Replication of 'The Likelihood of Mixed Hitting Times'
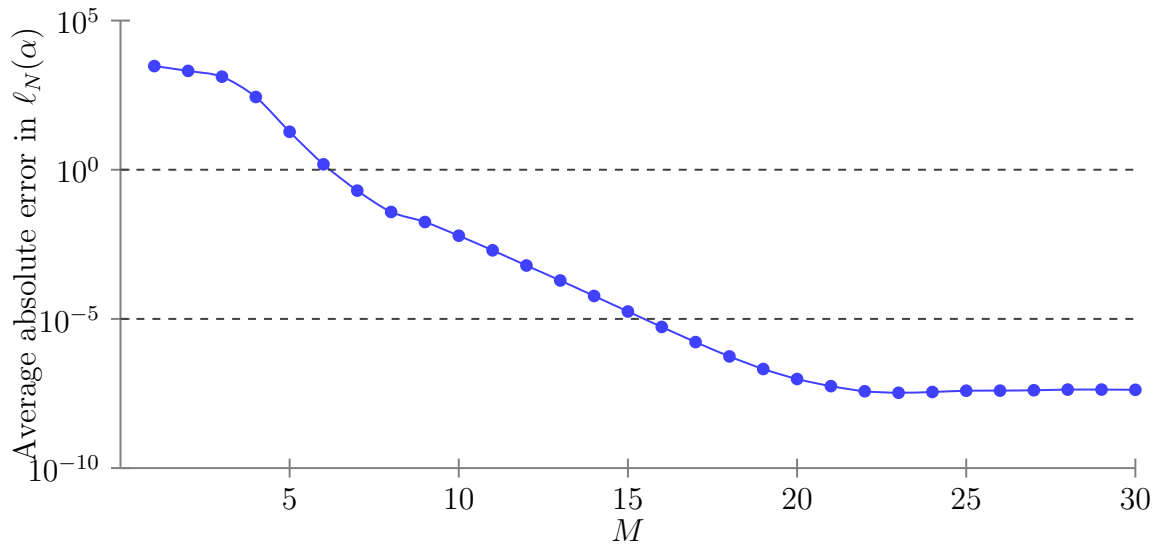
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This document reports on the replication of Abbring and Salimans (2021a). It was generated by running `make` *in the replication package (Abbring and Salimans, 2021b).*

1 Main Results

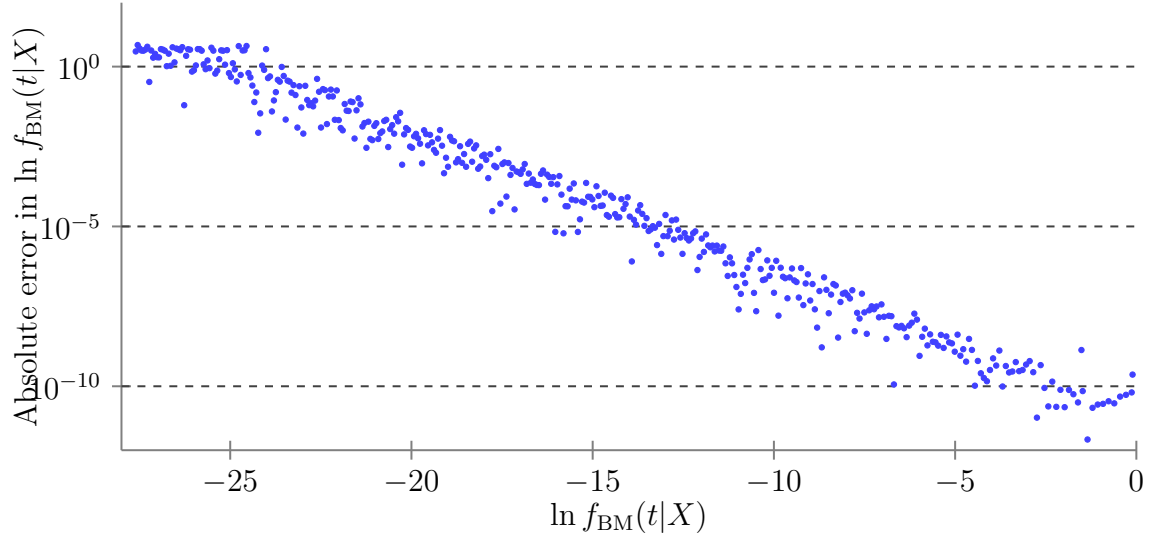Figure 1: Approximation Error of the Log Likelihood for Various M

Figure 2: Approximation Error of the Log Inverse Gaussian Density Function

Note: Mean calculation times are $3.45924e-04$ seconds (analytical) and $5.58742e-03$ seconds (numerical inversion), so that mean time numerical $= 16.15\times$ mean time analytical

