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Física

1- $x(t) = ct$

$$y(t) = ct(1 - \beta t)$$

a) $t = \frac{x}{c} \Rightarrow y(x) = \left(\frac{x}{c}\right) \left[1 - \beta \left(\frac{x}{c}\right)\right]$

$$= \frac{x}{c} - \frac{\beta x^2}{c^2}$$

b) $\frac{dx}{dt} = c$ $c = \frac{dy}{dt} = c(1 - 2\beta t)$

$$|v(t)| = \sqrt{\left(\frac{dx}{dt}\right)^2} + \sqrt{\left(\frac{dy}{dt}\right)^2}$$

$$|v(t)| = \sqrt{c^2 + c^2(1 - 2\beta t)^2}$$
$$= \sqrt{2c^2 - 4c^2\beta t + 4c^2\beta^2 t^2}$$

c) $n = \sqrt{x^2 + y^2}$

$$n = \sqrt{ct^2 + ct(1 - \beta t)^2}$$

$$n = \sqrt{2c^2 t^2 - 2c^2 \beta t^3 + c^2 \beta^2 t^4}$$

2- $\vec{F} = 2xy\vec{i} + x^2\vec{j}$

A(0;0)

B(2;4)

$$W = \int \vec{F} \cdot d\vec{n}$$

$$a) y = 2x$$

$$dn = dx \vec{i} + 2dx \vec{j}$$

$$W = \int (2x \vec{i} + x^2) \cdot (dx \vec{i} + 2dx \vec{j})$$

$$= \int (2x dx + 2x^2 dx)$$

$$= \int (2x + 2x^2) dx$$

$$= \int 2x dx + \int 2x^2 dx$$

$$= 2^2 + \left(\frac{2}{3}\right) \cdot 2^3 - 0$$

$$= 4 + \left(\frac{16}{3}\right) - 0$$

$$= \frac{12}{3} + \frac{16}{3}$$

$$= \frac{28}{3} = 9,3 \text{ J}$$

$$b) y(0,4) \quad x(2,4)$$

$$dn = 0i + dyj$$

$$W = \int (2xi + x^2j) (0i + dyj)$$

$$= \int x^2 dy$$

$$= x^2 y \Big|_0^4$$

$$= 2^2 \cdot 4 - 0$$

$$= 16 \text{ J}$$

$$W = \int (2xi + x^2j) (dx i + 0j)$$

$$= \int 2x dx$$

$$= x^2 \Big|_0^2$$

$$= 4 \text{ J}$$

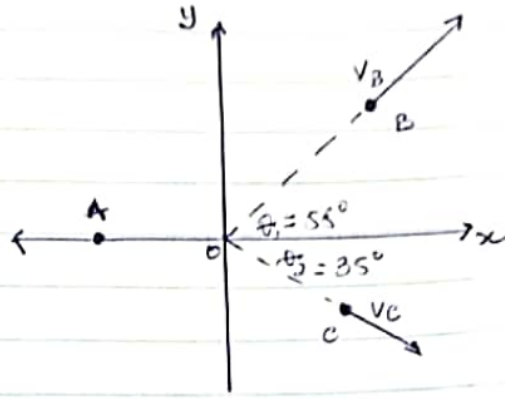
$$c) W_1 \neq W_2$$

$$W_1 = 16 + 4$$

$$W_1 = 20 \text{ J}$$

$9,3 \neq 20 \Rightarrow$ o trabalho varia com a trajetória então ela não é conservativa.

4-



$$a) a_{cm} = 0$$

$$b) v_{cm} = \frac{m_A \cdot v_A + m_B \cdot v_B + m_C \cdot v_C}{m_A + m_B + m_C}$$

$$v_{cm} = \frac{0,50 \cdot 40 + 0,30 \cdot 38,24 + 0,20 \cdot 81,92}{0,50 + 0,30 + 0,20}$$

$$v_{cm} = 47,8 \text{ m/s}$$

$$c) x_{cm} = \frac{m_A \cdot x_A + m_B \cdot x_B + m_C \cdot x_C}{m_A + m_B + m_C}$$

$$x_{cm} = \frac{0,50 \cdot 0 + 0,30 \cdot 0 + 0,20 \cdot 0}{0,50 + 0,30 + 0,20}$$

$$x_{cm} = 0 \text{ m}$$