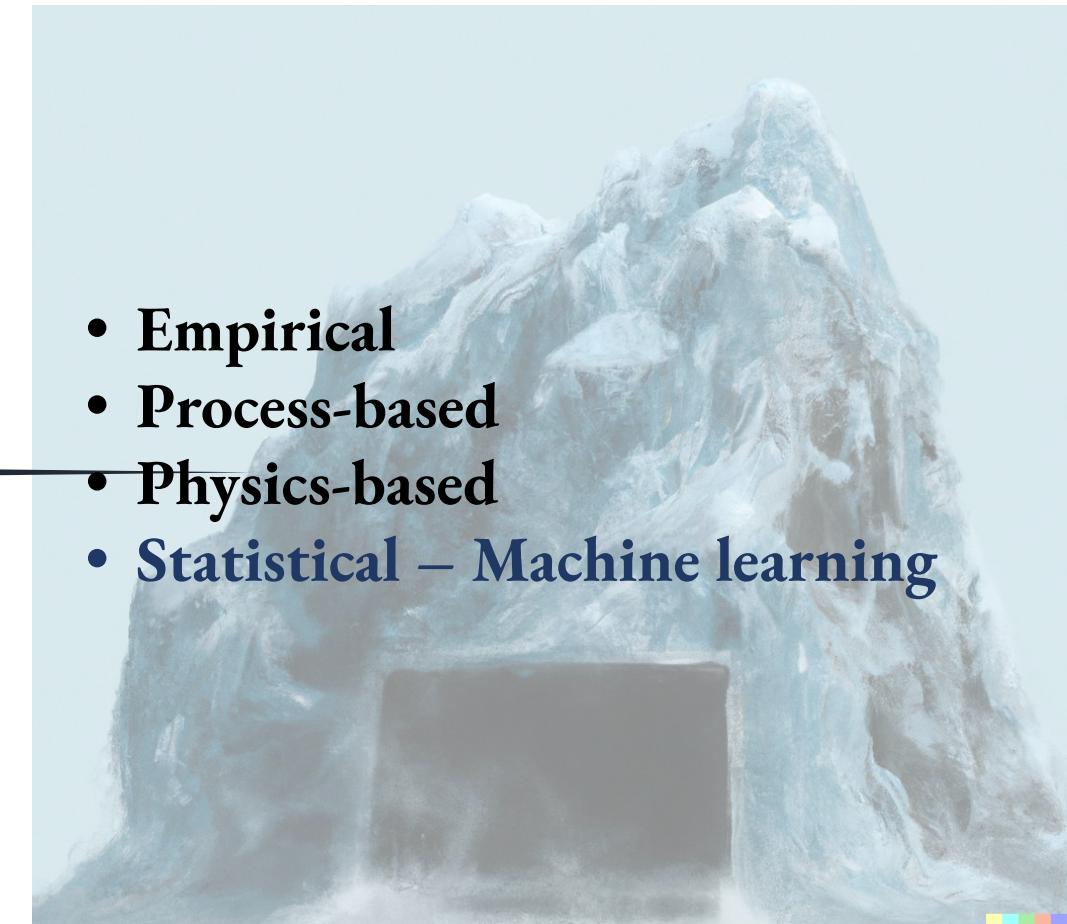
- Ablation
- Accumulation
- Refreezing
- Debris cover
- Calving
- ...

Ice dynamics component

- Creep
- Basal sliding
- ...

Analytical form

Differential
equations



- Empirical
- Process-based
- Physics-based
- Statistical – Machine learning

Local vs Global glacier modelling



Local modelling (1-10 glaciers)

- More complex models can be used (e.g. Full Stokes)
- Model parameters can be fine tuned manually

