

Oblig 1, Sanders

Komment

Since we did not have lectures in crossvalidation, a person asked the teacher what we should do with these tasks, and the teacher's answer was that we will not need to do them. So this is my solution for the oblig, where I have not completed what was needed from the delayed lecture. If it is not approved I will do the tasks.

Problem 1

```
# Getting data
res_bodyfat <- read.csv("res_bodyfat/res_bodyfat.csv")
attach(res_bodyfat)
```

Aim: Find how well bmi, easily computed as the ratio between weight and squared height (so measured in kg/m^2), can be used to predict pbfm, whose measurement involves instead a bioelectrical impedance analysis.

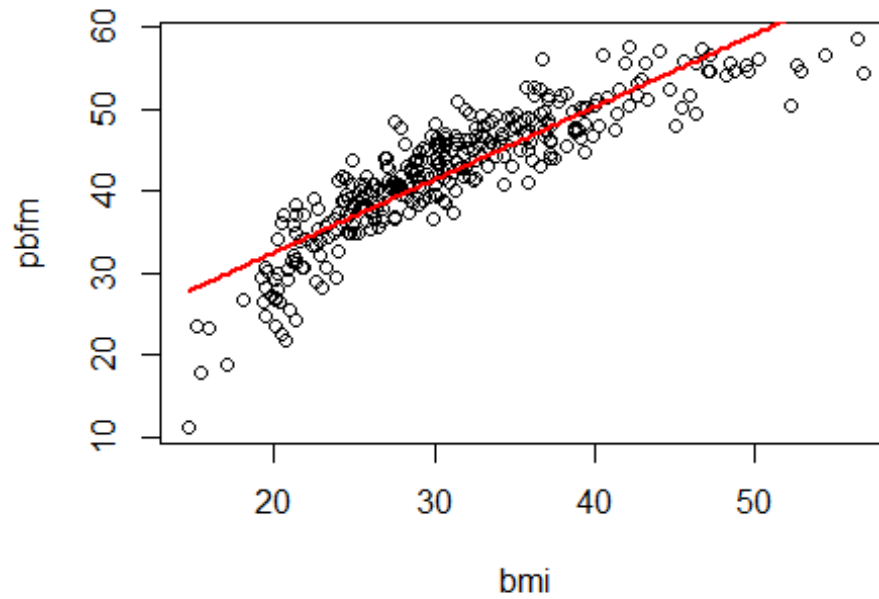
a

Plotting **bmi** against **pbfm**, and fitting a simple linear model with a summary.

```
plot(bmi, pbfm)
fit.simpleLinear <- lm(pbfm ~ bmi)
print(summary(fit.simpleLinear))

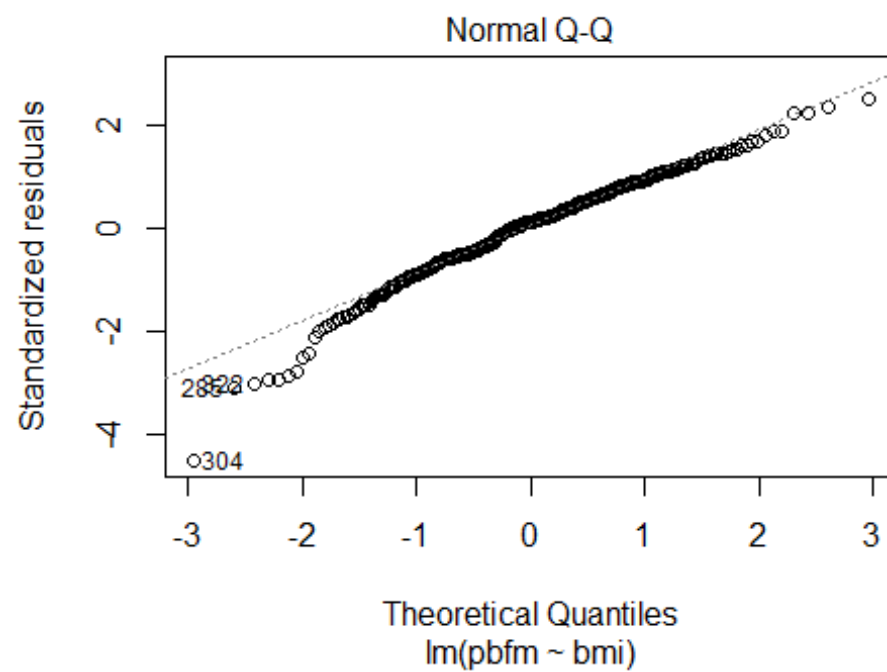
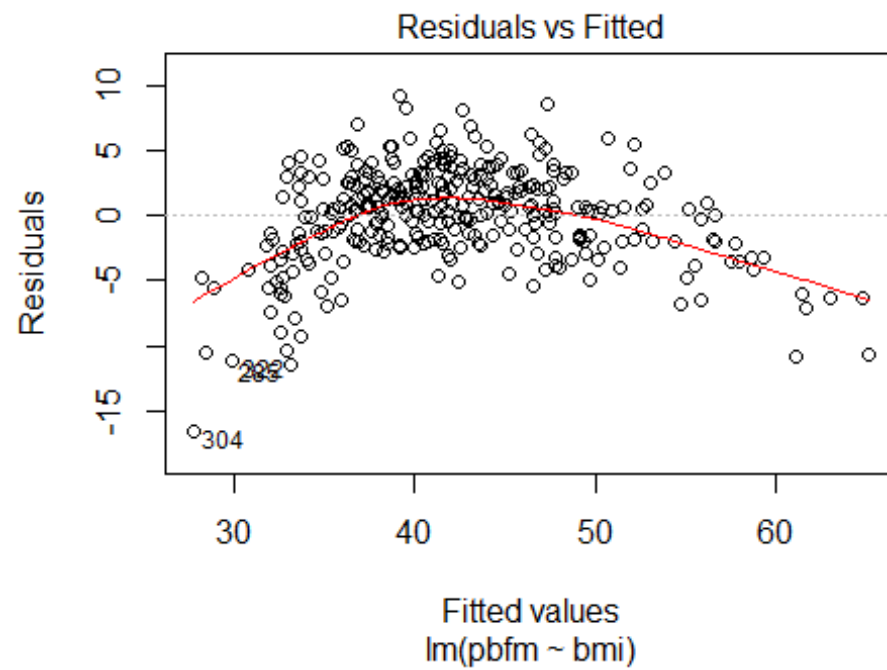
##
## Call:
## lm(formula = pbfm ~ bmi)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -16.5116  -2.0714   0.4083   2.4994   9.1758
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  14.82772    0.82671   17.94  <2e-16 ***
## bmi          0.88481    0.02589   34.17  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.702 on 325 degrees of freedom
## Multiple R-squared:  0.7823, Adjusted R-squared:  0.7816
## F-statistic: 1168 on 1 and 325 DF, p-value: < 2.2e-16
```

