Social network Graph Link Prediction - Facebook Challenge

Problem statement:

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

Data Overview

Taken data from facebook's recruting challenge on kaggle https://www.kaggle.com/c/FacebookRecruiting data contains two columns source and destination eac edge in graph

```
Data columns (total 2 columns):source_node int64destination node int64
```

Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of
 followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and
 trained ml model based on these features to predict link.
- Some reference papers and videos :
 - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
 - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf
 - https://kaggle2.blob.core.windows.net/forum-message-attachments/2594/supervised_link_prediction.pdf
 - https://www.youtube.com/watch?v=2M77Hgy17cg

Business objectives and constraints:

- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

Performance metric for supervised learning:

- Both precision and recall is important so F1 score is good choice
- · Confusion matrix

In [2]:

```
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import csv
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xgboost as xgb
```

```
import warnings
import networkx as nx
import pdb
import pickle
```

In [4]:

```
#reading graph
if not os.path.isfile('train_woheader.csv'):
    traincsv = pd.read_csv('train.csv')
    print(traincsv[traincsv.isna().any(1)])
    print(traincsv.info())
    print("Number of diplicate entries: ",sum(traincsv.duplicated()))
    traincsv.to_csv('train_woheader.csv',header=False,index=False)
    print("saved the graph into file")
else:
    g=nx.read_edgelist('train_woheader.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=int)
    print(nx.info(g))
```

Name:

Type: DiGraph

Number of nodes: 1862220 Number of edges: 9437519 Average in degree: 5.0679 Average out degree: 5.0679

In [2]:

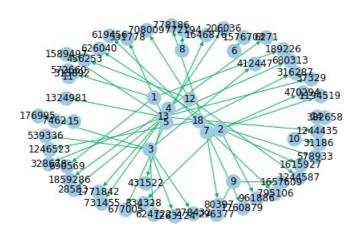
```
if not os.path.isfile('train_woheader_sample.csv'):
    pd.read_csv('train.csv', nrows=50).to_csv('train_woheader_sample.csv',header=False,index=False)

subgraph=nx.read_edgelist('train_woheader_sample.csv',delimiter=',',create_using=nx.DiGraph(),node
type=int)
# https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with-networkx-and-matplotlib

pos=nx.spring_layout(subgraph)
nx.draw(subgraph,pos,node_color='#AOCBE2',edge_color='#00bb5e',width=1,edge_cmap=plt.cm.Blues,with_labels=True)
plt.savefig("graph_sample.pdf")
print(nx.info(subgraph))
```

Name:

Type: DiGraph
Number of nodes: 66
Number of edges: 50
Average in degree: 0.7576
Average out degree: 0.7576



1. Exploratory Data Analysis

```
In [5]:
```

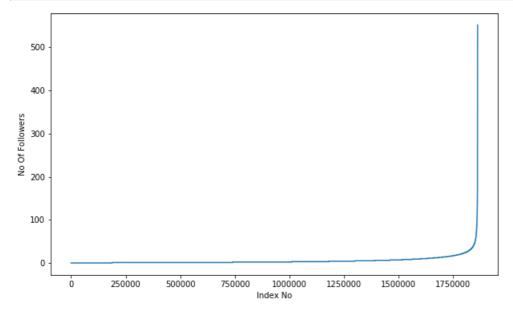
```
# No of Unique persons
print("The number of unique persons",len(g.nodes()))
```

The number of unique persons 1862220

1.1 No of followers for each person

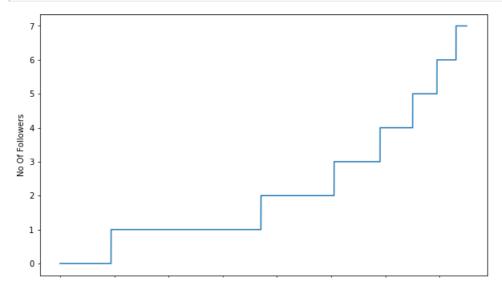
In [6]:

```
indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(indegree_dist)
plt.xlabel('Index No')
plt.ylabel('No Of Followers')
plt.show()
```



In [7]:

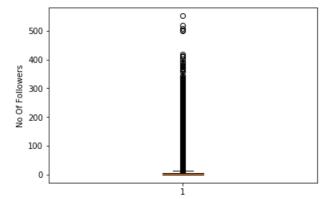
```
indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(indegree_dist[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of Followers')
plt.show()
```



0 200000 400000 600000 800000 1000000 1200000 1400000 Index No

```
In [8]:
```

```
plt.boxplot(indegree_dist)
plt.ylabel('No Of Followers')
plt.show()
```



In [9]:

```
### 90-100 percentile
for i in range(0,11):
    print(90+i, 'percentile value is',np.percentile(indegree_dist,90+i))

90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
```

96 percentile value is 21.0 97 percentile value is 24.0 98 percentile value is 29.0 99 percentile value is 40.0 100 percentile value is 552.0

95 percentile value is 19.0

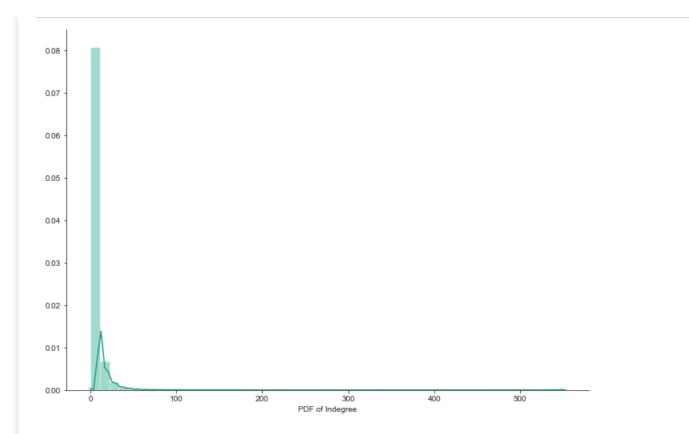
In [10]:

```
### 99-100 percentile
for i in range(10,110,10):
    print(99+(i/100),'percentile value is',np.percentile(indegree_dist,99+(i/100)))
```

```
99.1 percentile value is 42.0
99.2 percentile value is 44.0
99.3 percentile value is 47.0
99.4 percentile value is 50.0
99.5 percentile value is 55.0
99.6 percentile value is 61.0
99.7 percentile value is 70.0
99.8 percentile value is 84.0
99.9 percentile value is 112.0
100.0 percentile value is 552.0
```

In [11]:

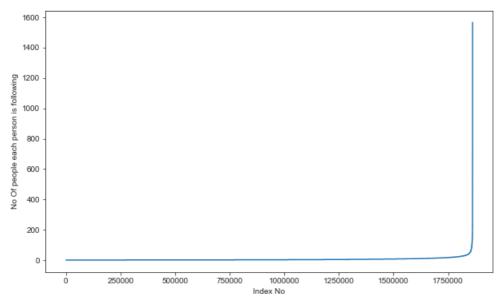
```
%matplotlib inline
sns.set_style('ticks')
fig, ax = plt.subplots()
fig.set_size_inches(11.7, 8.27)
sns.distplot(indegree_dist, color='#16A085')
plt.xlabel('PDF of Indegree')
sns.despine()
#plt.show()
```



1.2 No of people each person is following

In [12]:

```
outdegree_dist = list(dict(g.out_degree()).values())
outdegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(outdegree_dist)
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following')
plt.show()
```



In [13]:

