Complex Numbers and the Riemann Hypothesis How to win \$1 000 000

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1 The Riemann Zeta Function



Definition (The Riemann zeta function)

$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s} \left\{ s \in \mathbb{C} \mid \text{Re}(s) > 1 \right\}$$



Definition (The Riemann zeta function)

$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s} \left\{ s \in \mathbb{C} \mid \frac{\text{Re}(s)}{s} > 1 \right\}$$
$$s = \sigma + it$$