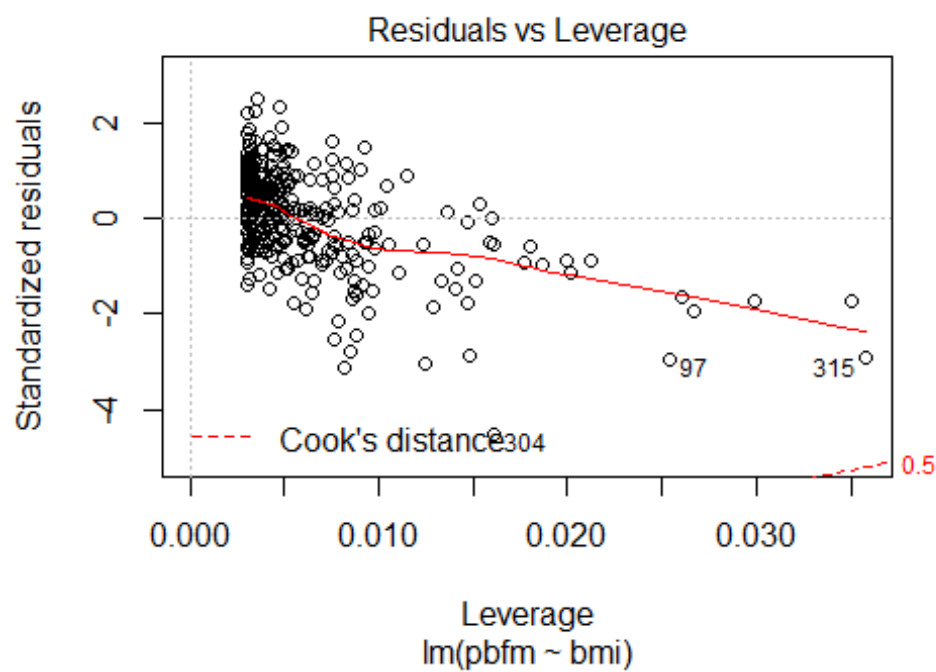
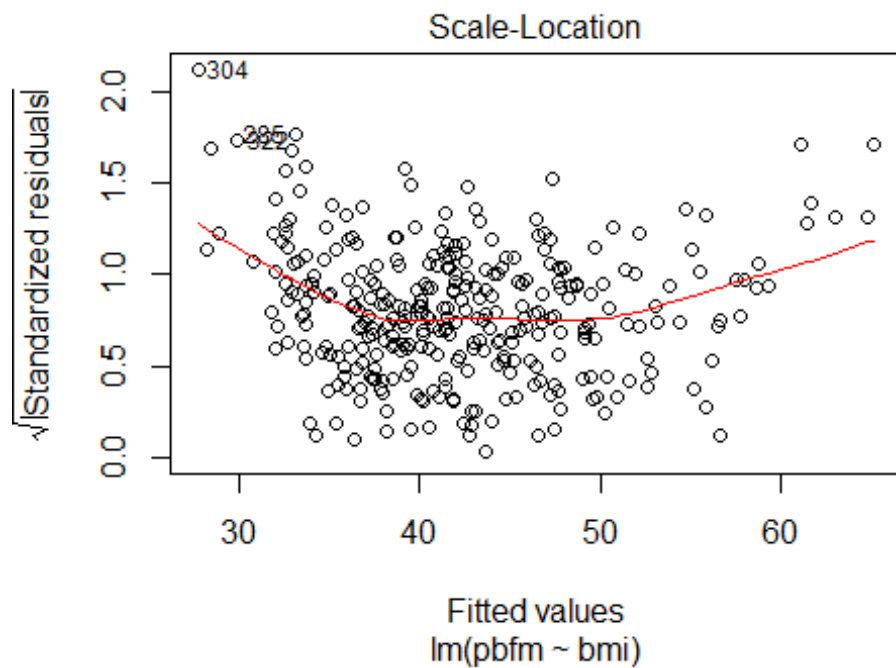
```
x = (seq(min(bmi), max(bmi), length = 200))
beta = coef(fit.simpleLinear)
lines(x, beta[1] + beta[2]* x, col = 2, lty = 1, lwd = 2)
```



A linear model seems ok in the center of the bmi. But it is quite off in the lower 1/4 and in the upper 1/4. We can see that the intercept and bmi is strongly significant, indicating a strong correlation between bmi and pbfm. The R-squared is significant, but not super high, so the model can probably be improved. To see this clearly we plot indicative plots on the fitness.

```
plot(fit.simpleLinear)
```





Residuals vs Fitted

Shows the Anscombe plot, which would ideally present an even scattering with no patterns in the points. In the plot we see a clear pattern, and is indicating possible violation of homoscedasticity. Meaning that must be independent of the index.

Normal Q-Q

This plot shows quantile-quantile plot. This plot shows the values of the residuals in increasing order. To see if the residuals follow a normal distribution. For the assumption of normality to be valid we would expect the values to follow the line in the plot. In the plot a heavy tail and head can be observed. So the assumption of normality is not strong.

Scale-Location

Residual vs Leverage

b

We can see that we don't have any negative number, in such cases it is often beneficial to use a logarithmic transformation.

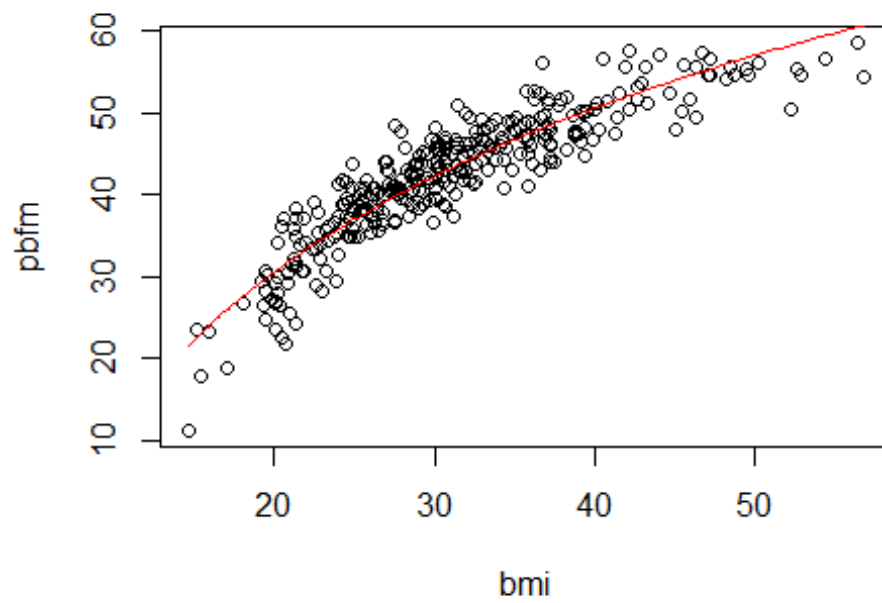
```
fit.log <- lm(pbfm ~ log(bmi))
print(summary(fit.log))

##
## Call:
## lm(formula = pbfm ~ log(bmi))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.2548  -2.0453   0.1026   2.1238   8.6029
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -55.7327     2.3337  -23.88  <2e-16 ***
## log(bmi)      28.8031     0.6845   42.08  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.125 on 325 degrees of freedom
## Multiple R-squared:  0.8449, Adjusted R-squared:  0.8444
## F-statistic: 1771 on 1 and 325 DF,  p-value: < 2.2e-16

beta = coef(fit.log)

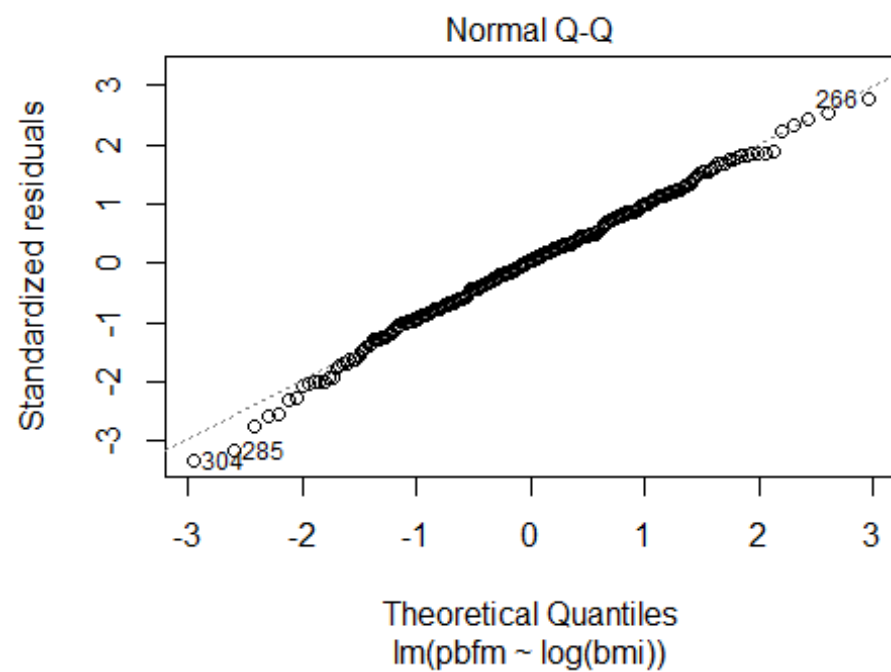
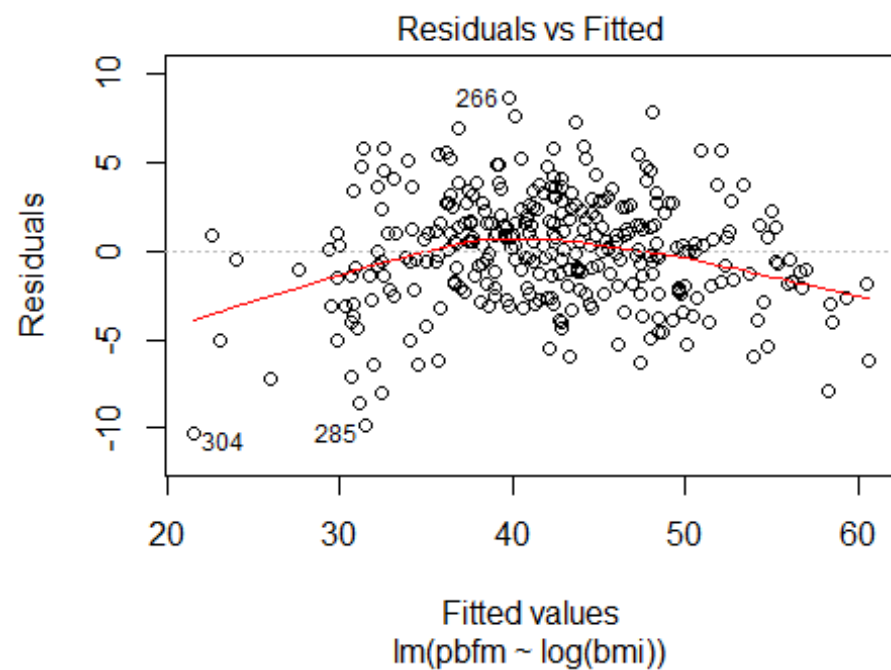
x = log(seq(min(bmi), max(bmi), length = 200))
plot(bmi, pbfm)

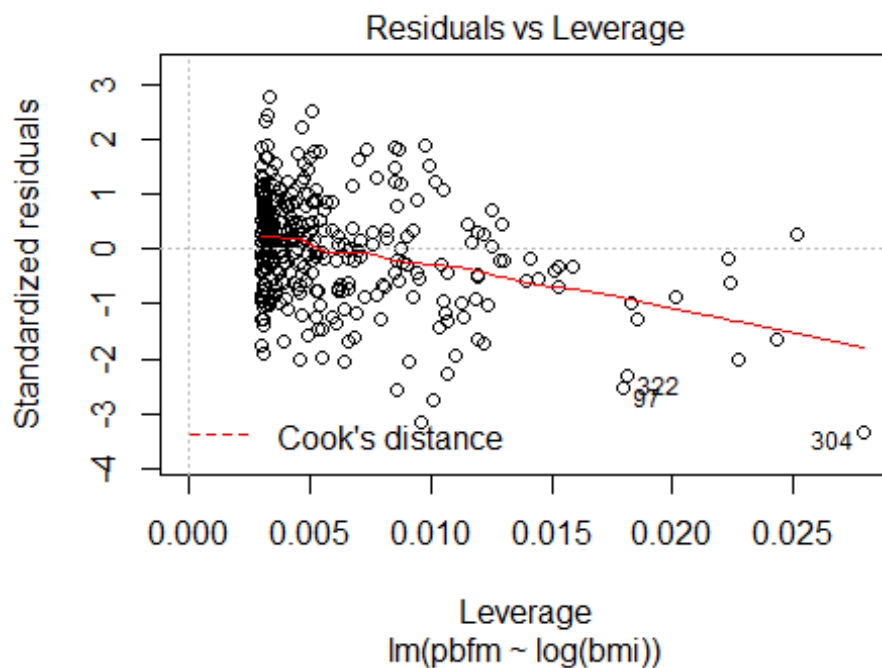
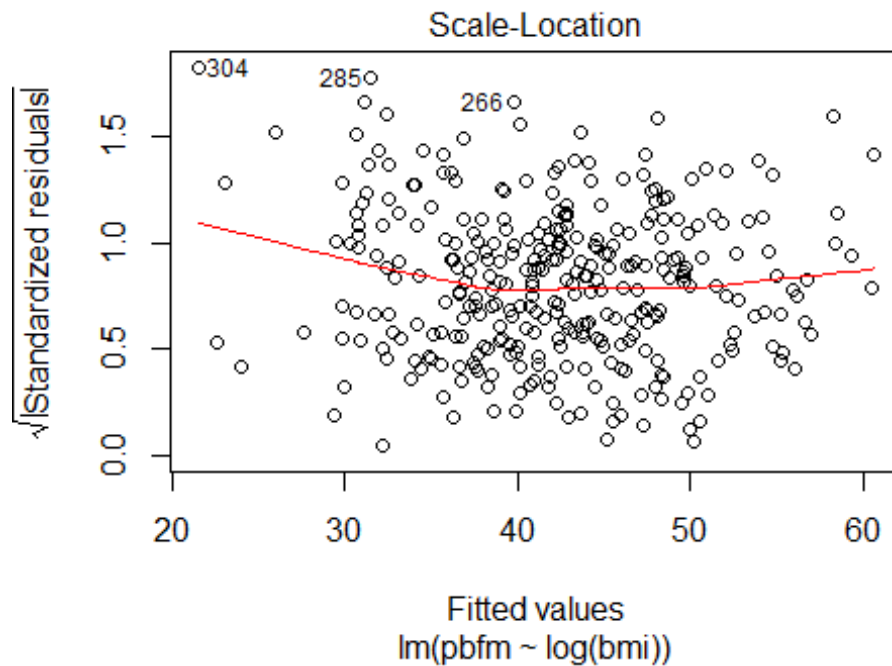
lines(exp(x), (beta[1] + beta[2]* x), col = 2)
```