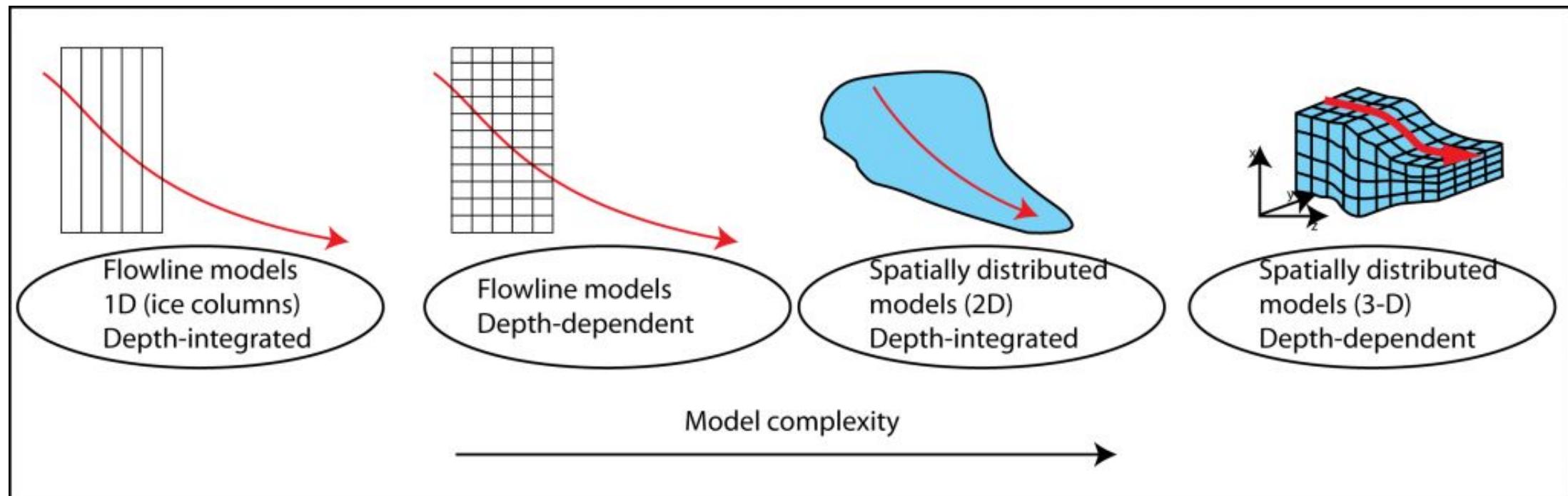


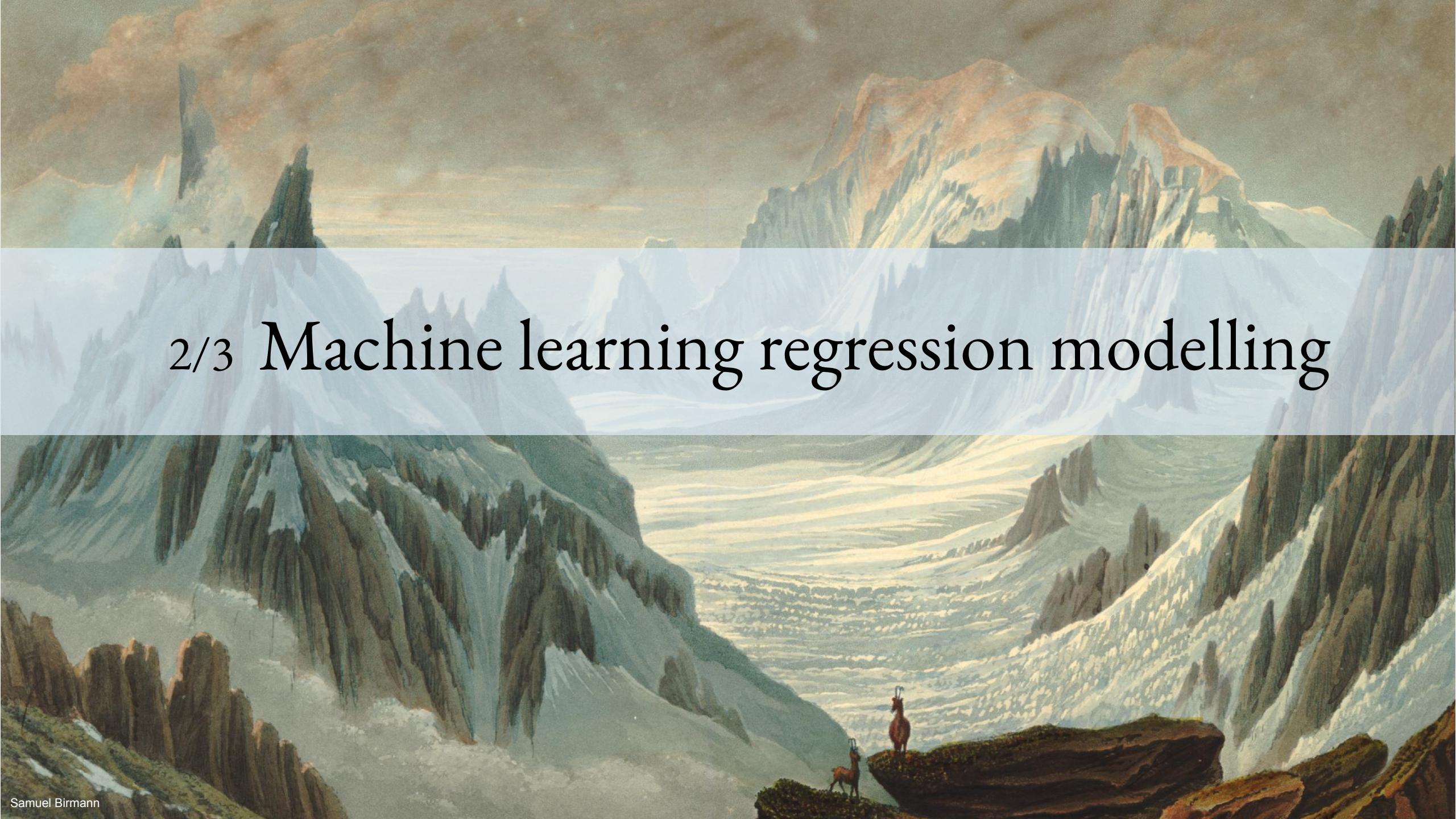
Regional to Global modelling (100s-200,000 glaciers, ice sheets)