Figure 3: Approximate Probability Density and Histogram of Simulated Values of $\ln T$ for a Specification With Shocks and Heterogeneity
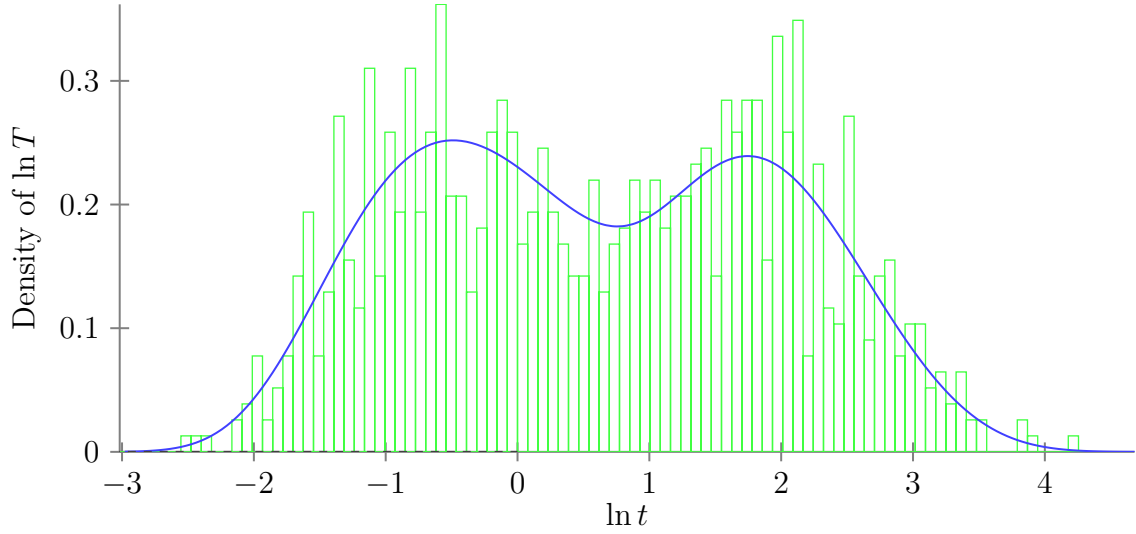
Table 1: Maximum Likelihood Estimates for Kennan's (1985) Strike Duration Data

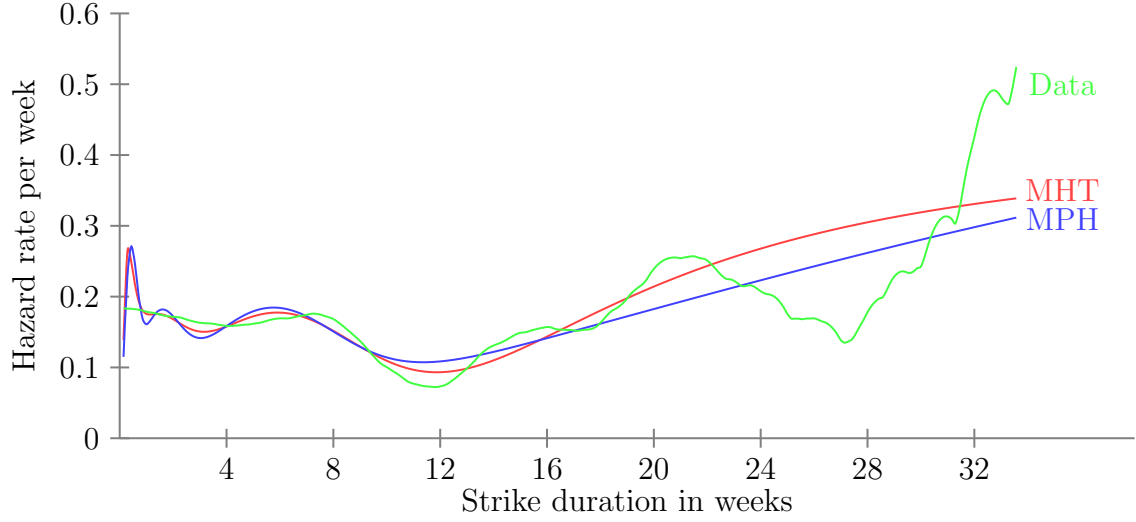|	I	II	III	IV	V	VI
μ	1	1	1	1	1	1
	(0)	(0)	(0)	(0)	(0)	(0)
σ^2	19.659	6.219	2.067	1.227	1.197	0.542
	(3.951)	(0.888)	(0.376)	(0.387)	(0.479)	(0.165)
λ						0.019
						(0.017)
ν						-5.132
						(2.412)
β	-0.931	-1.772	-1.085	-0.867	-0.862	-0.579
	(0.828)	(0.714)	(0.696)	(0.617)	(0.979)	(0.688)
v_1	6.260	2.543	1.537	1.105	1.031	0.755
	(0.543)	(0.211)	(0.134)	(0.200)	(0.531)	(0.113)
v_2		8.751	5.888	3.209	1.756	2.083
		(0.525)	(0.382)	(0.750)	(1.804)	(0.526)
v_3			18.161	7.165	3.518	4.138
			(1.007)	(0.711)	(0.937)	(0.859)
v_4				18.557	7.303	7.412
				(0.712)	(0.739)	(0.563)
v_5					18.575	17.004
					(0.838)	(0.885)
π_1	1.000	0.399	0.353	0.252	0.199	0.198
	(0.000)	(0.043)	(0.034)	(0.052)	(0.301)	(0.041)
π_2		0.601	0.492	0.283	0.098	0.201
		(0.043)	(0.035)	(0.053)	(0.346)	(0.066)
π_3			0.154	0.315	0.256	0.223
			(0.022)	(0.075)	(0.087)	(0.062)
π_4				0.151	0.297	0.238
				(0.019)	(0.095)	(0.058)
π_5					0.150	0.140
					(0.020)	(0.020)
ℓ_N	-1658.9	-1588.7	-1583.0	-1576.3	-1576.1	-1575.4

