

$$2.2 \quad f(x) \approx f(x_0) + \left(\frac{df}{dx} \right)_{x_0, y_0} (x - x_0) + \left(\frac{df}{dy} \right)_{x_0, y_0} (y - y_0)$$

$$2.a) \quad f(x) = \sin(x) \quad x_0 = 0$$

$$\begin{aligned} f(x) &\approx \sin 0 + \cos 0 (x - 0) \\ &\approx x \end{aligned}$$

$$c) \quad f(x) = e^{x^2}, \quad x_0 = 0 \quad \text{and} \quad x_0 = 1 \\ \frac{df}{dx} = e^{x^2} (x^2)' = 2x e^{x^2} \Rightarrow \begin{cases} 0 \\ 2e \end{cases}$$

$$f(x) \approx 1 + 0(x - 0) = 1$$

$x_0 = 0$

$$f(x) = e + 2e(x-1) = e(2x-1)$$

$x_0 = 1$

$$e) \quad g(x, y) = \sin x \cos y \quad \text{at point } (x_0, y_0) = (0, 0)$$

$$\frac{\partial g}{\partial y} = \sin x \cdot (-\sin y) \Rightarrow \left. \frac{\partial g}{\partial x} \right|_{(x_0, y_0)} = 0$$

$$\frac{\partial g}{\partial x} = \cos x \sin y \Rightarrow \left. \frac{\partial g}{\partial y} \right|_{(x_0, y_0)} = 1$$

$$g(x, y) \approx 0 + 1(x - 0) + 0(y - 0) = x$$

$$f) \quad g(x,y) = xy^2 - e^{x+y}, \quad (x_0, y_0) = (1, -1)$$

$$\frac{\partial g}{\partial x} = y^2 - e^{x+y} (1) =$$

$$5) \quad \Delta \beta = \frac{d\beta}{dx} \Delta x + \frac{d\beta}{dy} \Delta y + \frac{d\beta}{dz} \Delta z$$

$$a) \beta(x,y,z) = x^2 + xy + z^2$$

$$\frac{d\beta}{dx} = 2x + y, \quad \frac{d\beta}{dy} = x, \quad \frac{d\beta}{dz} = 2z$$

$$\underline{2x+y}i + \underline{x}j + \underline{2z}k$$

$$b) \quad \beta(x,y,z) = e^{-(x+y+z)}$$

$$\frac{d\beta}{dx} = e^{-(x+y+z)} \cdot (-(-x-y-z))' = e^{-(x+y+z)} \cdot -1 = -y e^{-(x+y+z)}$$

$$\frac{d\beta}{dy} = e^{-(x+y+z)} \cdot -x = -x e^{-(x+y+z)}$$

$$\frac{d\beta}{dz} = e^{-(x+y+z)}, \quad -1 = -e^{-(x+y+z)}$$

$$\nabla \beta = -y e^{-(x+y+z)} \underline{i} - x e^{-(x+y+z)} \underline{j} + -e^{-(x+y+z)} \underline{k}$$

$$= \underline{-e^{-(x+y+z)}} (\underline{y} \underline{i} + \underline{x} \underline{j} + \underline{k})$$