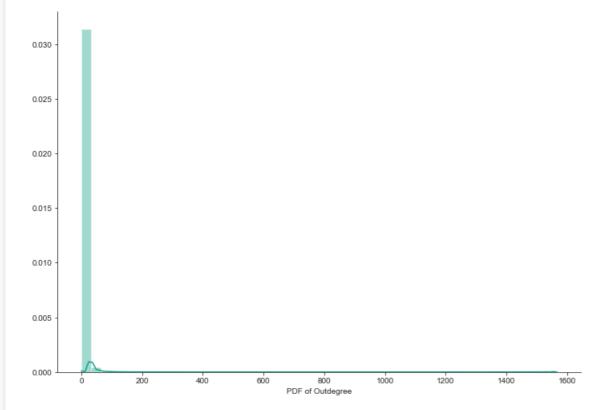
```
indegree_dist = list(dict(g.in_degree()).values())
indegree_dist.sort()
plt.figure(figsize=(10,6))
plt.plot(outdegree_dist[0:1500000])
plt.xlabel('Index No')
```

```
bir.Arabet(.Mo or beobie each betson is rottomind.)
plt.show()
  6
people each person is following
  5
  4
JJO ON
  0
                        400000
                                 600000
                                                   1000000
                                                             1200000
                                        Index No
In [14]:
plt.boxplot(indegree_dist)
plt.ylabel('No Of people each person is following')
h person is following
300
                            8
 each
  200
Of people
   100
    0
In [15]:
### 90-100 percentile
for i in range (0,11):
    print(90+i, 'percentile value is', np.percentile(outdegree_dist, 90+i))
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 1566.0
In [16]:
### 99-100 percentile
for i in range(10,110,10):
    print(99+(i/100),'percentile value is',np.percentile(outdegree_dist,99+(i/100)))
```

```
99.1 percentile value is 42.0
99.2 percentile value is 45.0
99.3 percentile value is 48.0
99.4 percentile value is 52.0
99.5 percentile value is 56.0
99.6 percentile value is 63.0
99.7 percentile value is 73.0
99.8 percentile value is 90.0
99.9 percentile value is 123.0
100.0 percentile value is 1566.0
```

In [17]:

```
sns.set_style('ticks')
fig, ax = plt.subplots()
fig.set_size_inches(11.7, 8.27)
sns.distplot(outdegree_dist, color='#16A085')
plt.xlabel('PDF of Outdegree')
sns.despine()
```



In [18]:

No of persons those are not following anyone are 274512 and \$ is 14.741115442858524

In [19]:

No of persons having zero followers are 188043 and % is 10.097786512871734

In [20]:

```
count=0
for i in g.nodes():
   if len(list(g.predecessors(i)))==0:
      if len(list(g.successors(i)))==0:
```

```
count+=1
print('No of persons those are not not following anyone and also not having any followers are',cou
nt)
```

No of persons those are not not following anyone and also not having any followers are 0

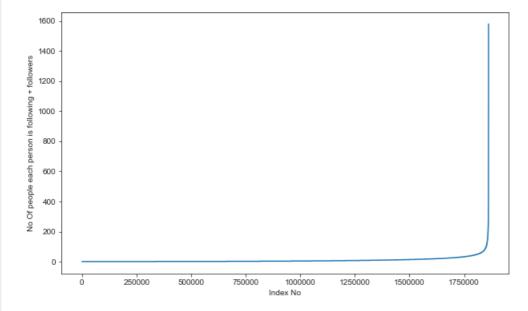
1.3 both followers + following

```
In [21]:
```

```
from collections import Counter
dict_in = dict(g.in_degree())
dict_out = dict(g.out_degree())
d = Counter(dict_in) + Counter(dict_out)
in_out_degree = np.array(list(d.values()))
```

In [22]:

```
in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort)
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



In [23]:

```
in_out_degree_sort = sorted(in_out_degree)
plt.figure(figsize=(10,6))
plt.plot(in_out_degree_sort[0:1500000])
plt.xlabel('Index No')
plt.ylabel('No Of people each person is following + followers')
plt.show()
```



```
No Of peop
   2
              200000
                       400000
                               600000
                                                1000000
                                                        1200000
                                                                 1400000
                                       800000
                                     Index No
In [24]:
### 90-100 percentile
for i in range (0,11):
    print(90+i,'percentile value is',np.percentile(in_out_degree_sort,90+i))
90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
In [25]:
### 99-100 percentile
for i in range(10,110,10):
    print(99+(i/100),'percentile value is',np.percentile(in_out_degree_sort,99+(i/100)))
99.1 percentile value is 83.0
99.2 percentile value is 87.0
99.3 percentile value is 93.0
99.4 percentile value is 99.0
99.5 percentile value is 108.0
99.6 percentile value is 120.0
99.7 percentile value is 138.0
99.8 percentile value is 168.0
99.9 percentile value is 221.0
100.0 percentile value is 1579.0
In [26]:
print('Min of no of followers + following is',in_out_degree.min())
print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of followers +
following')
Min of no of followers + following is 1
334291 persons having minimum no of followers + following
In [27]:
print('Max of no of followers + following is',in out degree.max())
print(np.sum(in out degree==in out degree.max()), ' persons having maximum no of followers +
following')
Max of no of followers + following is 1579
1 persons having maximum no of followers + following
In [28]:
```

No of persons having followers + following less than 10 are 1320326

print('No of persons having followers + following less than 10 are',np.sum(in out degree<10))

```
In [29]:

print('No of weakly connected components',len(list(nx.weakly_connected_components(g))))
count=0
for i in list(nx.weakly_connected_components(g)):
    if len(i)==2:
        count+=1
print('weakly connected components wit 2 nodes',count)
No of weakly connected components 45558
weakly connected components wit 2 nodes 32195
```

2. Posing a problem as classification problem

2.1 Generating some edges which are not present in graph for supervised learning

Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
In [6]:
%%time
###generating bad edges from given graph
import random
if not os.path.isfile('missing edges final.p'):
    #getting all set of edges
    r = csv.reader(open('train woheader.csv','r'))
    edges = dict()
    for edge in r:
        edges[(edge[0], edge[1])] = 1
    missing edges = set([])
    while (len(missing_edges)<9437519):</pre>
        a=random.randint(1, 1862220)
        b=random.randint(1, 1862220)
        tmp = edges.get((a,b),-1)
        if tmp == -1 and a!=b:
            try:
                if nx.shortest path length(g,source=a,target=b) > 2:
                    missing_edges.add((a,b))
                else:
                    continue
            except:
                    missing edges.add((a,b))
        else:
            continue
    pickle.dump(missing edges,open('missing edges final.p','wb'))
else:
    missing edges = pickle.load(open('missing edges final.p','rb'))
Wall time: 2.17 s
missing edges = pickle.load(open('missing edges final.p','rb'))
len (missing edges)
Out[10]:
```