- Computational cost needs to be taken into account by using simplifications (e.g. Δh , SIA, flowline...)
- Model parameters need automation based on optimization

Model complexity vs capacity (flexibility)

Local vs Global glacier modelling



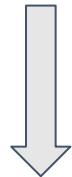


2/3 Machine learning regression modelling

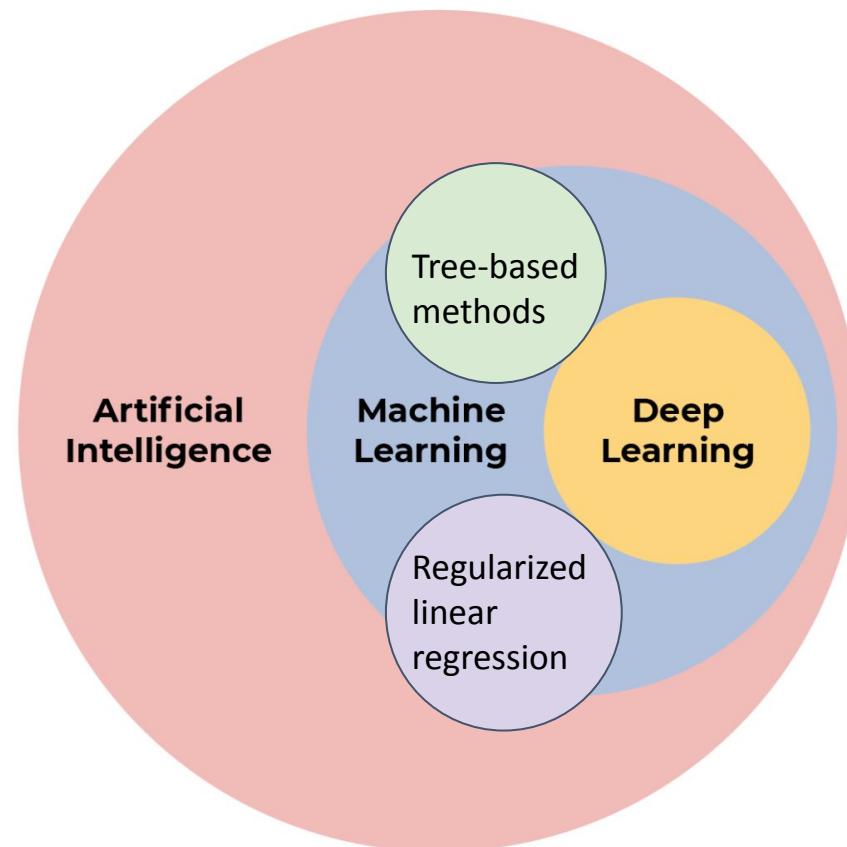
Machine learning models

Statistical
data-driven models

Regression



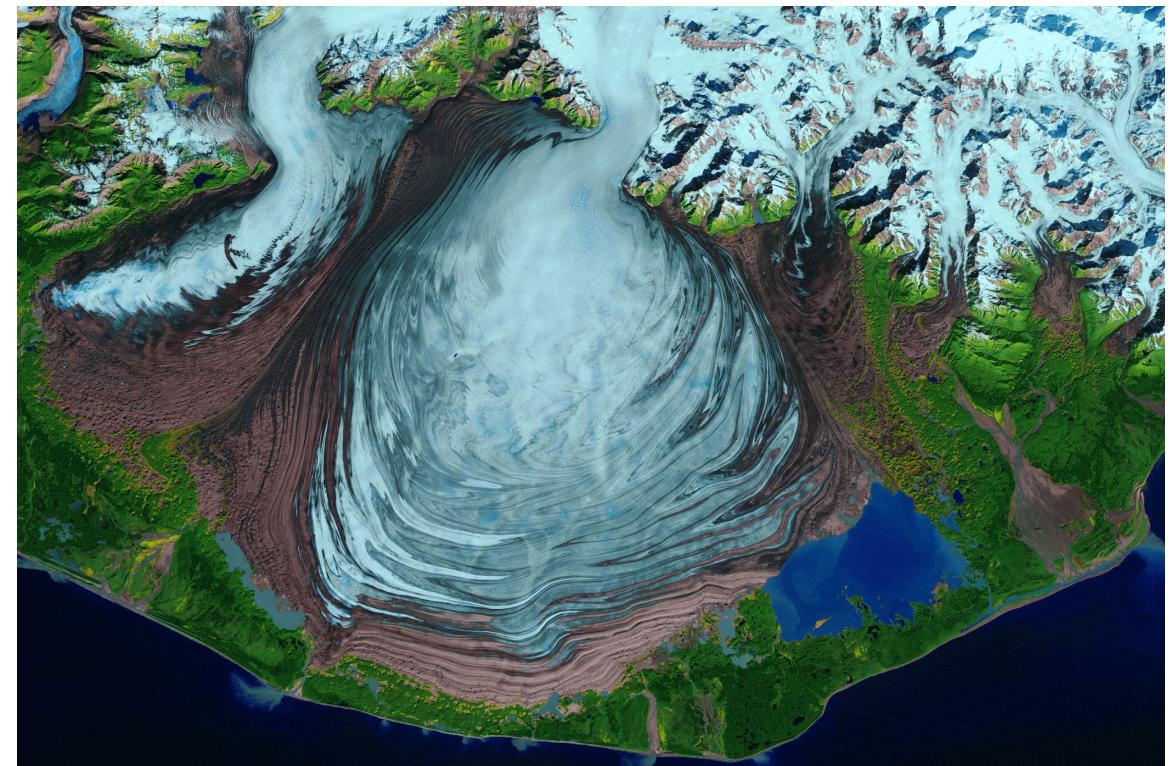
Approximating functions



A new era of remote sensing observations



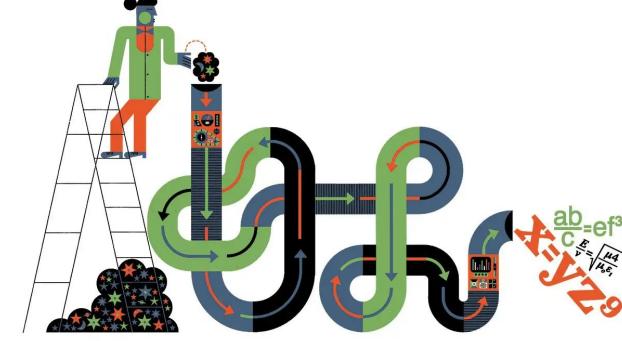
Baltoro glacier, Karakoram



Malaspina glacier, Alaska

How can ML be useful in glacier modelling?

Machine learning modelling can help in many directions:

- **Speed:** Statistical emulators 
- **Prediction:** Data-driven machine learning 
- **Discovering hidden physics:** Universal Differential Equations, Physics-Informed Neural Networks 

Raymond Biesinger



How can ML be useful in glacier modelling?

Let's see a few examples...