And to see how good the model is we plot some helping plots

```
plot(fit.log)
```





It was also suggested to use a quadratic model.

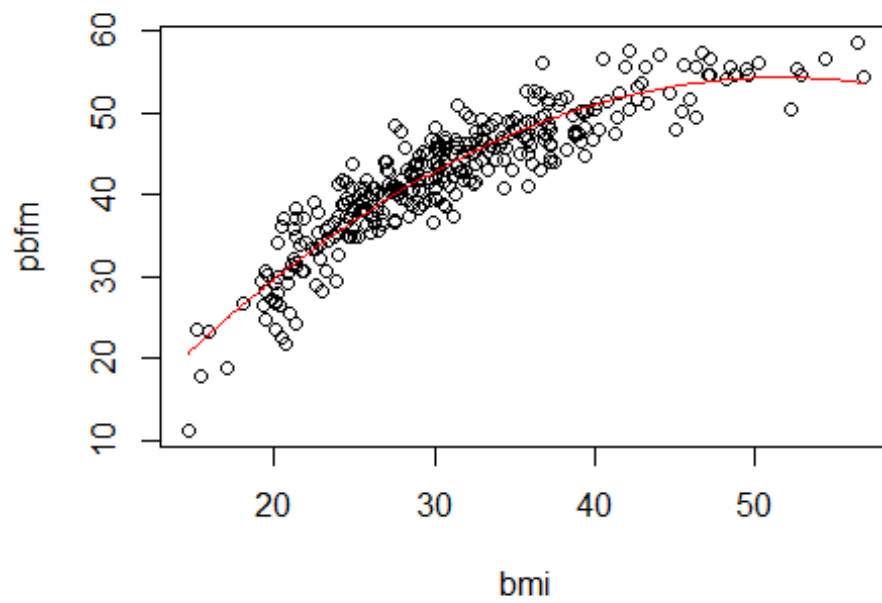
```
fit.quad<- lm(pbfm ~ bmi + I(bmi^2))
print(summary(fit.quad))
```



```
##
## Call:
## lm(formula = pbfm ~ bmi + I(bmi^2))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.3403 -1.9246  0.1433  1.8665  8.3780
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -11.17790    2.16977  -5.152 4.49e-07 ***
## bmi          2.53223    0.13229  19.142 < 2e-16 ***
## I(bmi^2)     -0.02448    0.00194 -12.617 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.036 on 324 degrees of freedom
## Multiple R-squared:  0.854, Adjusted R-squared:  0.8531
## F-statistic: 947.8 on 2 and 324 DF, p-value: < 2.2e-16

beta = coef(fit.quad)

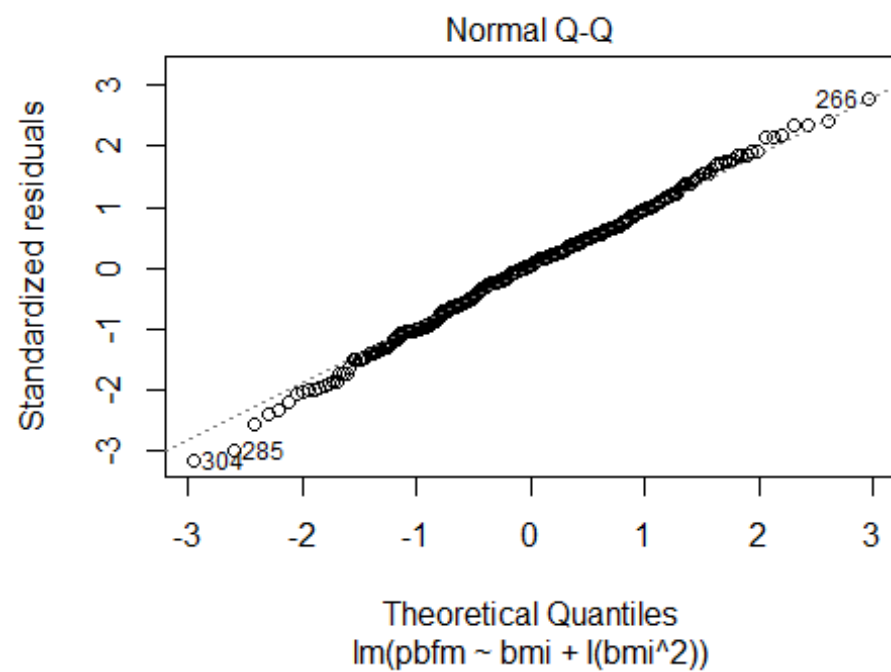
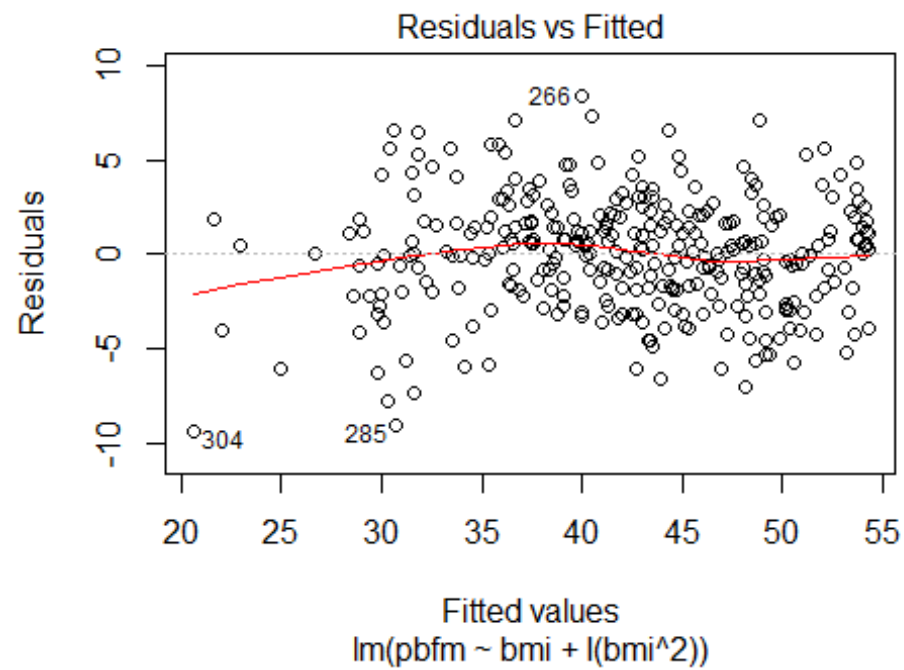
x = (seq(min(bmi), max(bmi), length = 200))
plot(bmi, pbfm)
#points(bmi, pbfm)
lines(x, beta[1] + beta[2]*x + beta[3]*x^2, col=2)
```