2.2 Training and Test data split:

9437519

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

from sklearn.model selection import train test split

```
if (not os.path.isfile('train_pos_after_eda.csv')) and (not os.path.isfile('test_pos_after eda.csv')
    #reading total data df
    df_pos = pd.read csv('train.csv')
    df neg = pd.DataFrame(list(missing edges), columns=['source node', 'destination node'])
    print("Number of nodes in the graph with edges", df pos.shape[0])
    print("Number of nodes in the graph without edges", df neg.shape[0])
    #Trian test split
    #Spiltted data into 80-20
    {\it\#positive~links~and~negative~links~seperatly~because~we~need~positive~training~data~only~for~c}
reating graph
    #and for feature generation
    X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,np.ones(len(df_pos)
),test_size=0.2, random_state=9)
    X train neg, X test neg, y train neg, y test neg = train test split(df neg,np.zeros(len(df neg
)),test size=0.2, random state=9)
    print('='*60)
    print ("Number of nodes in the train data graph with edges", X train pos.shape[0], "=", y train po
s.shape[0])
   print("Number of nodes in the train data graph without edges", X train neg.shape[0], "=", y trai
n neg.shape[0])
   print('='*60)
    print("Number of nodes in the test data graph with edges", X test pos.shape[0], "=", y test pos.s
hape[0])
    print ("Number of nodes in the test data graph without edges",
X_test_neg.shape[0], "=", y_test_neg.shape[0])
    #removing header and saving
    X train pos.to csv('train pos after eda.csv',header=False, index=False)
    X test pos.to csv('test pos after eda.csv',header=False, index=False)
    X_train_neg.to_csv('train_neg_after_eda.csv',header=False, index=False)
    X test neg.to csv('test neg after eda.csv', header=False, index=False)
else:
    #Graph from Traing data only
    print('deleting .....')
    del missing_edges
4
Number of nodes in the graph with edges 9437519
Number of nodes in the graph without edges 9437519
Number of nodes in the train data graph with edges 7550015 = 7550015
Number of nodes in the train data graph without edges 7550015 = 7550015
Number of nodes in the test data graph with edges 1887504 = 1887504
Number of nodes in the test data graph without edges 1887504 = 1887504
In [12]:
if (os.path.isfile('train pos after eda.csv')) and (os.path.isfile('test pos after eda.csv')):
train graph=nx.read edgelist('train pos after eda.csv',delimiter=',',create using=nx.DiGraph(),nod
etvpe=int)
test graph=nx.read edgelist('test pos after eda.csv',delimiter=',',create using=nx.DiGraph(),nodety
pe=int)
    print(nx.info(train graph))
    print(nx.info(test_graph))
    \# finding the unique nodes in the both train and test graphs
    train_nodes_pos = set(train_graph.nodes())
    test nodes pos = set(test graph.nodes())
    trY_teY = len(train_nodes_pos.intersection(test_nodes_pos))
    trY teN = len(train_nodes_pos - test_nodes_pos)
    teY trN = len(test nodes pos - train nodes pos)
    print('no of people common in train and test -- ',trY teY)
```

print('no of people present in train but not present in test -- ',trY teN)

```
print('no of people present in test but not present in train -- ',teY trN)
   print(' % of people not there in Train but exist in Test in total Test data are {} %'.format(te
Y trN/len(test nodes pos)*100))
Name:
Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree: 4.2399
Average out degree:
Type: DiGraph
Number of nodes: 1144623
Number of edges: 1887504
Average in degree: 1.6490
Average out degree:
                    1.6490
no of people common in train and test -- 1063125
no of people present in train but not present in test -- 717597
no of people present in test but not present in train -- 81498
\% of people not there in Train but exist in Test in total Test data are 7.1200735962845405 \%
In [13]:
#final train and test data sets
if (not os.path.isfile('train_after_eda.csv')) and \
(not os.path.isfile('test after eda.csv')) and \
(not os.path.isfile('train y.csv')) and \
(not os.path.isfile('test y.csv')) and \
(os.path.isfile('train_pos_after_eda.csv')) and \
(os.path.isfile('test_pos_after_eda.csv')) and \
(os.path.isfile('train_neg_after_eda.csv')) and \
(os.path.isfile('test_neg_after_eda.csv')):
    X train pos = pd.read csv('train pos after eda.csv', names=['source node', 'destination node'])
    X test pos = pd.read csv('test pos after eda.csv', names=['source node', 'destination node'])
    X_train_neg = pd.read_csv('train_neg_after_eda.csv', names=['source_node', 'destination_node'])
    X test neg = pd.read csv('test neg after eda.csv', names=['source node', 'destination node'])
    print('='*60)
    print("Number of nodes in the train data graph with edges", X train pos.shape[0])
    print("Number of nodes in the train data graph without edges", X_train_neg.shape[0])
    print('='*60)
    print("Number of nodes in the test data graph with edges", X test pos.shape[0])
    print("Number of nodes in the test data graph without edges", X_test_neg.shape[0])
    X train = X train pos.append(X train neg,ignore index=True)
    y_train = np.concatenate((y_train_pos,y_train_neg))
    X test = X test pos.append(X test neg,ignore index=True)
    y_test = np.concatenate((y_test_pos,y_test_neg))
    X train.to csv('train after eda.csv', header=False, index=False)
    X_test.to_csv('test_after_eda.csv',header=False,index=False)
    pd.DataFrame(y_train.astype(int)).to_csv('train_y.csv',header=False,index=False)
    pd.DataFrame(y test.astype(int)).to csv('test y.csv',header=False,index=False)
4
______
Number of nodes in the train data graph with edges 7550015
Number of nodes in the train data graph without edges 7550015
_____
Number of nodes in the test data graph with edges 1887504
Number of nodes in the test data graph without edges 1887504
```

In [14]:

```
print("Data points in train data",X_train.shape)
print("Data points in test data",X_test.shape)
print("Shape of traget variable in train",y_train.shape)
print("Shape of traget variable in test", y_test.shape)
```

Data points in train data (15100030, 2)
Data points in test data (3775008, 2)
Shape of traget variable in train (15100030,)

```
Shape of traget variable in test (3775008,)
```

```
In [1]:
```

```
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xgboost as xgb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore, DataFrame
from pandas import read hdf
from scipy.sparse.linalg import svds, eigs
import gc
from tqdm import tqdm
```

1. Reading Data

```
In [2]:
```

```
train_graph=nx.read_edgelist('train_pos_after_eda.csv',delimiter=',',create_using=nx.DiGraph(),nod
etype=int)
print(nx.info(train_graph))
Name:
```

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

```
In [3]:
```

```
SIM - (TEM (SEC (CLAIM STAPM.SUCCESSOLS (A)).IMCELSECTION (SEC (CLAIM STAPM.SUCCESSOLS (N))))))
(len(set(train_graph.successors(a)).union(set(train_graph.successors(b)))))
    except:
        return 0
    return sim
In [4]:
#one test case
print(jaccard for followees(273084,1505602))
0.0
In [5]:
#node 1635354 not in graph
print(jaccard for followees(273084,1505602))
0.0
In [6]:
#for followers
def jaccard for followers(a,b):
        if len(set(train graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
        sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b))))
)/\
                                  (len(set(train graph.predecessors(a)).union(set(train graph.predec
ssors(b)))))
        return sim
    except:
        return 0
In [7]:
print(jaccard for followers(273084,470294))
0
In [8]:
#node 1635354 not in graph
print(jaccard for followees(669354,1635354))
0
```

2.2 Cosine distance

```
In [9]:
```

```
In [10]:
print(cosine_for_followees(273084,1505602))
0.0
In [11]:
print(cosine_for_followees(273084,1635354))
0
In [12]:
def cosine for followers(a,b):
    try:
        if len(set(train graph.predecessors(a))) == 0 | len(set(train graph.predecessors(b))) == 0
            return 0
        sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b))))
) / \
                                      (math.sqrt(len(set(train graph.predecessors(a)))) * (len(set(tra
n graph.predecessors(b)))))
        return sim
    except:
        return 0
4
In [13]:
print(cosine for followers(2,470294))
0.02886751345948129
In [14]:
print(cosine for followers(669354,1635354))
0
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-

1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

```
In [15]:
```

```
if not os.path.isfile('page rank.p'):
```

```
pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr,open('page_rank.p','wb'))
else:
    pr = pickle.load(open('page_rank.p','rb'))

In [16]:

print('min',pr[min(pr, key=pr.get)])
    print('max',pr[max(pr, key=pr.get)])
    print('mean',float(sum(pr.values())) / len(pr))

min 1.6556497245737814e-07
    max 2.7098251341935827e-05
    mean 5.615699699389075e-07

In [17]:

#for imputing to nodes which are not there in Train data
mean_pr = float(sum(pr.values())) / len(pr)
    print(mean_pr)
```

5.615699699389075e-07

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [18]:
```

```
#if has direct edge then deleting that edge and calculating shortest path
def compute_shortest_path_length(a,b):
    p=-1
    try:
        if train_graph.has_edge(a,b):
            train_graph.remove_edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
            train_graph.add_edge(a,b)
        else:
            p= nx.shortest_path_length(train_graph,source=a,target=b)
        return p
    except:
        return -1
```

```
In [19]:
```

```
#testing
compute_shortest_path_length(77697, 826021)

Out[19]:
10

In [20]:
#testing
compute_shortest_path_length(669354,1635354)
```

