

Euclid Preparation 3

Circle Geometry

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Table of Contents

1 Star Trek Theorem

■ Theorem

■ Proof

■ Extensions

■ Extension 1

■ Extension 2

■ Extension 3

■ Extension 4

■ Extension 5

2 Crossed Chord Theorem

■ Theorem



Extending



Table of Contents

1 Star Trek Theorem

- Theorem

 - Proof

- Extensions

 - Extension 1

 - Extension 2

 - Extension 3

 - Extension 4

 - Extension 5

2 Crossed Chord Theorem

- Theorem

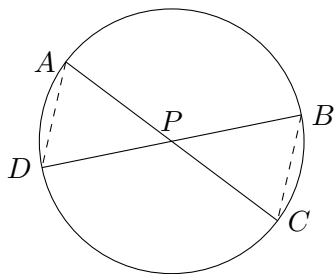


Theorem

Crossed Chord Theorem

Theorem (“Crossed Chord” Theorem)

If two chords AB and CD of a circle intersect at point P , then $(PA)(PB) = (PC)(PD)$.

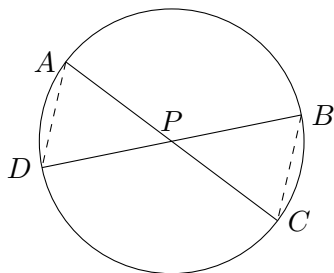


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Theorem (“Crossed Chord” Theorem)

If two chords AB and CD of a circle intersect at point P , then $(PA)(PB) = (PC)(PD)$.



This is proved using similar triangles and the fifth extension we developed for the Star Trek theorem. Try to prove it yourself!

