Euclid of Alexandria

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27th International Symposium of Prime Numbers

# Outline

#### 1. Motivation

1.1. The Basic Problem That We Studied

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# What Are Prime Numbers?

#### Definition

A prime number is a number that has exactly two divisors.

# Example

- 2 is prime (two divisors: 1 and 2).
- 3 is prime (two divisors: 1 and 3).
- 4 is not prime (three divisors: 1, 2, and 4).

The proof uses reductio ad absurdum

#### Theorem

There is no largest prime number.

#### **Proof**

1 Suppose p were the largest prime number.

The proof uses reductio ad absurdum

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- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.

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- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.
- Then q + 1 is not divisible by any of them.

The proof uses reductio ad absurdum

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#### Proof

- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.
- Then q + 1 is not divisible by any of them.
- But q + 1 is greater than 1, thus divisible by some prime number not in the first p numbers.

The proof used reductio ad absurdum.

# What's Still To Do?

- Answered Questions
  - How many primes are there?
- Open Questions
  - Is every even number the sum of two primes?

# An Algorithm For Finding Prime Numbers.

## Finding Prime Numbers

```
int main (void)
{
    std::vector<bool> is_prime (100, true);
    for (int i = 2; i < 100; i++)
        if (is_prime[i])
        {
            std::cout << i << "_";
            for (int j = i; j < 100; is_prime [j] = false, j+=i);
        }
    return 0;
}</pre>
```

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Note the use of std::.