Out[20]:

4.2 Checking for same community

In [21]:

```
#getting weekly connected edges from graph
wcc=list(nx.weakly connected components(train graph))
def belongs_to_same_wcc(a,b):
   index = []
   if train_graph.has_edge(b,a):
       return 1
    if train graph.has edge(a,b):
            for i in wcc:
                if a in i:
                    index= i
                    break
            if (b in index):
                train_graph.remove_edge(a,b)
                if compute_shortest_path_length(a,b) ==-1:
                    train graph.add edge(a,b)
                    return 0
                else:
                    train_graph.add_edge(a,b)
                    return 1
            else:
                return 0
    else:
            for i in wcc:
                if a in i:
                    index= i
                    break
            if(b in index):
               return 1
            else:
                return 0
```

```
In [22]:
```

```
belongs_to_same_wcc(861, 1659750)

Out[22]:
0

In [23]:
belongs_to_same_wcc(669354,1635354)

Out[23]:
0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices. $A(x,y)=\sum_{u \in N(x)}\frac{u \in N(x)}{(x)}$

```
In [24]:
```

```
In [25]:

calc_adar_in(1,189226)

Out[25]:
0

In [26]:

calc_adar_in(669354,1635354)

Out[26]:
0

4.4 Is persion was following back:
```

```
In [27]:

def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0

In [28]:

follows_back(1,189226)

Out[28]:
1

In [29]:
follows_back(669354,1635354)

Out[29]:
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/
Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node is \$\$x_i = \alpha \sum_{i=1}^{n} x_j + \beta_i x_i + \beta_

where A is the adjacency matrix of the graph G with eigenvalues \$\$\lambda\$\$.

The parameter $\$ controls the initial centrality and $\$ and $\$ and $\$ and $\$ and $\$ and $\$

```
if not os.path.isfile('katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('katz.p','wb'))
else:
    katz = pickle.load(open('katz.p','rb'))
```

т∽ гэтт.

```
print('min', katz[min(katz, key=katz.get)])
print('max', katz[max(katz, key=katz.get)])
print('mean', float(sum(katz.values())) / len(katz))

min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018

In [32]:

mean_katz = float(sum(katz.values())) / len(katz)
print(mean_katz)

0.0007483800935562018
```

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm

```
In [33]:
```

```
if not os.path.isfile('hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits.open('hits.p','wb'))
else:
    hits = pickle.load(open('hits.p','rb'))
```

```
In [34]:
```

```
print('min',hits[0][min(hits[0], key=hits[0].get)])
print('max',hits[0][max(hits[0], key=hits[0].get)])
print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
```

5. Featurization

In [35]:

```
import random
if os.path.isfile('train_after_eda.csv'):
    filename = "train_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 15100030
    # n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n_train = 15100028
    s = 100000 #desired sample size
    skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
    #https://stackoverflow.com/a/22259008/4084039
```

In [36]:

```
if os.path.isfile('train_after_eda.csv'):
    filename = "test_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 3775008
# n_test = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n_test = 3775006
s = 50000 #desired sample size
    skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
```

In [37]:

```
print("Number of rows in the train data file:", n_train)
print("Number of rows we are going to elimiate in train data are",len(skip_train))
print("Number of rows in the test data file:", n_test)
print("Number of rows we are going to elimiate in test data are",len(skip_test))
```

Number of rows in the train data file: 15100028 Number of rows we are going to elimiate in train data are 15000028 Number of rows in the test data file: 3775006 Number of rows we are going to elimiate in test data are 3725006

In [38]:

```
df_final_train = pd.read_csv('train_after_eda.csv', skiprows=skip_train, names=['source_node', 'des
tination_node'])
df_final_train['indicator_link'] = pd.read_csv('train_y.csv', skiprows=skip_train, names=['indicato
r_link'])
print("Our train matrix size ",df_final_train.shape)
df_final_train.head(2)
```

Our train matrix size (100002, 3)

Out[38]:

source_node destination_node indicator_link 0 273084 1505602 1 1 350205 76813 1

In [39]:

```
df_final_test = pd.read_csv('test_after_eda.csv', skiprows=skip_test, names=['source_node', 'destin
ation_node'])
df_final_test['indicator_link'] = pd.read_csv('test_y.csv', skiprows=skip_test, names=['indicator_l
ink'])
print("Our test matrix size ",df_final_test.shape)
df_final_test.head(2)
```

Our test matrix size (50002, 3)

Out[39]:

	source_node	destination_node	indicator_link
0	848424	784690	1
1	264224	132395	1

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard_followees
- 3. cosine_followers
- 4. cosine_followees
- 5. num_followers_s
- 6. num_followees_s7. num_followers_d
- 8. num_followees_d
- 9. inter followers
- 10. inter_followees

```
In [40]:
```

```
if not os.path.isfile('data/fea_sample/storage_sample_stage1.h5'):
    #mapping jaccrd followers to train and test data
    df final train['jaccard followers'] = df final train.apply(lambda row:
jaccard for followers(row['source node'],row['destination node']),axis=1)
    df final test['jaccard followers'] = df final test.apply(lambda row:
jaccard for followers(row['source node'], row['destination node']), axis=1)
    #mapping jaccrd followees to train and test data
    df final train['jaccard followees'] = df final train.apply(lambda row:
jaccard for followees(row['source node'],row['destination node']),axis=1)
    df final test['jaccard followees'] = df final test.apply(lambda row:
jaccard_for_followees(row['source_node'],row['destination_node']),axis=1)
        #mapping jaccrd followers to train and test data
    df final train['cosine followers'] = df final train.apply(lambda row:
cosine for followers(row['source node'], row['destination node']), axis=1)
    df final test['cosine followers'] = df final test.apply(lambda row:
cosine for followers(row['source node'], row['destination node']), axis=1)
    #mapping jaccrd followees to train and test data
    df final train['cosine followees'] = df final train.apply(lambda row:
cosine_for_followees(row['source_node'], row['destination_node']), axis=1)
    df final test['cosine followees'] = df final test.apply(lambda row:
cosine for followees(row['source node'],row['destination node']),axis=1)
```

In [41]:

```
def compute features stage1(df final):
    #calculating no of followers followees for source and destination
    #calculating intersection of followers and followees for source and destination
    num followers s=[]
    num followees s=[]
    num_followers_d=[]
    num followees d=[]
    inter followers=[]
    inter_followees=[]
    for i,row in df final.iterrows():
            s1=set(train graph.predecessors(row['source node']))
            s2=set(train graph.successors(row['source node']))
        except:
            s1 = set()
            s2 = set()
        try:
            d1=set(train graph.predecessors(row['destination node']))
            d2=set(train graph.successors(row['destination node']))
        except:
            d1 = set()
            d2 = set()
        num followers s.append(len(s1))
        num followees s.append(len(s2))
        num followers d.append(len(d1))
        num followees d.append(len(d2))
        inter followers.append(len(s1.intersection(d1)))
        inter followees.append(len(s2.intersection(d2)))
    return num followers s, num followers d, num followees s, num followees d, inter followers, int
er followees
4
                                                                                                  |
```

```
df_final_train['num_followers_s'], df_final_train['num_followers_d'], \
    df_final_train['num_followes_s'], df_final_train['num_followees_d'], \
    df_final_train['inter_followers'], df_final_train['inter_followees']= compute_features_stagel(c
f_final_train)

    df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
        df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
        df_final_test['inter_followers'], df_final_test['inter_followees']=
    compute_features_stagel(df_final_test)

    hdf = HDFStore('storage_sample_stagel.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()

else:
    df_final_train = read_hdf('storage_sample_stagel.h5', 'train_df',mode='r')
    df_final_test = read_hdf('storage_sample_stagel.h5', 'test_df',mode='r')

#]
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [ ]:
```

```
if not os.path.isfile('storage_sample_stage2.h5'):
    #mapping adar index on train
    df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node']
,row['destination_node']),axis=1)
    #mapping adar index on test
    df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],r
ow['destination node']),axis=1)
   #mapping followback or not on train
    df_final_train['follows_back'] = df_final_train.apply(lambda row:
follows back(row['source node'], row['destination node']), axis=1)
    #mapping followback or not on test
   df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node']
,row['destination node']),axis=1)
   #mapping same component of wcc or not on train
    df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source
node'],row['destination_node']),axis=1)
    ##mapping same component of wcc or not on train
    df final test['same_comp'] = df_final_test.apply(lambda row: belongs_to_same_wcc(row['source_no
de'], row['destination node']), axis=1)
    #mapping shortest path on train
    df final train['shortest path'] = df final train.apply(lambda row: compute_shortest_path_length
(row['source node'], row['destination node']), axis=1)
    #mapping shortest path on test
    df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute shortest path length(r
ow['source node'], row['destination node']), axis=1)
    hdf = HDFStore('storage sample stage2.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df final train = read hdf('storage sample stage2.h5', 'train df', mode='r')
    df final test = read hdf('storage sample stage2.h5', 'test df',mode='r')
```