Speeding up scientific models with emulators

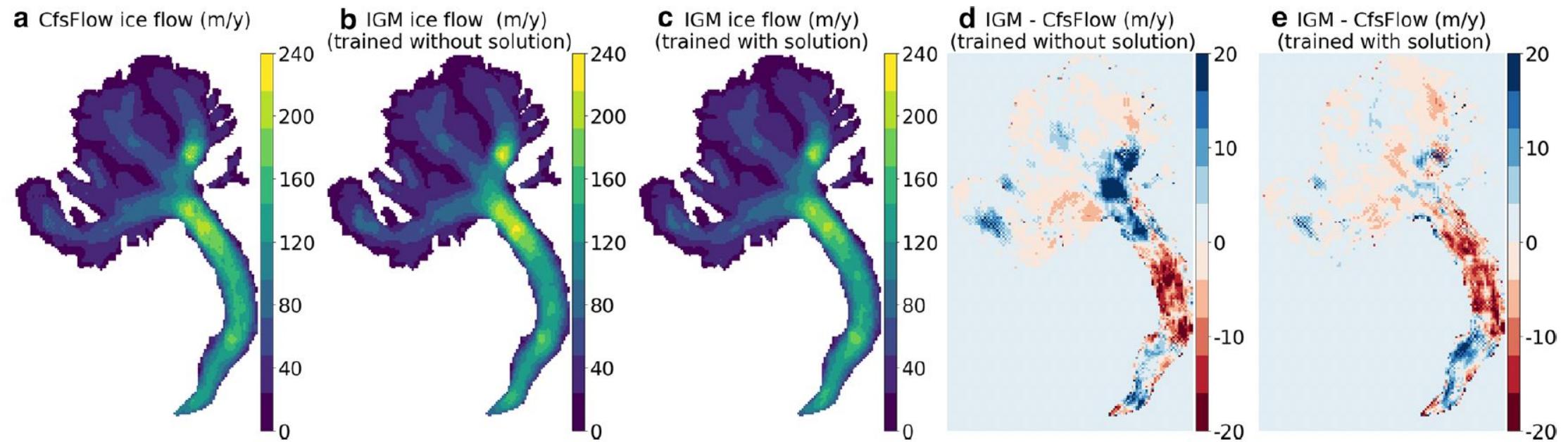
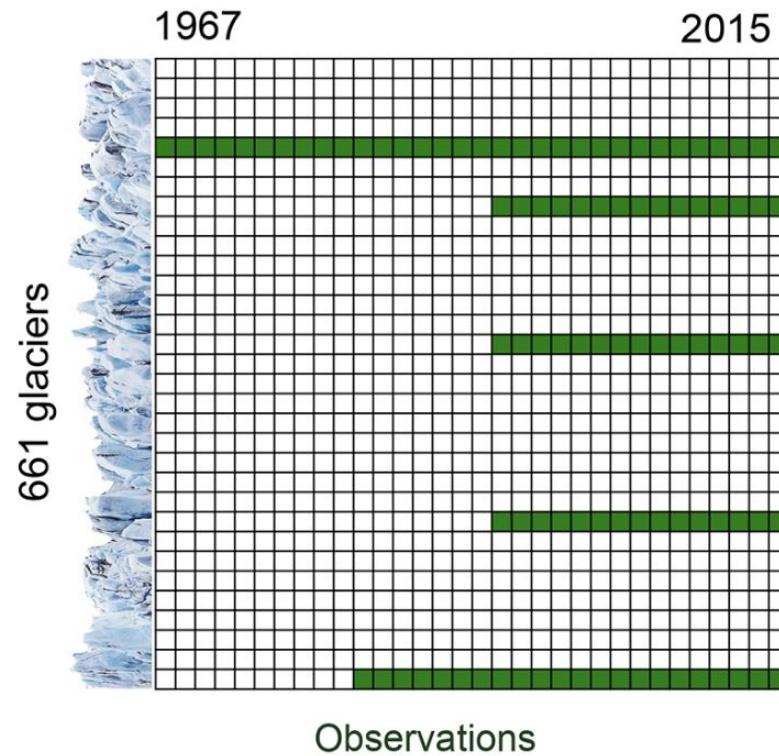


Fig. 10. Vertically-averaged ice flow magnitude of the Aletsch glacier at its maximum state: CfsFlow reference solution (a), the IGM solution trained without (b) and with (c) the solution, and the difference between IGM and CfsFlow solutions (d and e).

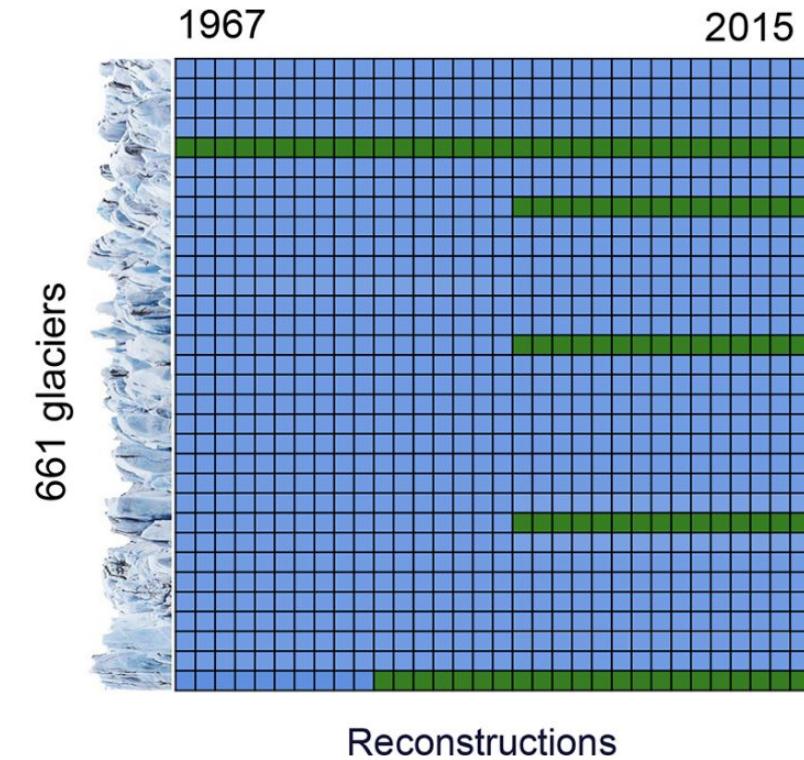
Fig. 3. The function we aim to emulate by learning from hybrid SIA + SSA or Stokes realizations maps geometrical fields (thickness and surface slopes) and basal sliding parametrization to ice flow fields.

