

Complex Numbers

The Riemann Hypothesis

Prove or disprove the following statement:

The nontrivial zeros of $\zeta(s)$ have real part equal to $\frac{1}{2}$.

Where:

$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s} \{s \in \mathbb{C} \mid \operatorname{Re}(s) > 1\}$$

$$\zeta(s) = 2^s \pi^{s-1} \sin\left(\frac{\pi s}{2}\right) \Gamma(1-s) \zeta(1-s) \{s \in \mathbb{C} \mid s \neq 1\}$$