•

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. Credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

\begin{equation} W = \frac{1}{\sqrt{1+|X|}} \end{equation}

it is directed graph so calculated Weighted in and Weighted out differently

In [44]:

In [45]:

```
if not os.path.isfile('storage_sample_stage3.h5'):
    #mapping to pandas train
    df_final_train['weight_in'] = df_final_train.destination_node.apply(lambda x: Weight_in.get(x,m ean_weight_in))
    df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out.get(x,mean_weight_out))

#mapping to pandas test
    df_final_test['weight_in'] = df_final_test.destination_node.apply(lambda x: Weight_in.get(x,mean_out.get(x)))
```

```
n_weignt_in;)
   df_final_test['weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out.get(x,mean_w
eight_out))

#some features engineerings on the in and out weights
   df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
   df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_out
   df_final_train['weight_f3'] = (2*df_final_train.weight_in + 1*df_final_train.weight_out)
   df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_out)

#some features engineerings on the in and out weights
   df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
   df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
   df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
   df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)
```

In [46]:

```
if not os.path.isfile('storage sample stage3.h5'):
        #page rank for source and destination in Train and Test
        #if anything not there in train graph then adding mean page rank
        df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
        df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x:pr.get(x,mean_pr
))
        df_final_test['page_rank_s'] = df_final_test.source_node.apply(lambda x:pr.get(x,mean_pr))
        df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
        #Katz centrality score for source and destination in Train and test
        #if anything not there in train graph then adding mean katz score
        df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x,mean_katz))
        df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x,mean_katz
))
        df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x,mean_katz))
        df_final_test['katz_d'] = df_final_test.destination_node.apply(lambda x: katz.get(x,mean_katz))
        #Hits algorithm score for source and destination in Train and test
        #if anything not there in train graph then adding 0
        \label{eq:contraction} $$ df_final_train.source_node.apply( \textbf{lambda} x: hits[0].get(x,0)) $$ $$
        df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].get(x,0))
        \label{eq:control_def} $$ df_final_test.source_node.apply( \textbf{lambda} x: hits[0].get(x,0)) $$ $$ (x,0) = df_final_test.source_node.apply( \textbf{lambda} x: hits[0].get(x,0)) $$ (x,0) = df_final_test.source_node.apply( \textbf{lambda} x: hits[0].ge
        df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
        #Hits algorithm score for source and destination in Train and Test
        #if anything not there in train graph then adding 0
        df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda x: hits[1].get(x,0))
        df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x
,0))
        df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
        df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: hits[1].get(x,0
))
        hdf = HDFStore('storage sample stage3.h5')
        hdf.put('train_df',df_final_train, format='table', data_columns=True)
        hdf.put('test_df',df_final_test, format='table', data_columns=True)
       hdf.close()
else:
        df_final_train = read_hdf('storage_sample_stage3.h5', 'train_df',mode='r')
        df_final_test = read_hdf('storage_sample_stage3.h5', 'test_df',mode='r')
```

In [47]:

```
df_final_train.head()
```

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	350205	76813	1	0	0.000000	0.000000	0.000000	
2	1200905	283891	1	0	0.052632	0.055556	0.109109	
3	247831	1403584	1	0	0.000000	0.000000	0.000000	
4	233609	1837109	1	0	0.000000	0.000000	0.000000	

5 rows × 31 columns

Adding new feature Preferential Attachement

One well-known concept in social networks is that users with many friends tend to create more connections in the future. This is due to the fact that in some social networks, like in finance, the rich get richer. We estimate how "rich" our two vertices are by calculating the multiplication between the number of friends ($|\Gamma(x)|$) or followers each vertex has.

Preferential Attachement for followers

In [53]:

Out[53]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	350205	76813	1	0	0.000000	0.000000	0.000000	
2	1200905	283891	1	0	0.052632	0.055556	0.109109	
3	247831	1403584	1	0	0.000000	0.000000	0.000000	
4	233609	1837109	1	0	0.000000	0.000000	0.000000	

5 rows × 32 columns

4

In [54]:

```
#for test dataset
nfs=np.array(df_final_test['num_followers_s'])
nfd=np.array(df_final_test['num_followers_d'])
preferential_followers=[]
for i in range(len(nfs)):
    preferential_followers.append(nfd[i]*nfs[i])
df_final_test['prefer_Attach_followers']= preferential_followers
df_final_test.head()
```

Out[54]:

0	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
1	264224	132395	1	0	0.4000	0.353553	0.571429	
2	289059	253522	1	0	0.0000	0.000000	0.000000	
3	1749265	963357	1	0	0.1875	0.121212	0.316228	
4	1199100	991335	1	0	0.0000	0.000000	0.000000	

5 rows × 32 columns

4

Preferential Attachement for followers

```
In [55]:
```

```
#for train dataset
nfs=np.array(df_final_train['num_followees_s'])
nfd=np.array(df_final_train['num_followees_d'])
preferential_followees=[]
for i in range(len(nfs)):
    preferential_followees.append(nfd[i]*nfs[i])
df_final_train['prefer_Attach_followees']= preferential_followees
df_final_train.head()
```

Out[55]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	350205	76813	1	0	0.000000	0.000000	0.000000	
2	1200905	283891	1	0	0.052632	0.055556	0.109109	
3	247831	1403584	1	0	0.000000	0.000000	0.000000	
4	233609	1837109	1	0	0.000000	0.000000	0.000000	

5 rows × 33 columns

4 P

In [56]:

```
#for test dataset
nfs=np.array(df_final_test['num_followees_s'])
nfd=np.array(df_final_test['num_followees_d'])
preferential_followees=[]
for i in range(len(nfs)):
    preferential_followees.append(nfd[i]*nfs[i])
df_final_test['prefer_Attach_followees']= preferential_followees
df_final_test.head()
```

Out[56]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
0	848424	784690	1	0	0.0000	0.029161	0.000000	
1	264224	132395	1	0	0.4000	0.353553	0.571429	
2	289059	253522	1	0	0.0000	0.000000	0.000000	
3	1749265	963357	1	0	0.1875	0.121212	0.316228	
4	1199100	991335	1	0	0.0000	0.000000	0.000000	

4

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [57]:

def svd(x, S):
    try:
        z = sadj_dict[x]
        return S[z]
    except:
        return [0,0,0,0,0,0]

In [58]:

#for svd features to get feature vector creating a dict node val and inedx in svd vector
sadj_col = sorted(train_graph.nodes())
sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
```

```
In [59]:
```

```
Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype()
```

In [60]:

```
U, s, V = svds(Adj, k = 6)
print('Adjacency matrix Shape', Adj.shape)
print('U Shape', U.shape)
print('V Shape', V.shape)
print('s Shape', s.shape)
```

```
Adjacency matrix Shape (1780722, 1780722)
U Shape (1780722, 6)
V Shape (6, 1780722)
s Shape (6,)
```

In [61]:

```
df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] =
     df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
     df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] =
     df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
     df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] =
     df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
     df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5','svd v d 6']] =
     df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
        hdf = HDFStore('data/fea sample/storage sample stage4.h5')
        hdf.put('train_df',df_final_train, format='table', data_columns=True)
        hdf.put('test df',df final test, format='table', data columns=True)
        hdf.close()
 4
In [62]:
df final train.head()
Out[62]:
    source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followe
 0
         273084
                         1505602
                                            1
                                                             0
                                                                        0.000000
                                                                                        0.000000
                                                                                                         0.000000
                                                                                        0.000000
                                                                                                         0.000000
 1
         350205
                           76813
                                            1
                                                             0
                                                                        0.000000
        1200905
                          283891
                                                                        0.052632
                                                                                        0.055556
                                                                                                         0.109109
 2
 3
         247831
                         1403584
                                            1
                                                             0
                                                                        0.000000
                                                                                        0.000000
                                                                                                         0.000000
         233609
                         1837109
                                                                        0.000000
                                                                                        0.000000
                                                                                                         0.000000
5 rows × 57 columns
4
In [65]:
df final train.columns
Out[65]:
Index(['source node', 'destination node', 'indicator link',
          'jaccard_followers', 'jaccard_followees', 'cosine_followers',
         'cosine_followees', 'num_followers_s', 'num_followers_d', 'num_followees_s', 'num_followees_d', 'inter_followers',
         'inter_followees', 'adar_index', 'follows_back', 'same_comp',
         'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
         'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
         'prefer_Attach_followers', 'prefer_Attach_followees', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6',
         'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3',
```

```
'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'], dtype='object')
```

Adding feature svd_dot

svd dot is Dot product between sourse node svd and destination node svd features

```
In [69]:
```

```
#for train datasets
s1,s2,s3,s4,s5,s6=df_final_train['svd_u_s_1'],df_final_train['svd_u_s_2'],df_final_train['svd_u_s_3'],df_final_train['svd_u_s_4'],df_final_train['svd_u_s_5'],df_final_train['svd_u_s_6']
s7,s8,s9,s10,s11,s12=df_final_train['svd_v_s_1'],df_final_train['svd_v_s_2'],df_final_train['svd_v_s_3'],df_final_train['svd_v_s_5'],df_final_train['svd_v_s_6']

d1,d2,d3,d4,d5,d6=df_final_train['svd_u_d_1'],df_final_train['svd_u_d_2'],df_final_train['svd_u_d_3'],df_final_train['svd_u_d_5'],df_final_train['svd_u_d_6']
d7,d8,d9,d10,d11,d12=df_final_train['svd_v_d_1'],df_final_train['svd_v_d_2'],df_final_train['svd_v_d_3'],df_final_train['svd_v_d_5'],df_final_train['svd_v_d_6']
```

In [70]:

```
svd dot=[]
for i in range(len(np.array(s1))):
    a=[]
   b=[]
    a.append(np.array(s1[i]))
    a.append(np.array(s2[i]))
    a.append(np.array(s3[i]))
    a.append(np.array(s4[i]))
    a.append(np.array(s5[i]))
    a.append(np.array(s6[i]))
    a.append(np.array(s7[i]))
    a.append(np.array(s8[i]))
    a.append(np.array(s9[i]))
    a.append(np.array(s10[i]))
    a.append(np.array(s11[i]))
    a.append(np.array(s12[i]))
    b.append(np.array(d1[i]))
    b.append(np.array(d2[i]))
    b.append(np.array(d3[i]))
    b.append(np.array(d4[i]))
    b.append(np.array(d5[i]))
    b.append(np.array(d6[i]))
    b.append(np.array(d7[i]))
    b.append(np.array(d8[i]))
    b.append(np.array(d9[i]))
    b.append(np.array(d10[i]))
    b.append(np.array(d11[i]))
    b.append(np.array(d12[i]))
    svd_dot.append(np.dot(a,b))
df final train['svd dot'] = svd dot
```

In [71]:

```
df_final_train.head()
```

Out[71]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followe
0	273084	1505602	1	0	0.000000	0.000000	0.000000	
1	350205	76813	1	0	0.000000	0.000000	0.000000	
2	1200905	283891	1	0	0.052632	0.055556	0.109109	

```
233609
                                                                                                                                                                                                     0.000000
                                              1837109
                                                                                                                                       0.000000
                                                                                                                                                                     0.000000
5 rows × 58 columns
In [72]:
#for test dataset
\verb|s1,s2,s3,s4,s5,s6| = \texttt|df_final_test['svd_u_s_1'], \\ df_final_test['svd_u_s_2'], \\ df_final_test['svd_u_s_3'] \\ ext| 
 ,df_final_test['svd_u_s_4'],df_final_test['svd_u_s_5'],df_final_test['svd_u_s_6']
s7,s8,s9,s10,s11,s12=df_final_test['svd_v_s_1'],df_final_test['svd_v_s_2'],df_final_test['svd_v_s_3
 '],df_final_test['svd_v_s_4'],df_final_test['svd_v_s_5'],df_final_test['svd_v_s_6']
d1,d2,d3,d4,d5,d6=df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_3']
,df_final_test['svd_u_d_4'],df_final_test['svd_u_d_5'],df_final_test['svd_u_d_6']
d7,d8,d9,d10,d11,d12=df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_final_test['svd_v_d_3
 '],df_final_test['svd_v_d_4'],df_final_test['svd_v_d_5'],df_final_test['svd_v_d_6']
In [73]:
svd dot=[]
for i in range(len(np.array(s1))):
         a=[]
         b=[]
         a.append(np.array(s1[i]))
         a.append(np.array(s2[i]))
         a.append(np.array(s3[i]))
         a.append(np.array(s4[i]))
         a.append(np.array(s5[i]))
         a.append(np.array(s6[i]))
         a.append(np.array(s7[i]))
         a.append(np.array(s8[i]))
         a.append(np.array(s9[i]))
         a.append(np.array(s10[i]))
         a.append(np.array(s11[i]))
         a.append(np.array(s12[i]))
         b.append(np.array(d1[i]))
         b.append(np.array(d2[i]))
         b.append(np.array(d3[i]))
         b.append(np.array(d4[i]))
         b.append(np.array(d5[i]))
         b.append(np.array(d6[i]))
         b.append(np.array(d7[i]))
         b.append(np.array(d8[i]))
         b.append(np.array(d9[i]))
         b.append(np.array(d10[i]))
         b.append(np.array(d11[i]))
         b.append(np.array(d12[i]))
         svd dot.append(np.dot(a,b))
df final test['svd dot'] = svd dot
In [74]:
df final test.head()
Out[74]:
       source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followe
                                                                                                                  0
 0
                848424
                                                784690
                                                                                   1
                                                                                                                                          0.0000
                                                                                                                                                                     0.029161
                                                                                                                                                                                                     0.000000
                264224
                                                132395
                                                                                                                  0
                                                                                                                                          0.4000
                                                                                                                                                                     0.353553
                                                                                                                                                                                                     0.571429
 2
                289059
                                                253522
                                                                                                                                          0.0000
                                                                                                                                                                     0.000000
                                                                                                                                                                                                     0.000000
```

source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followe

