

# Noise over the Business Cycle

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The key empirical question is how the effect of **noise** varies over the **business cycle**

We employ a **regime switching** econometric model where transitions across states (recession and expansion) are **smooth** to answer this question

We use a 2-step procedure

- 1 Estimate series of noise shocks orthogonal to any other exogenous source of fluctuations
- 2 Estimate a Smooth Transition Local Projection model (hereafter STLP) to estimate dynamic responses of key macroeconomic variables

# Step 1 - Overview

We estimate a noise shock as a change in the expected growth rate of Real GDP which is orthogonal to

- ① contemporaneous structural shocks
- ② lagged principal components from a large dataset
- ③ past and future TFP

# Step 1 - Estimation of $Z_t$

## Data

- $X_t$  is log of Real GDP at time  $t$
- $X_{t+k|t} = E[X_{t+k}|I(t)]$  provided by Survey of Professional Forecasters

## Procedure

$$Z_t = (X_{t+4|t} - X_{t|t}) - (X_{t+4|t-1} - X_{t|t-1})$$

where

- $(X_{t+4|t} - X_{t|t})$  is expected growth rate of Real GDP conditional on information set up to time  $t$
- $(X_{t+4|t-1} - X_{t|t-1})$  is expected growth rate of Real GDP conditional on information set up to time  $t - 1$
- $Z_t$  is a shock to the expectations of output growth rate

## Step 1 - Estimation of $\tilde{Z}_t$

**Problem.**  $Z_t$  is correlated with current and future fundamentals such as fiscal policy, monetary policy, current and future TFP.

**Solution.** Estimate  $\tilde{Z}_t$  as follows

$$Z_t = C + \sum_{j=-J}^H \delta_j TFP_{t+j} + \gamma SS_t + \mu PC_{t-1} + \tilde{Z}_t$$

where

- $C$  is the constant
- $TFP_t$  is total factor productivity at time  $t$
- $SS_t$  is a vector of structural shocks at time  $t$
- $PC_{t-1}$  is a vector of principal component at time  $t - 1$

$\tilde{Z}_t$  represents a change expectation which is not related to any source of fundamental fluctuations, i.e. a **noise shock**.

## Step 2 - Smooth Transition Local Projection

Following Auerbach and Gorodnichenko (2012), our basic specification is

$$Y_{t+k} = [1 - F(\eta_{t-1})]\Pi_E \tilde{Z}_t + F(\eta_{t-1})\Pi_R \tilde{Z}_t + u_t$$

where

$$F(\eta_t) = \frac{\exp(-\gamma\eta_t)}{1 + \exp(-\gamma\eta_t)}, \quad \gamma > 0$$

and variables  $\eta_t$  is an index (normalized to have zero mean and unit variance) of the business cycle. [ $\eta_t > 0 \Rightarrow$  expansion.]

**Note.** We date the index  $\eta$  by  $t - 1$  to avoid contemporaneous feedbacks of  $\tilde{Z}_t$  on the underlying state.





# Details on $\eta_t$ and STPL procedure

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