Jouvet et al. (2021)

Making predictions with ML models

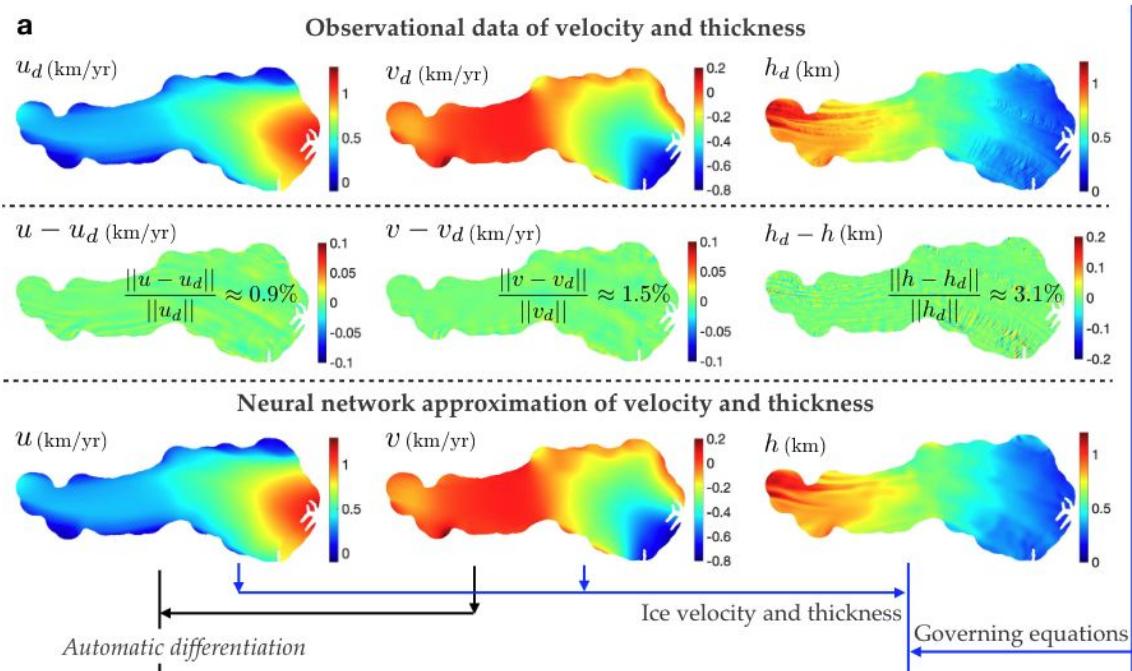


Annual glacier-wide
surface mass balance

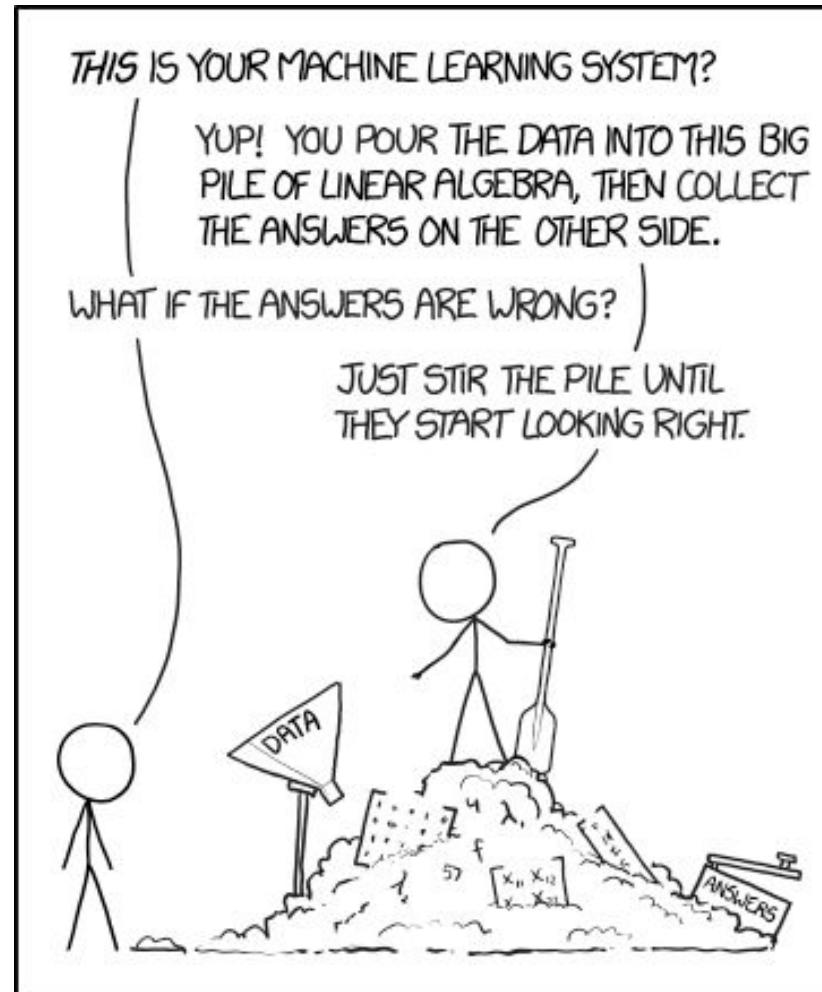


Bolibar et al. (2020b)

Discovering hidden physics



How do we actually train ML models?