```
source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followe
       1749265
       1199100
                       991335
                                                        0
                                                                    0.0000
                                                                                 0.000000
                                                                                                 0.000000
5 rows × 58 columns
In [76]:
hdf = HDFStore('storage sample stage4.h5')
hdf.put('train df', df final train, format='table', data columns=True)
hdf.put('test df', df final test, format='table', data columns=True)
hdf.close()
In [77]:
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import csv
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
 # if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
 # to install xgboost: pip3 install xgboost
import xgboost as xgb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore, DataFrame
from pandas import read hdf
from scipy.sparse.linalg import svds, eigs
import gc
from tqdm import tqdm
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import f1 score
In [78]:
df final train.columns
Out[78]:
Index(['source node', 'destination node', 'indicator link',
         'jaccard_followers', 'jaccard_followees', 'cosine_followers',
        'cosine_followees', 'num_followers_s', 'num_followers_d',
'num_followees_s', 'num_followees_d', 'inter_followers',
'inter_followees', 'adar_index', 'follows_back', 'same_comp',
        'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
        'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
        'katz d', 'hubs s', 'hubs d', 'authorities s', 'authorities d',
        'prefer_Attach_followers', 'prefer_Attach_followees', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6',
        'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5',
        'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4',
        'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6', 'svd_dot'],
```

```
dtype='object')
```

In [79]:

```
y_train = df_final_train.indicator_link
y_test = df_final_test.indicator_link
```

In [80]:

```
df_final_train.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=True)
df_final_test.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=True)
```

In [81]:

```
estimators = [10, 50, 100, 250, 450]
train scores = []
test scores = []
for i in estimators:
    clf = RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
            max_depth=5, max_features='auto', max_leaf_nodes=None,
            min_impurity_decrease=0.0, min_impurity_split=None,
            min samples leaf=52, min samples split=120,
            min_weight_fraction_leaf=0.0, n_estimators=i, n_jobs=-1,random_state=25,verbose=0,warm_
start=False)
    clf.fit(df_final_train,y_train)
    train_sc = f1_score(y_train,clf.predict(df_final_train))
    test sc = f1 score(y_test,clf.predict(df_final_test))
    test_scores.append(test_sc)
    train scores.append(train sc)
    print('Estimators = ',i,'Train Score',train sc,'test Score',test sc)
plt.plot(estimators, train scores, label='Train Score')
plt.plot(estimators, test scores, label='Test Score')
plt.xlabel('Estimators')
plt.ylabel('Score')
plt.title('Estimators vs score at depth of 5')
```

```
Estimators = 10 Train Score 0.9098260968992651 test Score 0.9027976742226341

Estimators = 50 Train Score 0.9193635607321131 test Score 0.8992469654628069

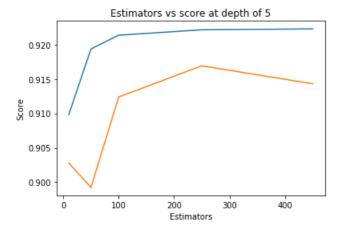
Estimators = 100 Train Score 0.9213647068631332 test Score 0.9123853017040889

Estimators = 250 Train Score 0.922151931824123 test Score 0.9169170863842214

Estimators = 450 Train Score 0.9222848891353711 test Score 0.9143039049235995
```

Out[81]:

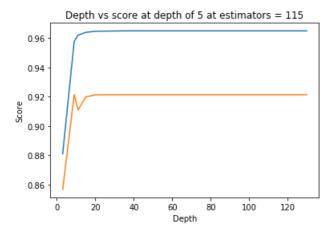
Text(0.5, 1.0, 'Estimators vs score at depth of 5')



In [82]:

```
min impurity decrease=0.0, min_impurity_split=None,
            min_samples_leaf=52, min_samples_split=120,
            min_weight_fraction_leaf=0.0, n_estimators=115, n_jobs=-1,random_state=25,verbose=0,war
m start=False)
   clf.fit(df_final_train,y_train)
    train sc = f1 score(y train,clf.predict(df final train))
    test_sc = f1_score(y_test,clf.predict(df_final_test))
    test_scores.append(test_sc)
    train scores.append(train sc)
    print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
plt.plot(depths,train_scores,label='Train Score')
plt.plot(depths, test scores, label='Test Score')
plt.xlabel('Depth')
plt.ylabel('Score')
plt.title('Depth vs score at depth of 5 at estimators = 115')
plt.show()
```

```
depth = 3 Train Score 0.8810698327858115 test Score 0.8568133350742045
depth = 9 Train Score 0.9577372747230306 test Score 0.9214581783398874
depth = 11 Train Score 0.9619094028547643 test Score 0.9109016920111374
depth = 15 Train Score 0.9638184936720423 test Score 0.9198179420647412
depth = 20 Train Score 0.9645779882568882 test Score 0.921292953319458
depth = 35 Train Score 0.9648535734566399 test Score 0.9213712246718492
depth = 50 Train Score 0.9648535734566399 test Score 0.9213712246718492
depth = 70 Train Score 0.9648535734566399 test Score 0.9213712246718492
depth = 130 Train Score 0.9648535734566399 test Score 0.9213712246718492
```



In [83]:

```
from sklearn.metrics import fl_score
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import f1 score
from sklearn.model_selection import RandomizedSearchCV
from scipy.stats import randint as sp randint
from scipy.stats import uniform
param dist = {"n estimators":sp randint(105,125),
              "max_depth": sp_randint(10,15),
              "min_samples_split": sp_randint(110,190),
              "min_samples_leaf": sp_randint(25,65)}
clf = RandomForestClassifier(random state=25, n jobs=-1)
rf random = RandomizedSearchCV(clf, param distributions=param dist,
                                   n iter=5,cv=10,scoring='f1',random state=25)
rf random.fit(df final train,y train)
print('mean test scores',rf random.cv results ['mean test score'])
print('mean train scores',rf random.cv results ['mean train score'])
```

mean test scores $[0.96268665\ 0.9623128\ 0.96125205\ 0.96238543\ 0.96369861]$ mean train scores $[0.96356236\ 0.96323862\ 0.96180049\ 0.96303285\ 0.96482231]$

In [84]:

```
print(rf_random.best_estimator_)
```

```
RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
            max depth=14, max features='auto', max leaf nodes=None,
            min impurity decrease=0.0, min impurity split=None,
            min_samples_leaf=28, min_samples_split=111,
            min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1,
            oob score=False, random state=25, verbose=0, warm start=False)
In [85]:
clf=RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
            max depth=14, max features='auto', max leaf nodes=None,
            min impurity decrease=0.0, min impurity split=None,
            min samples leaf=28, min samples split=111,
            min weight fraction leaf=0.0, n estimators=121, n jobs=-1,
            oob_score=False, random_state=25, verbose=0, warm_start=False)
In [86]:
clf.fit(df_final_train,y_train)
y_train_pred = clf.predict(df_final_train)
y test pred = clf.predict(df final test)
In [87]:
from sklearn.metrics import f1 score
print('Train f1 score', f1 score(y train, y train pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
Train f1 score 0.9648075109754738
Test f1 score 0.9213158621275512
In [88]:
from sklearn.metrics import confusion matrix
def plot_confusion_matrix(test_y, predict_y):
    C = confusion matrix(test y, predict y)
    A = (((C.T) / (C.sum(axis=1))).T)
    B = (C/C.sum(axis=0))
    plt.figure(figsize=(20,4))
    labels = [0,1]
    # representing A in heatmap format
    cmap=sns.light_palette("blue")
    plt.subplot(1, 3, 1)
    sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
    plt.xlabel('Predicted Class')
    plt.ylabel('Original Class')
    plt.title("Confusion matrix")
    plt.subplot(1, 3, 2)
    sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
    plt.xlabel('Predicted Class')
    plt.ylabel('Original Class')
    plt.title("Precision matrix")
    plt.subplot(1, 3, 3)
    # representing B in heatmap format
    sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
    plt.xlabel('Predicted Class')
    plt.ylabel('Original Class')
    plt.title("Recall matrix")
    plt.show()
```

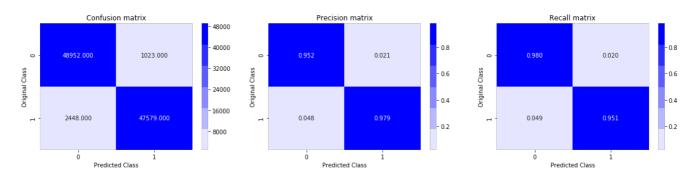
In [89]:

print('Train confusion matrix')

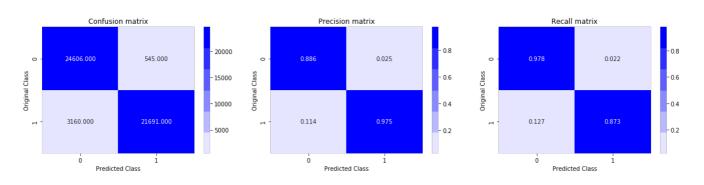
plot confusion matrix(v train.v train pred)

