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ML 6143 Prof Sundeep Ragan

PRJOECT: NITS CBRS RADAR 3.5 GHz Waveform Detection

RadarWaveformsML - Detecting the Presence of the Waveform Immersed in Gaussian Noise using PCA

Manipulation of Radar and Communication Waveforms using new ML algorithms but not forgetting the Old Tricks

This repository was originally created for project for the Class "Introduction to Machine Learning at NYU Tandon" ministered by Professor Sundeep Ragan (more details at <https://github.com/sdrangan/introml>) (<https://github.com/sdrangan/introml>))

The main goal is to use synthetic radar waveforms (**RF Dataset of Incumbent Radar Systems in the 3.5 GHz CBRS Band**) provided by the scientists at the US National Institute of Standards and Technology (NIST) (more details at <https://data.nist.gov/od/id/mds2-2116> (<https://data.nist.gov/od/id/mds2-2116>)) to investigate the detection of features in the waveforms using *Machine Learning* techniques.

We are interested in simple trainable algorithms that able to detect the waveforms in the presence of noise (and also fading in the future). We are also interested in find the *signatures* of the waveforms to be able to classify the different radar waveforms and differentiate them from other electromagnetic signals, like the ones used for microwave wireless communications.

Real-time time identification of waveforms is an important tool that can be used to allow coexistence of different emitters sharing the same geographical space. It is also relevant for cyber-security, helping to assure security in cyber-physical environments.

NOTE: to develop the code here we used examples provided in the NIST directory about how read the data files and label files fields correctly in the Python Programming Language. The MATLAB code used by the scientists at NIST to generated radar wavforms simililar to the ones they made avaiable can be found at

<https://github.com/usnistgov/SimulatedRadarWaveformGenerator.git/trunk>
(<https://github.com/usnistgov/SimulatedRadarWaveformGenerator.git/trunk>)

NIST Data Website <https://data.nist.gov/od/id/mds2-2116> (<https://data.nist.gov/od/id/mds2-2116>)

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Importing some Libraries

```
In [1]: import numpy as np
import h5py
from pathlib import Path
import pandas as pd
import matplotlib.pyplot as plt
GDRIVE_MOUNTED=False
```

Some Details about How to Dowload RF Dataset of Incumbent Radar Systems in the 3.5 GHz CBRS Band

Each file has 200 synthetically created waveforms, each being 80 ms long. Some waveorms have only gaussian noise. Others have radar waveforms immersered in gaussian noise under several different SNR. Radar waveforms can be different types of simple pulse trains or more complex chirped waveforms.

Each file size is 2.5 GB. The total dataset is 500 GB! We will use just a few files from the database. Additional small csv files provide different types of labels related to the data.

The data can be download directly from NIST using the link <https://data.nist.gov/od/id/mds2-2116>
(<https://data.nist.gov/od/id/mds2-2116>)

For convencience, a subset of of the data was downloaded in the Google drive and is accessible for people from NYU. The shared link below provides access to the NYU folks. The shared folder has the same structure as the NIST database but only few of the large waveform files.

<https://drive.google.com/drive/folders/1lhVG7mAMoTFjsXbArvrz3cEIXDIJVnDS?usp=sharing>
(<https://drive.google.com/drive/folders/1lhVG7mAMoTFjsXbArvrz3cEIXDIJVnDS?usp=sharing>)

Once the code is copied into the person google drive, the code below can be easily adjusted to access the data by chaning the variables *data_folder* and *remote_folder_gdrive*. The code below also allows to run the iphython notebook locally in the machine. In this case the variable *remote_folder_local* needs to be updated