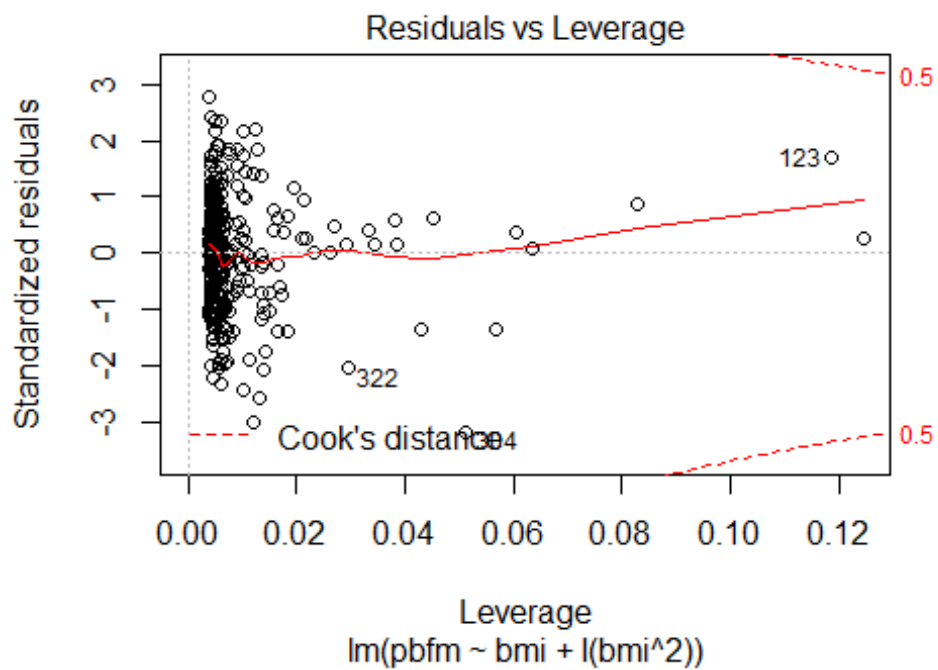
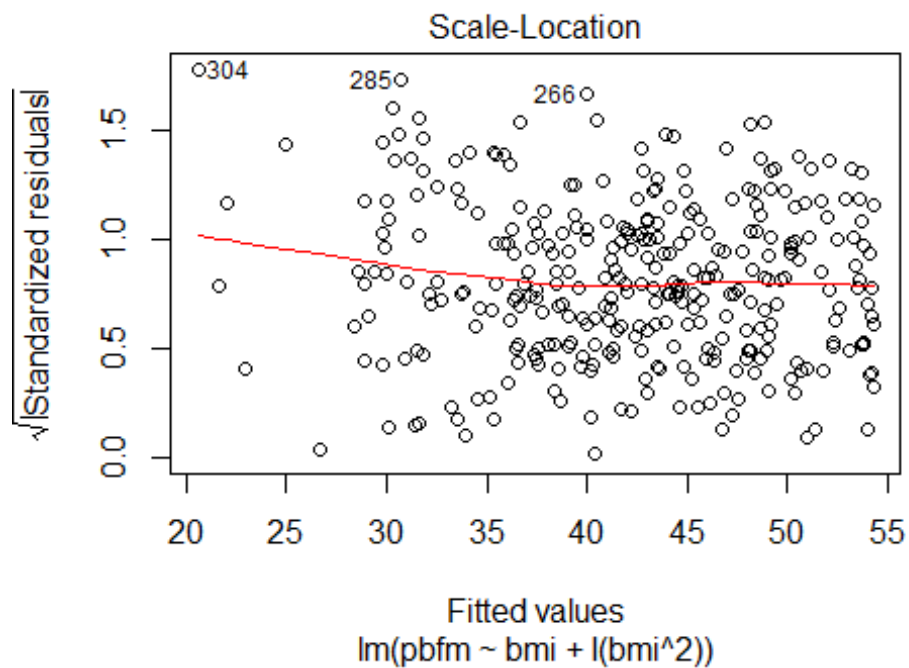


And the acopening

helping plots

```
plot(fit.quad)
```





C - Leave-p-out cross-validation ([https://en.wikipedia.org/wiki/Cross-validation_\(statistics\)](https://en.wikipedia.org/wiki/Cross-validation_(statistics)))

```
#max.p = 10 #n = 4 # n = len bmi #shuffled = sample(1:length(bmi)) #subset.size =
length(bmi) %% n #indices<-matrix(list(), nrow=n, ncol=1) # indices[[1,1]] =
shuffled[1:subset.size] # indices[[2,1]] = shuffled[subset.size + 1:subset.size*2] #
indices[[3,1]] = shuffled[(subset.size*2 + 1):subset.size*3] # indices[[4,1]] =
shuffled[(subset.size*3 + 1):length(bmi)]

#for(i in 0:n-1){ # a = (subset.size*i) + 1 # b = subset.size(i+1) # print(c(a,b)) #
indices[[i+1,1]] = shuffled[a : b] #}

#for (i in 1:max.p){ # for(j in 0:n){ # x = bmi[c(indices[[j %% n]], indices[[j+1] %% n]],
indices[[j+2] %% n]] # y = pbfm[c(indices[[j %% n]], indices[[j+1] %% n]],
indices[[j+2] %% n]] # fit = lm(pbfm ~ poly(x, i), x = TRUE) # x.test = bmi[i] # } #}
```

Problem 2

```
oral_ca <- read.csv("oral_ca/oral_ca.csv")
attach(oral_ca)
print(summary(oral_ca))
```

```
##      drinks      ccstatus      cigs      age
## Min.   : 0.00   Min.   :0.0000   Min.   : 0.00   Min.   :21
## 1st Qu.: 1.50   1st Qu.:0.0000   1st Qu.: 3.00   1st Qu.:48
## Median :15.75   Median :0.0000   Median :20.00   Median :56
## Mean   :31.40   Mean   :0.4887   Mean   :16.36   Mean   :56
## 3rd Qu.:48.00   3rd Qu.:1.0000   3rd Qu.:20.00   3rd Qu.:65
## Max.   :140.00   Max.   :1.0000   Max.   :60.00   Max.   :80
##      sex      M_drinks      M_cigs
## Min.   :0.0000   Min.   :0.000000   Min.   :0.00000
## 1st Qu.:0.0000   1st Qu.:0.000000   1st Qu.:0.00000
## Median :0.0000   Median :0.000000   Median :0.00000
## Mean   :0.2771   Mean   :0.005038   Mean   :0.01511
## 3rd Qu.:1.0000   3rd Qu.:0.000000   3rd Qu.:0.00000
## Max.   :1.0000   Max.   :1.000000   Max.   :1.00000
```

Aim of the study was to evaluate the risk of Oral cancer based on the variables **drinks** (number of 1oz ethanol-equivalent drinks consumed per week), **sex**, **age** and **cigs** (number of cigarettes smoked per day).