Note: The drift is normalized to 1 per week. All specifications include a single covariate, Kennan's (1985) deseasonalized and detrended log industrial production. Asymptotic standard errors are in parentheses.

Table 2: Replication of Table 1 with $M = 15$

	I	II	III	IV	V	VI
μ	1	1	1	1	1	1
	(0)	(0)	(0)	(0)	(0)	(0)
σ^2	19.659	6.219	2.067	1.227	1.197	0.541
	(3.247)	(0.898)	(0.354)	(0.184)	(0.183)	(0.187)
λ						0.019
						(0.018)
ν						-5.113
						(2.398)
β	-0.931	-1.772	-1.085	-0.867	-0.862	-0.579
	(0.606)	(0.719)	(0.636)	(0.597)	(0.666)	(0.616)
v_1	6.260	2.543	1.537	1.104	1.031	0.754
	(0.476)	(0.197)	(0.131)	(0.108)	(0.167)	(0.117)
v_2		8.751	5.888	3.209	1.756	2.083
		(0.516)	(0.380)	(0.455)	(1.037)	(0.506)
v_3			18.161	7.165	3.518	4.138
			(1.013)	(0.560)	(0.778)	(0.840)
v_4				18.557	7.303	7.410
				(0.699)	(0.654)	(0.550)
v_5					18.575	16.997
					(0.691)	(0.959)
π_1	1.000	0.399	0.353	0.252	0.199	0.198
	(0.000)	(0.044)	(0.034)	(0.039)	(0.114)	(0.039)
π_2		0.601	0.492	0.283	0.098	0.201
		(0.044)	(0.034)	(0.050)	(0.132)	(0.068)
π_3			0.154	0.315	0.256	0.223
			(0.022)	(0.053)	(0.084)	(0.060)
π_4				0.151	0.297	0.238
				(0.019)	(0.066)	(0.060)
π_5					0.150	0.140
					(0.019)	(0.020)
ℓ_N	-1658.9	-1588.7	-1583.0	-1576.3	-1576.1	-1575.4

Note: The drift is normalized to 1 per week. All specifications include a single covariate, Kennan's (1985) deseasonalized and detrended log industrial production. Asymptotic standard errors are in parentheses.

Figure 4: Aggregate Strike End Hazard Rates

The numbers in Column IV imply that there are four unobserved types of labor conflict, on average commanding respectively 1.1, 3.2, 7.2, and 18.6 strike weeks.

Computation times (in seconds):

I	II	III	IV	V	VI
0.9	1.3	3.0	4.3	12.8	24.6

Both the MHT and the MPH models fit the empirical hazard well, but the MPH model's log likelihood, at -1577.9, is 1.6 points lower.

2 Other Checks

Table R1: Analytical and Numerical Gradients MHT

63.109743	63.133264
−24.600649	−24.604226
−10.666863	−10.668835
31.395502	31.392171
−16.443511	−16.447705
−63.825155	−63.827932
3.959228	3.956069
44.661001	44.663154
−62.913234	−62.910462
33.435364	33.440150
26.771924	26.768178
27.405938	27.402772
1.711623	1.714859

Table R2: Analytical and Numerical Gradients MPH

0.000095	0.000095	−521.944454	−521.944454
−0.000002	−0.000002	4.234742	4.234743
0.000014	0.000014	−71.661453	−71.661453
0.000007	0.000007	−8.757202	−8.757202
0.000001	0.000001	10.686492	10.686492
0.000002	0.000002	5.471933	5.471933
−0.000010	−0.000010	50.583811	50.583811
−0.000002	−0.000002	−42.823964	−42.823964
0.000002	0.000002	−1.252138	−1.252138

References

Abbring, J. H. and T. Salimans (2021a). The likelihood of mixed hitting times. *Journal of Econometrics XX*, forthcoming. arXiv:1905.03463 [econ.EM].

Abbring, J. H. and T. Salimans (2021b). The likelihood of mixed hitting times: Replication package. doi:10.5281/zenodo.4287734.

Kennan, J. (1985). The duration of contract strikes in U.S. manufacturing. *Journal of Econometrics 28*, 5–28.