Regression machine learning pipelines



Split X and Y into train, validation and test datasets,
where X is the feature matrix and Y is the target variable



Train **parameters** of model M to learn a function f , such as $Y = f(X) + \epsilon$



Tune **hyperparameters** which determine model M using the train
and validation datasets



Assess final model performance on independent test dataset

Regression for physical processes

Modelling physical processes implies a series of challenges:

1. How can we be sure that we are respecting basic physical properties?
Feature selection, Physical constraints
2. How can we be sure that we are modelling the actual physical process?
Testing and validation
3. What are the limitations in the model design and its predictions?
Training strategies, Spatiotemporal resolution

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1. Respecting physics

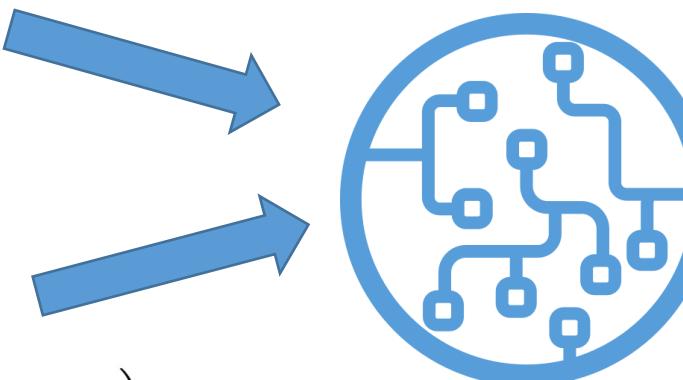
- Good domain knowledge in the physics involved. Make sure the chosen features are relevant to the process.

Literature review



Review physical equations

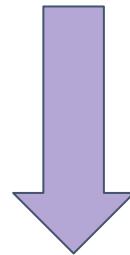
$$\frac{\partial H}{\partial t} = \dot{b} + \nabla \cdot \left(\left(C + \frac{2A}{n+2} H \right) (\rho g)^n H^{n+1} \|\nabla S\|^{n-1} \nabla S \right)$$



Model design

1. Respecting physics

- Add physical constraints in the model design (e.g. PINNs, UDEs)
- Train model on physical model outputs (i.e. an **emulator**)



Want to learn more?

Attend bonus lecture on Physics-informed Machine Learning!

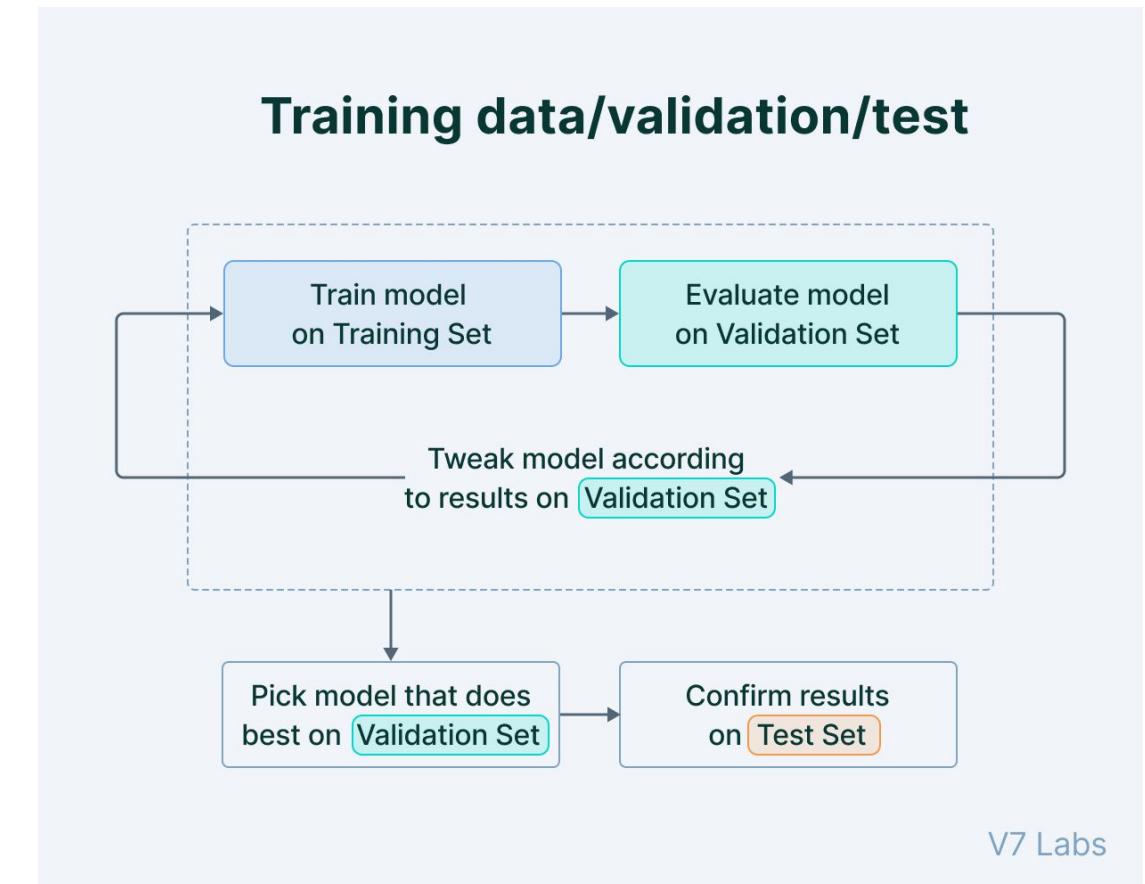
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2. Trustworthy models

