## **Project**

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## Objective of the Project

Estimating responses of key macroeconomic variables to a noise shock.

#### Preview of the results:

- GDP, consumption, investment, and hours worked display a positive and hump-shaped response over the first 6-8 quarters.
- Inflation decreases

#### **Econometric Procedure - Overview**

We use a 2-step procedure

- Estimate series of noise shocks controlling for other possible source of fluctuations
- 2 Estimate IRFs via local projection à la Jorda (2005)

### Step 1 - Overview

We estimate a noise shock as a change in the expected future growth rate of real GDP which is orthogonal to

- contemporaneous structural shocks
- 2 lagged principal components from a large dataset
- past and future TFP

## Step 1 - Estimation of $Z_t$

#### Data

- $X_t$  is log of Real GDP at time t
- $X_{t+k|t} = E[X_{t+k}|I(t)]$  provided by Survey of Professional Forecasters

#### Procedure

$$Z_t = (X_{t+4|t} - X_{t|t}) - (X_{t+4|t-1} - X_{t|t-1})$$

where

- $(X_{t+4|t} X_{t|t})$  is expected growth rate of Real GDP conditional on information set up to time t
- $(X_{t+4|t-1} X_{t|t-1})$  is expected growth rate of Real GDP conditional on information set up to time t-1
- $Z_t$  is a shock to the expectations of output growth rate

# Step 1 - Estimation of $\widetilde{Z}_t$

**Problem.**  $Z_t$  is correlated with current and future fundamentals such as fiscal policy, monetary policy, current and future TFP.

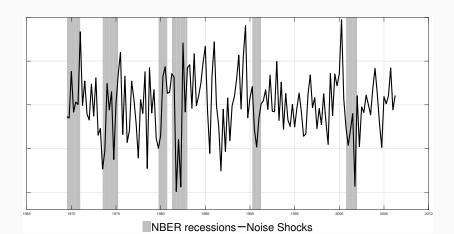
**Solution.** Estimate  $\tilde{Z}_t$  as follows

$$Z_{t} = C + \sum_{j=-J}^{H} \delta_{j} \Delta TFP_{t+j} + \gamma SS_{t} + \mu PC_{t-1} + \tilde{Z}_{t}$$

where

- C is a constant parameter
- ullet  $\Delta$   $TFP_t$  is first difference of utility-adjusted total factor productivity at time t
- SS<sub>t</sub> is a vector of structural shocks at time t possibly estimated via narrative approach
- $PC_{t-1}$  is a vector of principal component at time t-1

## Noise Shocks $\tilde{Z}_t$



## Step 2 - Estimation of IRFs to $\tilde{Z}_t$

Define  $Y_t$  to be the log-transformation of an endogenous aggregate macroeconomic variable.

Using standard OLS techniques we estimate H regressions

$$Y_{t+h} = C + \gamma T_t + \Theta_h^Y \tilde{Z}_t + \delta X_{t-1} + \epsilon_{t+h}$$

where

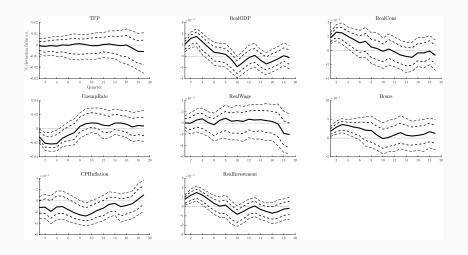
- h = 1, 2, ..., H represent the forecast horizon
- *C* is a constant parameter
- $T_t$  is a linear time trend
- $X_t$  is a vector of control variables at t-1: TFP, PC, ...

 $\Theta_1^Y$ ,  $\Theta_2^Y$ , ...,  $\Theta_H^Y$  represent the path of the impulse response function of  $Y_2$  to a unit deviation of  $\tilde{Z}_2$ 

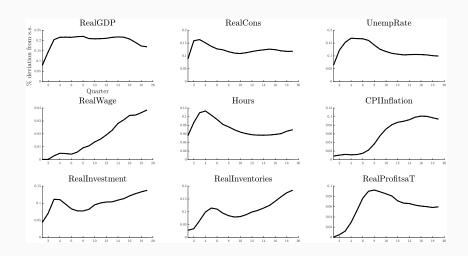
## **Bootstrapping Techniques**

- **1** Consider the tuple  $\Gamma_h^Y = \{Y_{t+h}, T_t, \tilde{Z}_t, X_{t-1}\}.$
- ② Divide  $\Gamma_h^Y$  over time t in smaller blocks and randomly reorder these blocks in order to form a new tuple  $\Gamma_{h,Boot1}^Y$  of the same size of the previous one.
- **3** Estimate  $\Theta_{h,Boot1}$  from  $\Gamma_{h,Boot1}^{Y}$  using standards OLS techniques.
- Redo (1)-(3) 2000 times and select confidence intervals.

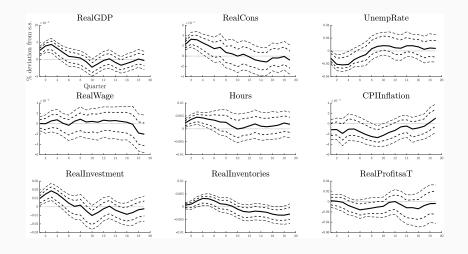
## Local Projection - Confidence Interval 68% and 90%



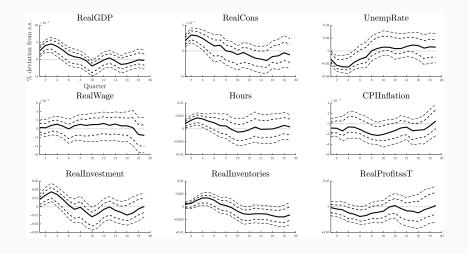
## Variance Explained



### Robustness Check 1 - Adding PCs and lags in both steps



### Robustness Check 2 - Adding PCs and lags in both steps



### **Consumer Price Index**

