

公式（三角関数）

角の単位変換

$$\text{度} \quad \text{ラジアン} : \quad \alpha^{\circ} = \frac{\alpha\pi}{180} \qquad \text{ラジアン} \quad \text{度} : \quad \theta = \left(\frac{180\theta}{\pi} \right)^{\circ}$$

一般角の公式

$$\sin(\alpha + 2n\pi) = \sin \alpha \qquad \cos(\alpha + 2n\pi) = \cos \alpha \qquad \tan(\alpha + 2n\pi) = \tan \alpha \quad (n \text{ は整数})$$

反角公式

$$\sin(-\alpha) = -\sin \alpha \qquad \cos(-\alpha) = +\cos \alpha \qquad \tan(-\alpha) = -\tan \alpha$$

余角公式

$$\sin\left(\frac{\pi}{2} - \alpha\right) = \cos \alpha \qquad \cos\left(\frac{\pi}{2} - \alpha\right) = \sin \alpha \qquad \tan\left(\frac{\pi}{2} - \alpha\right) = \frac{1}{\tan \alpha}$$

補角公式

$$\sin(\pi - \alpha) = +\sin \alpha \qquad \cos(\pi - \alpha) = -\cos \alpha \qquad \tan(\pi - \alpha) = -\tan \alpha$$

相互関係

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\cos^2 \theta + \sin^2 \theta = 1 \qquad 1 + \tan^2 \theta = \frac{1}{\cos^2 \theta} \qquad \frac{1}{\tan^2 \theta} + 1 = \frac{1}{\sin^2 \theta}$$

加法定理

$$\begin{aligned} \sin(\alpha + \beta) &= \sin \alpha \cos \beta + \cos \alpha \sin \beta & \sin(\alpha - \beta) &= \sin \alpha \cos \beta - \cos \alpha \sin \beta \\ \cos(\alpha + \beta) &= \cos \alpha \cos \beta - \sin \alpha \sin \beta & \cos(\alpha - \beta) &= \cos \alpha \cos \beta + \sin \alpha \sin \beta \\ \tan(\alpha + \beta) &= \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} & \tan(\alpha - \beta) &= \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta} \end{aligned}$$

倍角公式

$$\begin{aligned} \sin 2\theta &= 2 \sin \theta \cos \theta \\ \cos 2\theta &= \cos^2 \theta - \sin^2 \theta & \cos 2\theta &= 2 \cos^2 \theta - 1 & \cos 2\theta &= 1 - 2 \sin^2 \theta \\ \tan 2\theta &= \frac{2 \tan \theta}{1 - \tan^2 \theta} & \cos 2\theta &= \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} & \sin 2\theta &= \frac{2 \tan \theta}{1 + \tan^2 \theta} \end{aligned}$$

半角公式

$$\sin^2 \frac{\theta}{2} = \frac{1 - \cos \theta}{2}$$

$$\cos^2 \frac{\theta}{2} = \frac{1 + \cos \theta}{2}$$

三倍角公式

$$\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$$

$$\sin^3 \theta = \frac{3 \sin \theta - \sin 3\theta}{4}$$

$$\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$$

$$\cos^3 \theta = \frac{3 \cos \theta + \cos 3\theta}{4}$$

積和公式

$$\sin \alpha \cos \beta = \frac{1}{2} (\sin(\alpha + \beta) + \sin(\alpha - \beta)) \quad \cos \alpha \sin \beta = \frac{1}{2} (\sin(\alpha + \beta) - \sin(\alpha - \beta))$$

$$\cos \alpha \cos \beta = \frac{1}{2} (\cos(\alpha + \beta) + \cos(\alpha - \beta)) \quad \sin \alpha \sin \beta = -\frac{1}{2} (\cos(\alpha + \beta) - \cos(\alpha - \beta))$$

和積公式

$$\sin \alpha + \sin \beta = 2 \sin \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2} \quad \sin \alpha - \sin \beta = 2 \cos \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$$

$$\cos \alpha + \cos \beta = 2 \cos \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2} \quad \cos \alpha - \cos \beta = -2 \sin \frac{\alpha + \beta}{2} \sin \frac{\alpha - \beta}{2}$$

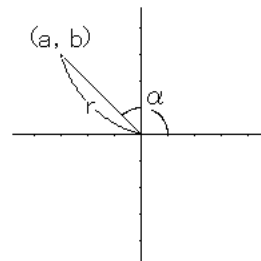
合成

$$a \sin \theta + b \cos \theta = r \sin(\theta + \alpha)$$

$$a \cos \theta + b \sin \theta = r \cos(\theta - \alpha)$$

$$\text{ただし, } r = \sqrt{a^2 + b^2}$$

$$\cos \alpha = \frac{a}{r}, \quad \sin \alpha = \frac{b}{r}$$



逆三角関数

$$\theta = \sin^{-1} y \quad \Longleftrightarrow \quad \sin \theta = y \quad \text{かつ} \quad -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

$$\theta = \cos^{-1} x \quad \Longleftrightarrow \quad \cos \theta = x \quad \text{かつ} \quad 0 \leq \theta \leq \pi$$

$$\theta = \tan^{-1} m \quad \Longleftrightarrow \quad \tan \theta = m \quad \text{かつ} \quad -\frac{\pi}{2} < \theta < \frac{\pi}{2}$$