#### Game Theory

Caroline Liu Vincent Macri Samantha Unger



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#### What is game theory?

"Game theory is about finding a way to rig games in your favour"



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— Vincent Macri



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#### The first game

# Pick Up Sticks!

The most accurately named game of all time.



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Variations include the winner being the one who takes the last stick, or the loser being the one who takes the last stick.

The game can be structured in such ways that certain players can win every time. Lets look at some of these scenarios!



# The scenarios: your worksheet Pick Up Sticks!

Let's go over some scenarios.



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Scenario 1 Whoever picks the last stick **loses**. Which player can guarantee a win?

There are 24 sticks in total, and the players can take up to 4 sticks.



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Scenario 1 Whoever picks the last stick **loses**. Which player can guarantee a win?

There are 24 sticks in total, and the players can take up to 4 sticks.

Scenario 2 Whoever picks the last stick **wins**. Which player can guarantee a win?

There are 35 sticks, and the players can take up to 4 sticks on their turns.



Try it out yourself!
Pick Up Sticks!

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# Answers: The Strats Pick Up Sticks!

Let's take those scenarios up together.



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Scenario 1 Player 1 always wins. Why?



#### Answers: The Strats Pick Up Sticks!

Let's take those scenarios up together.

Scenario 1 Player 1 always wins. Why?

Scenario 2 Player 2 always wins. Why?