The code below also checks if GPU is enabled.

```

In [2]: str_GPU='GPU'
#str_GPU='CPU' #To fake having a GPU
data_folder="SimulatedRadarWaveforms"
remote_folder_gdrive="./gdrive/My Drive/_BIG1/NIST/CBRS/"+data_folder
remote_folder_local="/G/_BIG1/NIST/CBRS/"+data_folder

import os
#!df -k | egrep "Filesystem|overlay"
#!ls

# MOUNT GDRIVE
if 'google.colab' in str(get_ipython()):
    GCOLAB_ENV=True
    print('***RUNNING on CoLab')
    if False==GDRIVE_MOUNTED:
        from google.colab import drive
        drive.mount("/content/gdrive")
        GDRIVE_MOUNTED=True
    else:
        print('***NOT RUNNING on CoLab')
        GCOLAB_ENV=False

# CHECK if System has GPU
from tensorflow.python.client import device_lib
resp = device_lib.list_local_devices()
if str_GPU in str(resp):
    has_gpu=True
    gpu_info = !nvidia-smi
    gpu_info = '\n'.join(gpu_info)
    if gpu_info.find('failed') >= 0: print('GPU Info NOT AVAILABLE (!?!')
    else:
        print(gpu_info)
else:
    has_gpu=False

# LOAD Data
if True==GCOLAB_ENV:
    data_folder_full = remote_folder_gdrive
    #!rsync -av "$remote_folder" .
    #!du "$data_folder"
    #!rsync -av "$data_folder" .
else:
    data_folder_full = remote_folder_local

print('Data Folder:', data_folder_full)
!ls -l "$data_folder_full"

!rm -rf ./flickr2
if (True==has_gpu):
    print("*** DO SOMETHING (HAS GPU)")
else:
    print("*** DO SOMETHING (HAS NO GPU)")

```

```

***NOT RUNNING on CoLab
Data Folder: /G/_BIG1/NIST/CBRS/SimulatedRadarWaveforms
total 3789
-rwxrwxrwx 1 root root 3864830 Nov 19 08:05 allWaveformsTableCombined.csv
-rwxrwxrwx 1 root root      64 Nov 19 08:05 allWaveformsTableCombined.csv.sha
256
-rwxrwxrwx 1 root root    136 Dec  9 21:40 desktop.ini
dr-xr-xr-x 1 root root   4096 Dec  9 21:40 Group1
dr-xr-xr-x 1 root root      0 Dec  9 21:40 Group2
dr-xr-xr-x 1 root root      0 Dec  9 21:40 Group3
dr-xr-xr-x 1 root root      0 Dec  9 21:40 Group4
-rwxrwxrwx 1 root root   2282 Nov 19 08:04 License.txt
-rwxrwxrwx 1 root root     64 Nov 19 08:04 License.txt.sha256
-rwxrwxrwx 1 root root   1399 Nov 19 08:05 ReadMe.txt
-rwxrwxrwx 1 root root     64 Nov 19 08:04 ReadMe.txt.sha256
dr-xr-xr-x 1 root root   4096 Dec  9 21:40 readWaveformsCodeExamples
*** DO SOMETHING (HAS NO GPU)

```

Reading the Radar Waveform Data Set .mat files and the .csv file with the Additional Labels

This will take some time because the files are large.

```

In [3]: #dataRootFolder=data_folder
group_No =1  # 1 to 4
subset_No=2 # 1 to 50
# Preps
dataRootFolder =data_folder_full
fileName        ='group'+str(group_No)+'_subset_'+str(subset_No)+'.mat'
filePath        =Path(dataRootFolder)/('Group'+str(group_No))/(fileName)
waveform_var    ='group'+str(group_No)+'_waveformSubset_'+str(subset_No)
status_var      ='group'+str(group_No)+'_radarStatusSubset_'+str(subset_No)
table_var       ='group'+str(group_No)+'_waveformTableSubset_'+str(subset_No)
infoFileNamePath=Path(dataRootFolder)/('Group'+str(group_No))/( 'group'+
                                str(group_No)+'_subset_CSVInfo')/(table_var+'.csv')

#
# Read data from .mat file
h5pyObj         = h5py.File(filePath,'r')
subsetSignals    = h5pyObj[waveform_var][()].view(np.complex)
subsetRadarStatus = h5pyObj[status_var][()]
#
# Now use Panda to read the info csv file
subsetInfo = pd.read_csv(infoFileNamePath)

print('***DONE')