We are first interested in the effect of smoking alone

(a)

Q:

Dichotomize the variable cigs in two categories, smokers and not smokers, and create a table with the observed frequencies for cases and controls. In addition, provide the

estimated probabilities (including their standard errors) of experiencing an oral cancer (i.e., being a case) for the two sub-populations.

A:

```
N = length(oral_ca$ccstatus)
smoker.nonSmoker = cigs == 0
smokers = subset( oral_ca, oral_ca$cigs > 0 )#smokers = oral_ca[ oral_ca$cigs
> 0]
nonSmokers = subset(oral_ca, oral_ca$cigs == 0) # nonSmokers = oral_ca[ oral
_ca$cigs == 0 ]
number.of.cc = nrow( subset(oral_ca,oral_ca$ccstatus == 1) )
number.of.cc.smokers = nrow( subset(oral_ca, oral_ca$ccstatus == 1 & oral_ca$
cigs > 0) )
number.of.cc.nonSmokers = nrow(subset(oral_ca, oral_ca$ccstatus == 1 & oral_c
a$cigs == 0) )
n.smoker = nrow( subset( oral_ca, oral_ca$cigs > 0) )
n.nonSmoker = nrow( subset( oral_ca, oral_ca$cigs == 0 ))

# Binomial - Mean
pi.common.hat = number.of.cc / N # Number of ppl with cancer devided on ppl (
people in the query )
pi.smoker.hat = number.of.cc.smokers / n.smoker # Number of ppl with cancer a
nd smokes, devided on number of ppl who smokes.
pi.nonSmoker.hat = number.of.cc.nonSmokers / n.nonSmoker# Number of ppl with
cancer and does not smoke, devided on number of ppl who does not soke.

# Binomial Vairance - Var(X) = n*p*(1-p)
se.pi.common = sqrt(pi.common.hat * (1 - pi.common.hat) / N)
se.pi.smoker = sqrt(pi.smoker.hat * (1 - pi.nonSmoker.hat) /n.smoker)
se.pi.nonSmoker = sqrt(pi.nonSmoker.hat * (1 - pi.nonSmoker.hat) /n.nonSmoker
)

cc.smoke.df = data.frame(
  pi = c(pi.common.hat, pi.smoker.hat, pi.nonSmoker.hat),
  se = c(se.pi.common, se.pi.smoker, se.pi.nonSmoker),
  row.names = c("General", "Smoker", "NonSmoker")
)
```

(b)

Q:

Test the hypothesis that the two probabilities are equal and comment on the result.

A:

Hypothesis: H0: probSmokers == probNonSmokers against H1: probSmokers != probNonSmokers. Computing the p-value

```
# compute the likelihood ratio statistics test
llik_pi.smoker.hat_pi.nonSmoker.hat = sum(dbinom(smoker.nonSmoker[ smoker.non
Smoker == TRUE], 1, pi.smoker.hat, log = TRUE)) +
sum(dbinom(smoker.nonSmoker[ smoker.non
Smoker == FALSE], 1, pi.nonSmoker.hat, log = TRUE))
llik_pi.common.hat = sum(dbinom(smoker.nonSmoker, 1, pi.common.hat, log=TRUE)
)

w = 2 * (llik_pi.smoker.hat_pi.nonSmoker.hat - llik_pi.common.hat)
p.val = 1 - pchisq(w, df = 1)
```

We can see that the p-val is zero, so we can drop H0.

(c)

Q:

Fit a linear logistic model using the dichotomized variable as explanatory variable and comment on the result: does being a smoker increase or decrease the risk of experiencing oral cancer? How much, in terms of log-odds?

A:

```
y = oral_ca$ccstatus == 1
x = oral_ca$cigs > 0

mod = glm(y ~ x, family = 'binomial')
print(summary(mod))

##
## Call:
## glm(formula = y ~ x, family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.285  -1.285  -0.744   1.073   1.685
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.1431     0.2448  -4.669 3.03e-06 ***
## xTRUE         1.3927     0.2706   5.147 2.65e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 520.14  on 395  degrees of freedom
## AIC: 524.14
##
## Number of Fisher Scoring iterations: 4
```

```

beta = mod$coefficients
print(beta)

## (Intercept)          xTRUE
## -1.143064      1.392719

pi.nonSmoker = exp(beta[1]) / (1 + exp(beta[1]))
pi.smoker = exp(beta[1] + beta[2]) / (1 + exp(beta[1] + beta[2]))

#odds
odds.nonSmoker = pi.nonSmoker.hat / (1 - pi.nonSmoker.hat)
odds.smoker = pi.smoker.hat / (1 - pi.smoker.hat)
#Log odds ratio
log.odds.ratio = (odds.smoker / odds.nonSmoker)

log.odds.ratio

## [1] 4.02578

```

We see that the odds of cc for a smoker against a non smoker is approx 4, aka. 4 to 1.

(d)

Q:

Repeat the analysis of point (c) by considering, now, the number of cigarettes as a continuous variable. Comment on the result: What does the regression coefficient for this variable mean now? Why does the value of the intercept change with respect to point (c), although they are both related to the odds for non-smokers?

A:

```

x = cigs
y = ccstatus
mod.continuous = glm(y ~ x, family = 'binomial')
print(summary(mod.continuous))

##
## Call:
## glm(formula = y ~ x, family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.1923  -1.0237  -0.8228   1.1088   1.5796
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.909057   0.171766  -5.292 1.21e-07 ***
## x            0.053624   0.008614   6.225 4.81e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```



```
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 504.39  on 395  degrees of freedom
## AIC: 508.39
##
## Number of Fisher Scoring iterations: 4
```

The regression coefficient now tells us the increase in odds of cancer per cigarets smoked per day. The intercept is changed since smoking one sigaret per day is closer to zero than smoking 20. In the non continius model the biggest smoker and the rest is given the same odds.

Consider now the other three variables (drinks, sex and age) as well:

(e)

Q:

Fit a linear logistic model including all the explanatory variables and report the result. What is the increase in terms of log-odds for an increasing number of cigarettes per day smoked estimated by this model? Why did it change from the one obtained in model fitted in point (c)?

```
mod.all = glm(y ~ oral_ca$drinks + oral_ca$cigs + oral_ca$age + oral_ca$sex,
family = 'binomial')
print(summary(mod.all))

##
## Call:
## glm(formula = y ~ oral_ca$drinks + oral_ca$cigs + oral_ca$age +
##      oral_ca$sex, family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.7185  -0.8589  -0.5832   0.9644   1.9776
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.966071   0.620756  -3.167  0.00154 **
## oral_ca$drinks  0.029623   0.004643   6.380 1.77e-10 ***
## oral_ca$cigs    0.035480   0.009571   3.707  0.00021 ***
## oral_ca$age     0.006529   0.009960   0.656  0.51213
## oral_ca$sex     0.594499   0.272752   2.180  0.02928 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
```

