

$$y \quad y'' - 4y' + 4 = 0 \quad y(0) = 1 \quad , \quad y'(0) = 1$$

$$r = \frac{-(-4) \pm \sqrt{(-4)^2 - 4 \cdot 4}}{2 \cdot 1}$$

$$= \frac{4 \pm \sqrt{0}}{2}$$

$$r = 2$$

$$y(x) = C \cdot e^{2x} + D x e^{2x}$$

$$y(0) = 1 = C e^{2 \cdot 0} + D \cdot 0 \cdot e^{2 \cdot 0}$$

$$1 = C \cdot 1$$

$$C = 1$$

$$\begin{aligned} y'(x) &= 2C e^{2x} + (Dx)' e^{2x} + Dx \cdot 2 e^{2x} \\ &= 2C e^{2x} + D e^{2x} + 2Dx e^{2x} \end{aligned}$$

$$y'(0) = 2 \cdot 1 \cdot 1 + D \cdot e^{2 \cdot 0} + 0 = 1$$

$$1 = 2 + D \cdot 1$$

$$-1 = D$$

$$e^{2x} - x e^{2x}$$

$$x^2 y' y^2 = 2x$$

$$y' y^2 = \frac{2}{x}$$