- A robust validation and test pipeline is the best way to make sure we are learning useful information.
- Respect spatiotemporal structures in dataset
- Using an independent **well-chosen** test dataset will help identify if the model has any pathologies.



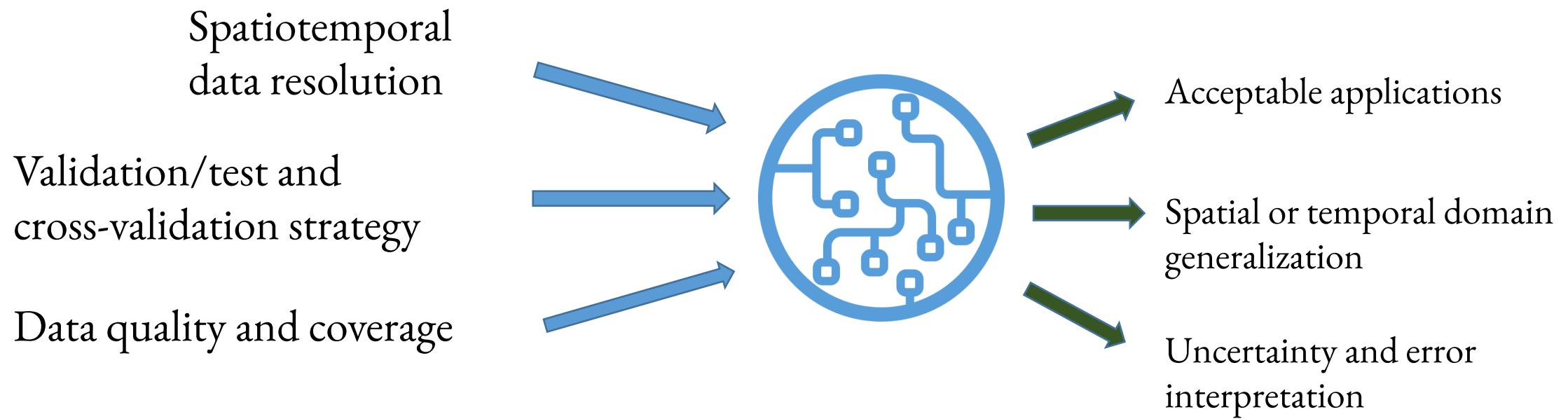
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3. Being mindful about model limitations

- It is crucial to understand how the model has been designed and what its strengths and weaknesses are





3/3 Project description



Machine learning for glacier modelling

Main project:

Explore different regression methods and learn the fundamentals of a machine learning pipeline, applied to glacier mass balance modelling.

Bonus projects:

1. Predict distributed (2D) geodetic mass balance rates
2. Infer distributed (2D) glacier ice thickness



Machine learning for mass balance modelling

Follow the tutorials from the following Jupyter notebooks:

https://github.com/Machine-Learning-in-Glaciology-Workshop/Project_MB_Regression

 1_Preprocessing.ipynb	grammar check	5 days ago
 2_Data_exploration.ipynb	grammar check	5 days ago
 3_Training.ipynb	grammar check	5 days ago
 4_Validation.ipynb	grammar check	5 days ago
 5_Distributed_preprocessin...	grammar check	5 days ago
 6_Bonus_Projects.ipynb	grammar check	5 days ago



A panoramic landscape featuring a range of majestic, snow-capped mountains under a clear, bright blue sky. The mountains in the background have rugged, rocky peaks partially hidden by white snow. In the foreground, there is a vast expanse of white, textured snow and ice, likely a glacier or large snowfield, with some darker, shadowed areas where the ice meets the ground.

Thank you for your attention