```
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 443.84  on 392  degrees of freedom
## AIC: 453.84
##
## Number of Fisher Scoring iterations: 5
```

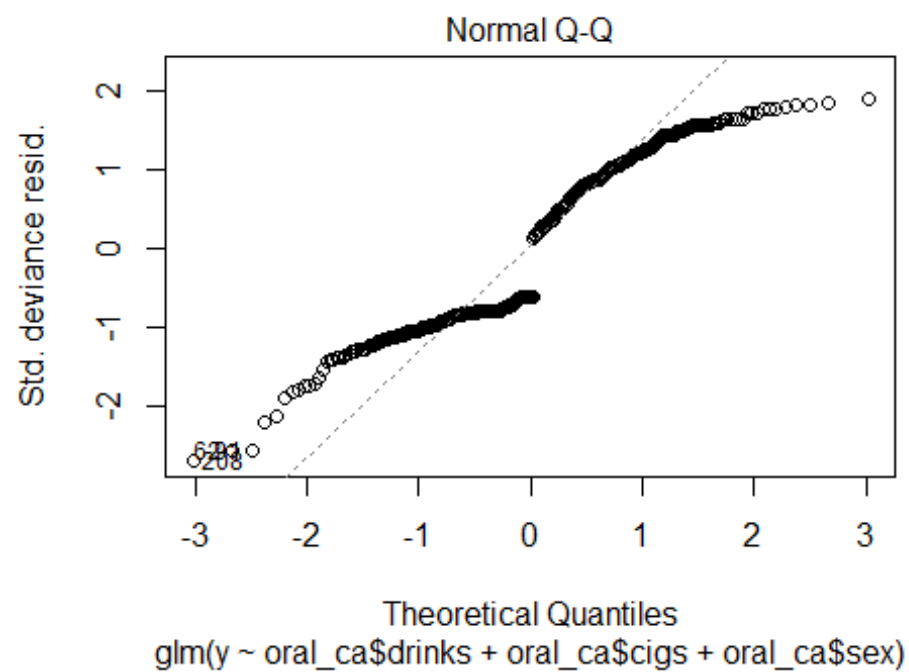
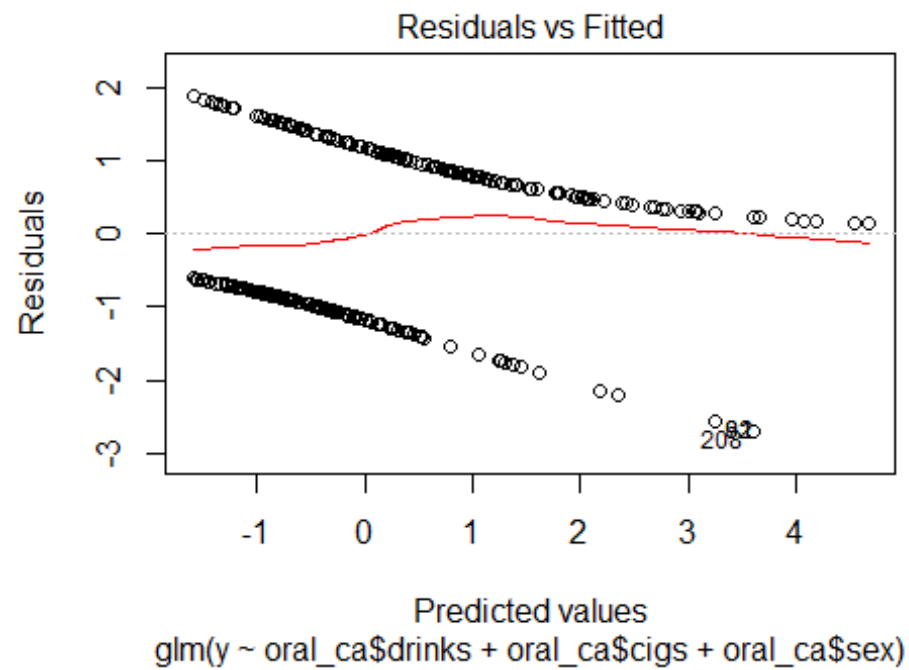
The increase in terms of log-odds for an increasing number of cigarettes per day by this model is 0.035, which is a little lower than in the previous model. This can be because of some of the effects of other factors was tried explained by one factor. Now we have other factors to explain this change. Which will change the value.

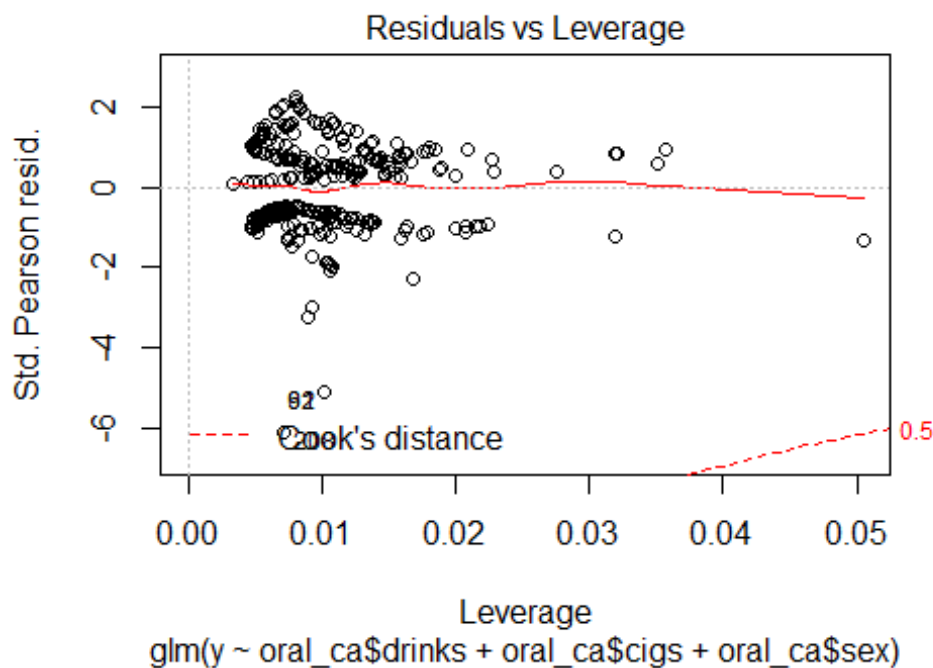
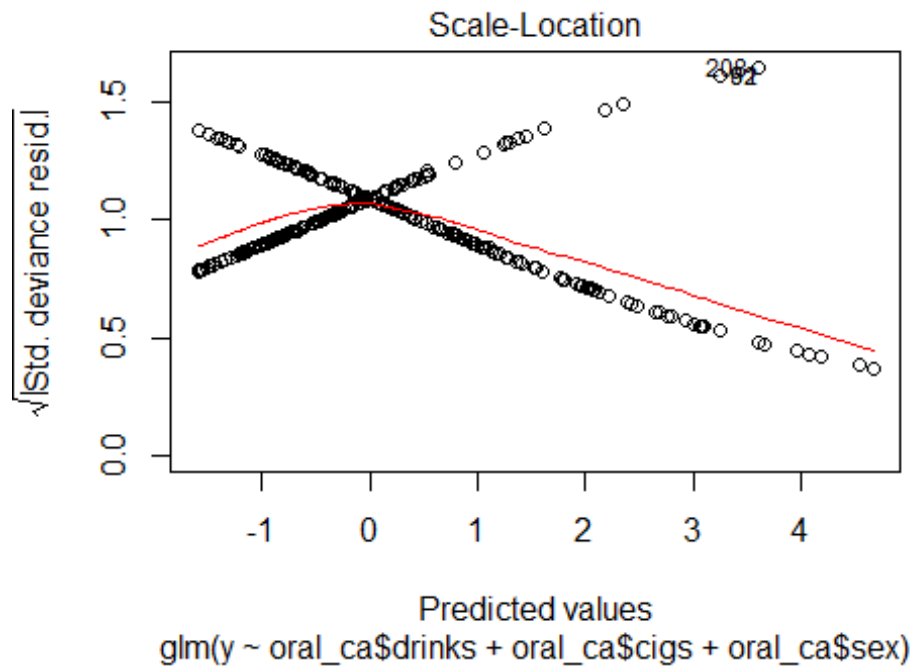
(e)

```
mod.without.Age = glm(y ~ oral_ca$drinks + oral_ca$cigs + oral_ca$sex, family = 'binomial')
print(summary(mod.without.Age))

##
## Call:
## glm(formula = y ~ oral_ca$drinks + oral_ca$cigs + oral_ca$sex,
##      family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.6943  -0.8596  -0.6084   0.9607   1.8857
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.592919   0.238787  -6.671 2.54e-11 ***
## oral_ca$drinks  0.029498   0.004638   6.360 2.01e-10 ***
## oral_ca$cigs    0.035536   0.009565   3.715 0.000203 ***
## oral_ca$sex     0.582183   0.271756   2.142 0.032169 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 444.27  on 393  degrees of freedom
## AIC: 452.27
##
## Number of Fisher Scoring iterations: 5