```
print('Test confusion_matrix')
plot_confusion_matrix(y_test,y_test_pred)
```

Train confusion_matrix

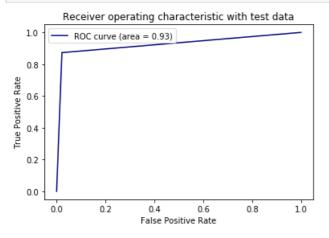


Test confusion matrix



In [90]:

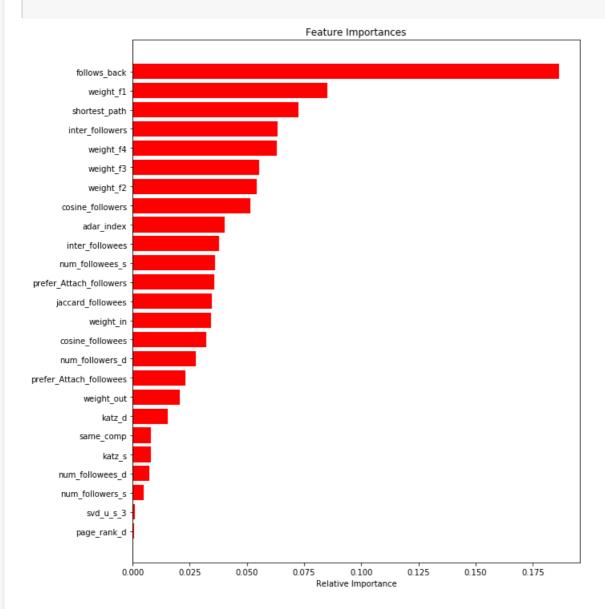
```
from sklearn.metrics import roc_curve, auc
fpr,tpr,ths = roc_curve(y_test,y_test_pred)
auc_sc = auc(fpr, tpr)
plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc_sc)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic with test data')
plt.legend()
plt.show()
```



In [91]:

```
features = df_final_train.columns
importances = clf.feature_importances_
indices = (np.argsort(importances))[-25:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
```

plt.show()



Applying XGBOOST

colsample_bytree=1, gamma=0, learning_rate=0.1, max_delta_step=0,
max_denth=10 min_child_weight=1 missing=None n_estimators=109

```
max_depth=10, min_chitd_weight=1, missing=None, n_estimators=100,
n_jobs=1, nthread=None, objective='binary:logistic', random_state=0,
reg_alpha=0, reg_lambda=1, scale_pos_weight=1, seed=None,
silent=True, subsample=1)
```

In [96]:

In [97]:

```
clf.fit(df_final_train,y_train)
y_train_pred = clf.predict(df_final_train)
y_test_pred = clf.predict(df_final_test)
```

In [98]:

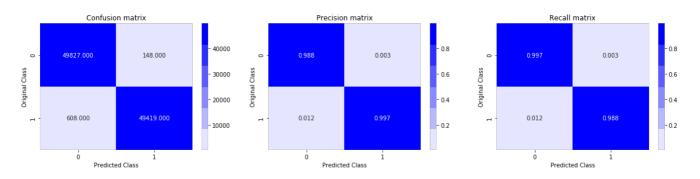
```
from sklearn.metrics import f1_score
print('Train f1 score',f1_score(y_train,y_train_pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
```

Train f1 score 0.9924091812759805 Test f1 score 0.9262852634496876

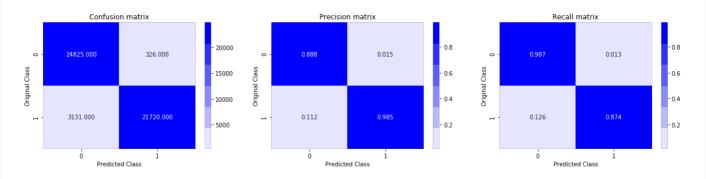
In [99]:

```
print('Train confusion_matrix')
plot_confusion_matrix(y_train_pred)
print('Test confusion_matrix')
plot_confusion_matrix(y_test,y_test_pred)
```

 ${\tt Train \ confusion_matrix}$



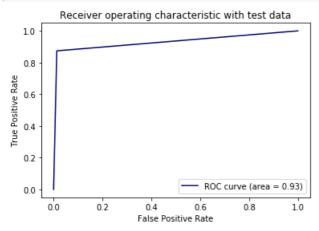
Test confusion matrix



In [100]:

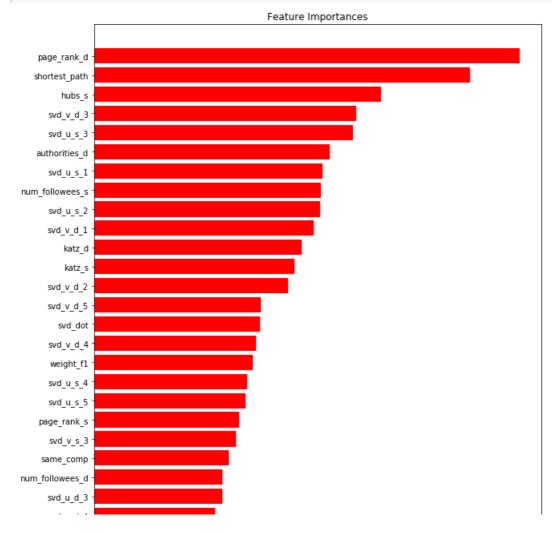
from sklearn.metrics import roc_curve, auc
fpr,tpr,ths = roc curve(y test,y test pred)

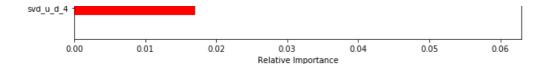
```
auc_sc = auc(fpr, tpr)
plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc_sc)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic with test data')
plt.legend()
plt.show()
```



In [101]:

```
features = df_final_train.columns
importances = clf.feature_importances_
indices = (np.argsort(importances))[-25:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```





Procedure and Observation

In [105]:

```
from prettytable import PrettyTable
x = PrettyTable()
x.field_names = ["Model", "n_estimators", "max_depth", "Train f1-Score","Test f1-Score"]
x.add_row(['Random Forest','121','14','0.964','0.921'])
x.add_row(['XGBOOST','109','10','0.992','0.926'])
print(x)
```

Model	n_estimators 		Train f1-Score	
Random Forest XGBOOST	121 109	14	0.964	0.921 0.926

- 1) Initially we have only a couple feature in our data-set. First we performed exploratory data analysis on our given data set such as number of followers and followees of each person.
- 2) Then after we generated some datapoints which were not present in our given data-set, since we had only class label 1 data.
- 3) Then we did some feature engineering on dataset like finding shortest path, kartz centrality, jaccard distances, page rank, preferential attachements etc.
- 4) After performing eploratory data analysis and feature engineering we splitted whole dataset into train and test and performed random forest and xgboost taking f1-score as our metric.
- 5) At the end we plotted confusion matrix and pretty-table for both algorithm and found best hyperparameters.

```
In [ ]:
```