plot(mod.without.Age)
```





Since the explanatory variable age has a large p-value can we not say it gives significant value to the model. So it does not seem like there is a difference in age. Lookin at the deviance the age variable did noting significant for the model ether. So i would choose the one with less explanatory variables, aka the one without Age

(g)

Q:

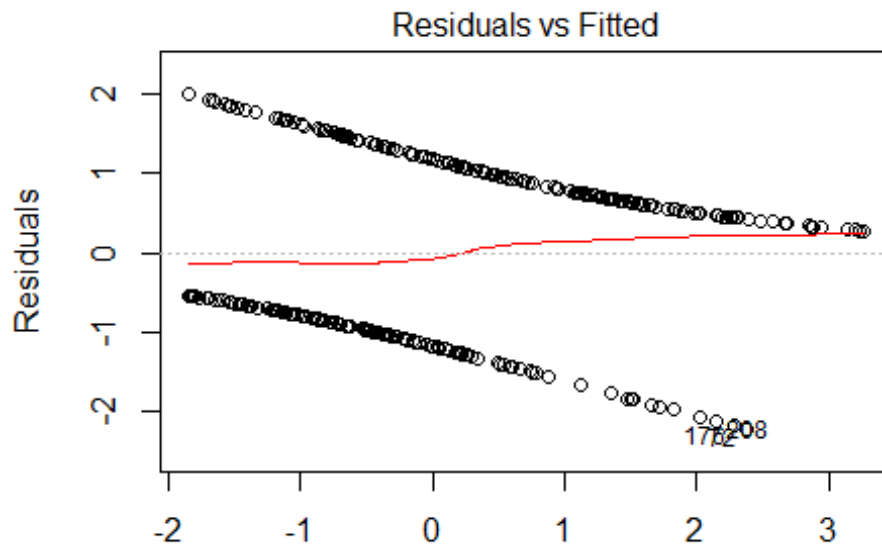
Use a polynomial of degree 2 to model the effect of drinks. Does it improve the model?

A:

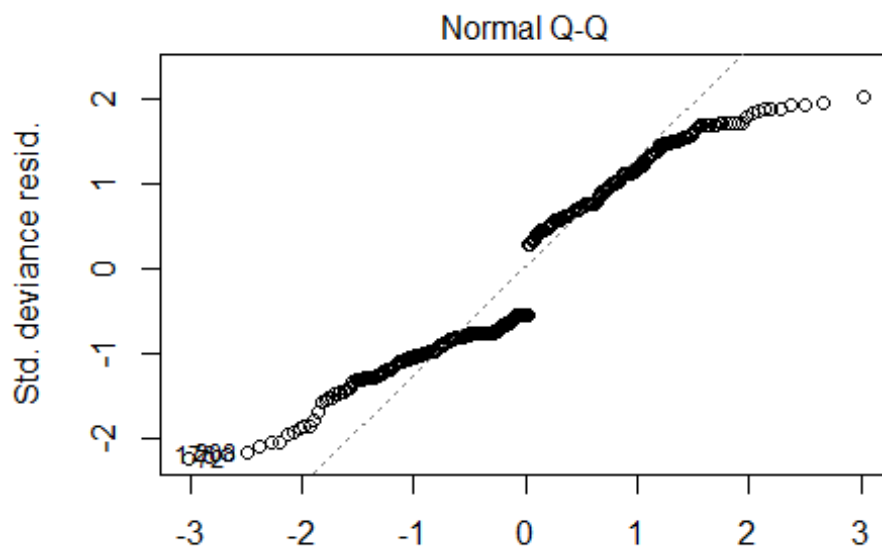
```
mod.quad.drinks = glm(y ~ oral_ca$drinks + I(oral_ca$drinks^2) + oral_ca$cigs + oral_ca$sex, family = 'binomial')
print(summary(mod.quad.drinks))

##
## Call:
## glm(formula = y ~ oral_ca$drinks + I(oral_ca$drinks^2) + oral_ca$cigs +
##      oral_ca$sex, family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.2192  -0.8379  -0.5405   0.8756   1.9980
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -1.850e+00  2.667e-01  -6.936 4.03e-12 ***
## oral_ca$drinks    5.362e-02  1.052e-02   5.099 3.42e-07 ***
## I(oral_ca$drinks^2) -2.295e-04  8.419e-05  -2.726 0.006405 **
## oral_ca$cigs     3.301e-02  9.642e-03   3.424 0.000618 ***
## oral_ca$sex      7.256e-01  2.854e-01   2.542 0.011007 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 437.62  on 392  degrees of freedom
## AIC: 447.62
##
## Number of Fisher Scoring iterations: 4

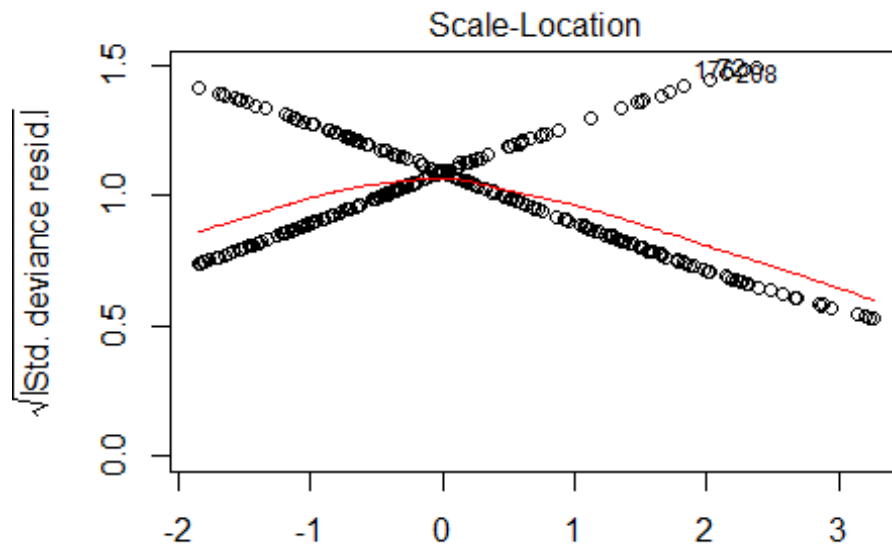
plot(mod.quad.drinks)
```



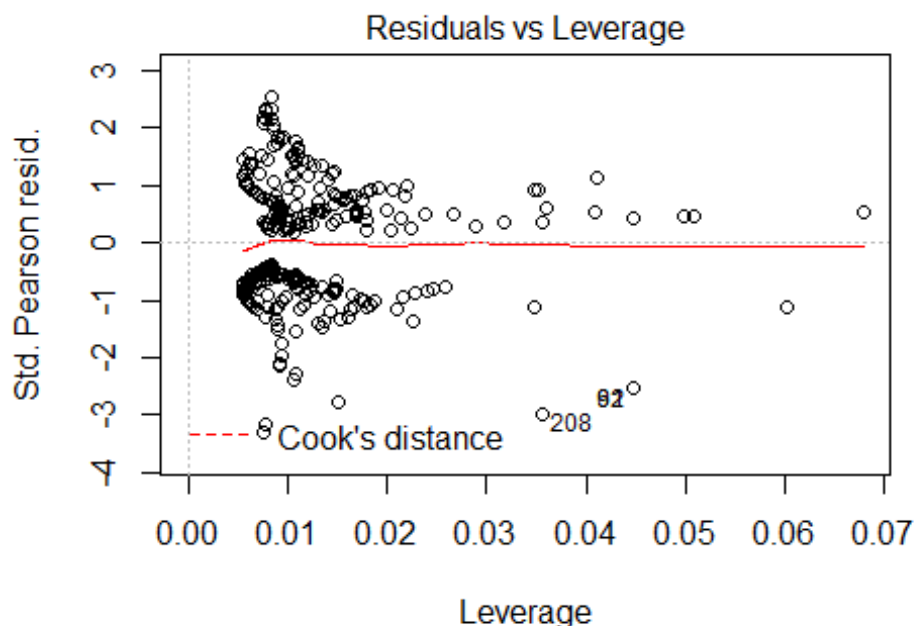
Predicted values
 $\text{glm}(y \sim \text{oral_ca}\$drinks + I(\text{oral_ca}\$drinks^2) + \text{oral_ca}\$cigs + \text{oral_ca}$



Theoretical Quantiles
 $\text{glm}(y \sim \text{oral_ca}\$drinks + I(\text{oral_ca}\$drinks^2) + \text{oral_ca}\$cigs + \text{oral_ca}$



Predicted values
 $\text{glm}(y \sim \text{oral_ca}\$drinks + I(\text{oral_ca}\$drinks^2) + \text{oral_ca}\$cigs + \text{oral_ca}$



Leverage
 $\text{glm}(y \sim \text{oral_ca}\$drinks + I(\text{oral_ca}\$drinks^2) + \text{oral_ca}\$cigs + \text{oral_ca}$

The change to a quadratic polynomial for the drinks variable did not seem to change much, it is a small variable compared to the other one, but has a significant p-value. The p-value can be caused by the high similarity between drinks and drinks², this theory is strengthened by the increase in the p-value of drinks.

(h)

Q:

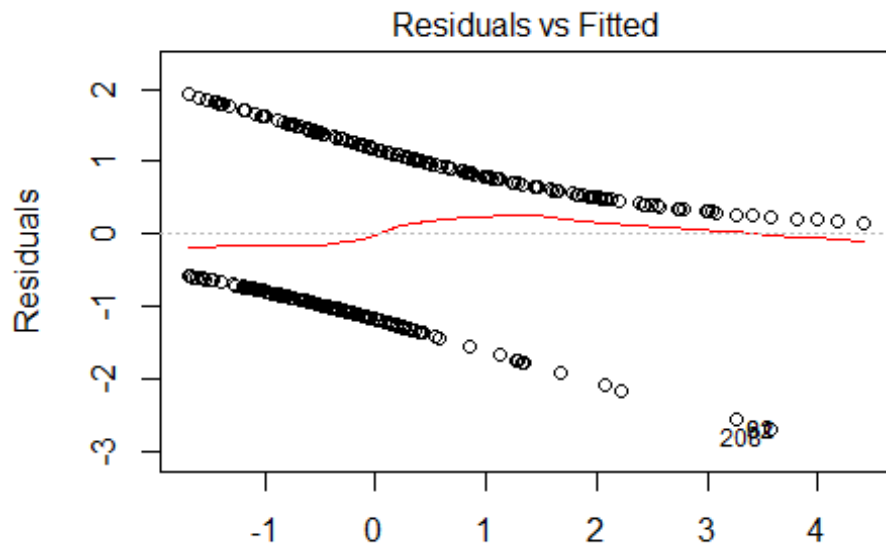
What about doing that for cigs instead of drinks? What is the effect on the model?

A:

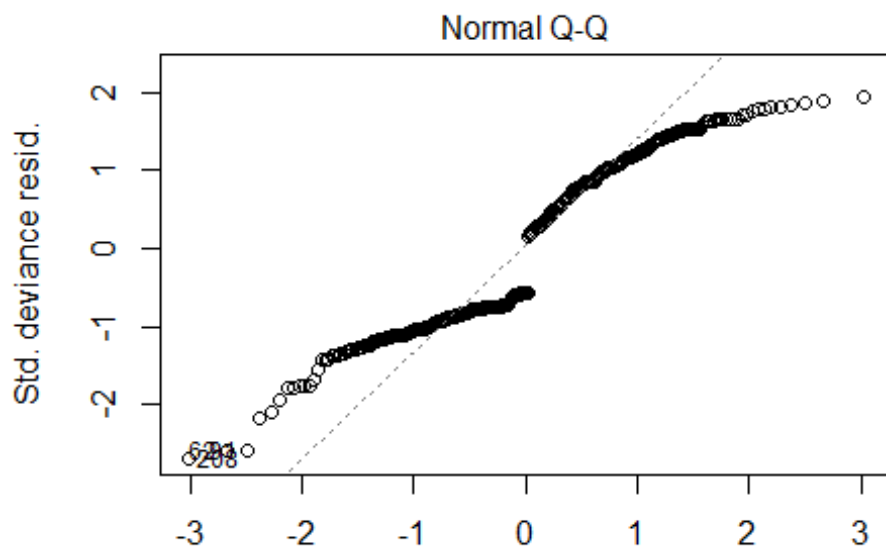
```
mod.quad.smokes = glm(y ~ oral_ca$drinks + oral_ca$cigs + I(oral_ca$cigs^2) +
oral_ca$sex, family = 'binomial')
print(summary(mod.quad.smokes))

##
## Call:
## glm(formula = y ~ oral_ca$drinks + oral_ca$cigs + I(oral_ca$cigs^2) +
##      oral_ca$sex, family = "binomial")
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.6870  -0.8764  -0.5808   0.9695   1.9303
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -1.6943120   0.2697349  -6.281 3.36e-10 ***
## oral_ca$drinks    0.0289791   0.0046347   6.253 4.04e-10 ***
## oral_ca$cigs     0.0541177   0.0238775   2.266  0.0234 *
## I(oral_ca$cigs^2) -0.0004485   0.0005225  -0.858  0.3907
## oral_ca$sex      0.6019008   0.2742844   2.194  0.0282 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 550.15  on 396  degrees of freedom
## Residual deviance: 443.55  on 392  degrees of freedom
## AIC: 453.55
##
## Number of Fisher Scoring iterations: 5

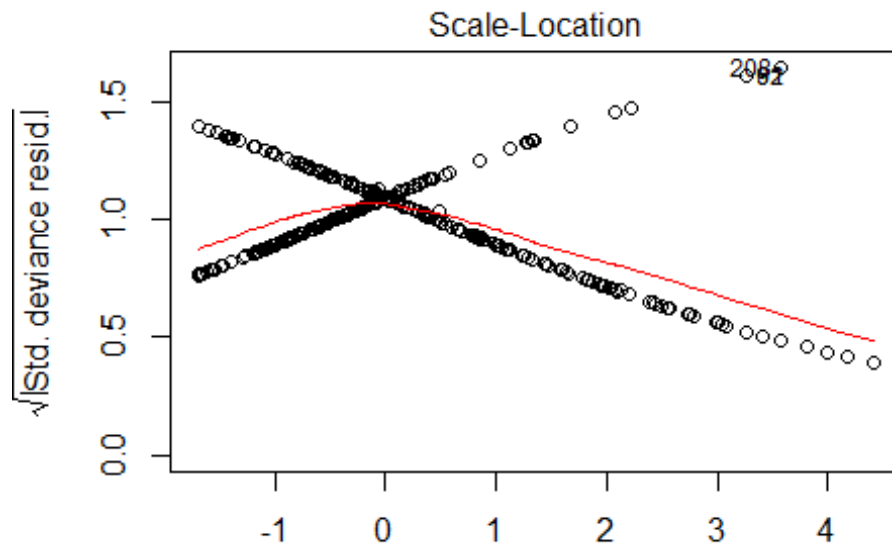
plot(mod.quad.smokes)
```

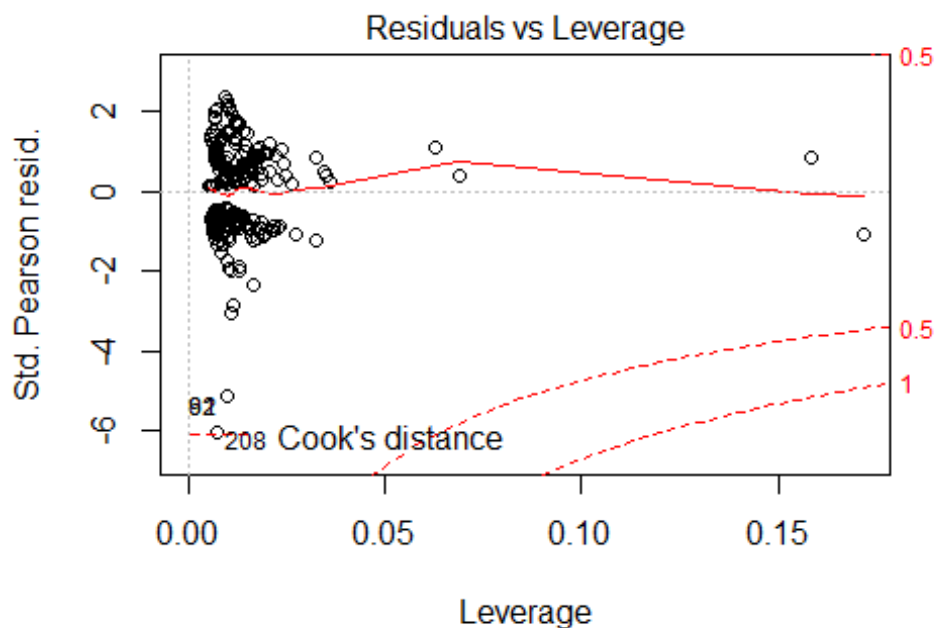
Predicted values
 $\text{glm}(y \sim \text{oral_ca\$drinks} + \text{oral_ca\$cigs} + \text{l}(\text{oral_ca\$cigs}^2) + \text{oral_ca\$}$



Theoretical Quantiles
 $\text{glm}(y \sim \text{oral_ca\$drinks} + \text{oral_ca\$cigs} + \text{l}(\text{oral_ca\$cigs}^2) + \text{oral_ca\$}$



glm(y ~ oral_ca\$drinks + oral_ca\$cigs + l(oral_ca\$cigs^2) + oral_ca\$



glm(y ~ oral_ca\$drinks + oral_ca\$cigs + l(oral_ca\$cigs^2) + oral_ca\$

Adding $cigs^2$ as a variable also did not change the model much. Here the $cigs^2$ variable even has a high p-value, showing the insignificance of the variable.

(i)

Adding the quadratic variables did not seem to give the biggest effect. It seems to make the non-squared variable (cigs, drinks) less significant with a comparable degree the quadratic values give to the model. So they might be better but not significantly. No significant difference in the residuals either.

(j)

If the model fit a quadratic scale, that means that two drinks is more than twice as bad than one drink. It does not necessarily make it worse to drink 10 units, if the model fits with linear or quadratic variables, it will just change the coefficients. A way to explain this is with the functions

$$f(x = 10) = \beta_1 * x = a, \text{ and } f(x = 10) = \beta_1 * x + \beta_2 * x^2 = a.$$

The point of the function is to show that if you drink 10 drinks and the relation is linear can be the same as drinking 10 drinks in a quadratic model. This is correct in all polynomials.

(k)

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