```

***DONE

Now Printing Some Fields to Get Familiar with the Data

Two label columns of special interest are *subsetRadarStatus=h5pyObj[status_var]* and *

1. *h5pyObj[status_varList]*: Indicates if a radar waveform is present
2. *subsetInfo['BinNo']*: Indicates the type of the waveform
3. *subsetInfo['SNR']*: Indicates the Signal-to-Noise Ratio when the radar waveform is present.

```
In [4]: def P2R(radii, angles):
        return radii * np.exp(1j*angles)

def R2P(x):
    return np.abs(x), np.angle(x)
```

```
In [5]: jj = 1.j
print("fileName      =", fileName)
print("waveform_var=", waveform_var)
print("status_var   =", status_var)
print("table_var    =", table_var)
print("h5pyObj      =", h5pyObj)
print('---')
print(['', waveform_var, '   ] subsetSignals.shape=', subsetSignals.shape)
print(['', status_var, '   ] subsetRadarStatus.shape=', subsetRadarStatus.shape)
print('subsetInfo.shape=', subsetInfo.shape)
print('---')
print(['', waveform_var, '   ] subsetSignals.shape=', subsetSignals.shape)
NPT=5
r, ang = R2P(subsetSignals[0, 0:NPT])
#print(subsetSignals[sigIndex, 0:NPT])
#print('r=\n', r.T)
#print('ang=\n', ang.T)
print(r*np.exp(jj*ang))

fileName      = group1_subset_2.mat
waveform_var= group1_waveformSubset_2
status_var   = group1_radarStatusSubset_2
table_var    = group1_waveformTableSubset_2
h5pyObj      = <HDF5 file "group1_subset_2.mat" (mode r)>
---
[ group1_waveformSubset_2   ] subsetSignals.shape= (200, 800000)
[ group1_radarStatusSubset_2 ] subsetRadarStatus.shape= (200, 1)
subsetInfo.shape= (200, 16)
---
[ group1_waveformSubset_2   ] subsetSignals.shape= (200, 800000)
[1.66089269e-07-2.31654912e-07j 1.35645134e-07+2.35493766e-07j
 1.58416011e-07-1.24614912e-07j 1.21105281e-07+4.92919982e-08j
 4.46692447e-07-3.11198016e-07j]
```

```
In [6]: ### show the info and status of the first 10
        #print(subsetRadarStatus[0:20])
        print("LABEL RADAR Waveform Present:\n\n", subsetRadarStatus[0:20].ravel())
        print("\nOTHER LABELS below:\n")
        print("...LABEL NAMES (Columns):\n... ..", subsetInfo.columns)
        print("\n... .. LABELS:\n",subsetInfo[0:20])
        #print(subsetInfo['BinNo'][0:20])
        aux = subsetInfo['SNR']; aux = aux[~np.isnan(aux)]; aux = np.unique(aux); print(aux);
        print('***DONE QUICKLY')
```

LABEL RADAR Waveform Present:

[0 0 1 1 0 0 0 0 0 0 0 0 1 0 1 1 0 1 0 0]

OTHER LABELS below:

...LABEL NAMES (Columns):

```
... ... Index(['BinNo', 'PulseWidth', 'PulsesPerSecond', 'PulsesPerBurst',
              'ChirpWidth', 'ChirpDirection', 'SamplingFrequency', 'ActualPulseWidth',
              'PhaseCodingType', 'SUID', 'radarStatus', 'radarSignalCenterFreq',
              'radarSignalStartTime', 'SNR', 'NoisePowerdBmPerMHz', 'duration'],
              dtype='object')
```

... ... LABELS:

	BinNo	PulseWidth	PulsesPerSecond	PulsesPerBurst	ChirpWidth \
0	NaN	NaN	NaN	NaN	NaN
1	NaN	NaN	NaN	NaN	NaN
2	Q3N#3	0.000085	800.0	20.0	50000000.0
3	P0N#2	0.000026	1690.0	10.0	NaN
4	NaN	NaN	NaN	NaN	NaN
5	NaN	NaN	NaN	NaN	NaN
6	NaN	NaN	NaN	NaN	NaN
7	NaN	NaN	NaN	NaN	NaN
8	NaN	NaN	NaN	NaN	NaN
9	NaN	NaN	NaN	NaN	NaN
10	NaN	NaN	NaN	NaN	NaN
11	NaN	NaN	NaN	NaN	NaN
12	Q3N#1	0.000003	1620.0	20.0	50000000.0
13	NaN	NaN	NaN	NaN	NaN
14	Q3N#1	0.000004	870.0	22.0	70000000.0
15	P0N#1	0.000002	1010.0	35.0	NaN
16	NaN	NaN	NaN	NaN	NaN
17	Q3N#2	0.000021	1750.0	2.0	3000000.0
18	NaN	NaN	NaN	NaN	NaN
19	NaN	NaN	NaN	NaN	NaN

	ChirpDirection	SamplingFrequency	ActualPulseWidth	PhaseCodingType \
0	NaN	10000000	NaN	NaN
1	NaN	10000000	NaN	NaN
2	Down	10000000	0.000085	NaN
3	NaN	10000000	0.000026	Barker
4	NaN	10000000	NaN	NaN
5	NaN	10000000	NaN	NaN
6	NaN	10000000	NaN	NaN
7	NaN	10000000	NaN	NaN
8	NaN	10000000	NaN	NaN
9	NaN	10000000	NaN	NaN
10	NaN	10000000	NaN	NaN
11	NaN	10000000	NaN	NaN
12	Down	10000000	0.000003	NaN
13	NaN	10000000	NaN	NaN
14	Up	10000000	0.000004	NaN
15	NaN	10000000	0.000002	NaN
16	NaN	10000000	NaN	NaN
17	Down	10000000	0.000021	NaN
18	NaN	10000000	NaN	NaN

19	NaN	10000000	NaN	NaN
		SUID	radarStatus	radarSignalCenterFreq
\				
0		NaN	0	NaN
1		NaN	0	NaN
2	1c19ef39-f88b-4ff9-a77d-68bc9eb141ef		1	0.0
3	b6e3b197-b0ff-49d2-916c-5bc60df615e4		1	1623597.0
4		NaN	0	NaN
5		NaN	0	NaN
6		NaN	0	NaN
7		NaN	0	NaN
8		NaN	0	NaN
9		NaN	0	NaN
10		NaN	0	NaN
11		NaN	0	NaN
12	6ac0e889-f818-49de-9e7b-40779815a572		1	0.0
13		NaN	0	NaN
14	6d0b9cf4-8efd-4e2c-bc77-139f0c4a8054		1	0.0
15	00c8c6d2-064b-4396-b340-b0ce8d321716		1	-705689.0
16		NaN	0	NaN
17	f9643519-bda0-47e9-9ea0-9745406539c6		1	-1046091.0
18		NaN	0	NaN
19		NaN	0	NaN

	radarSignalStartTime	SNR	NoisePowerdBmPerMHz	duration
0	NaN	NaN	-109	0.08
1	NaN	NaN	-109	0.08
2	0.008170	10.0	-109	0.08
3	0.015718	18.0	-109	0.08
4	NaN	NaN	-109	0.08
5	NaN	NaN	-109	0.08
6	NaN	NaN	-109	0.08
7	NaN	NaN	-109	0.08
8	NaN	NaN	-109	0.08
9	NaN	NaN	-109	0.08
10	NaN	NaN	-109	0.08
11	NaN	NaN	-109	0.08
12	0.018937	16.0	-109	0.08
13	NaN	NaN	-109	0.08
14	0.020553	14.0	-109	0.08
15	0.022690	16.0	-109	0.08
16	NaN	NaN	-109	0.08
17	0.022535	16.0	-109	0.08
18	NaN	NaN	-109	0.08
19	NaN	NaN	-109	0.08

[10. 12. 14. 16. 18. 20.]

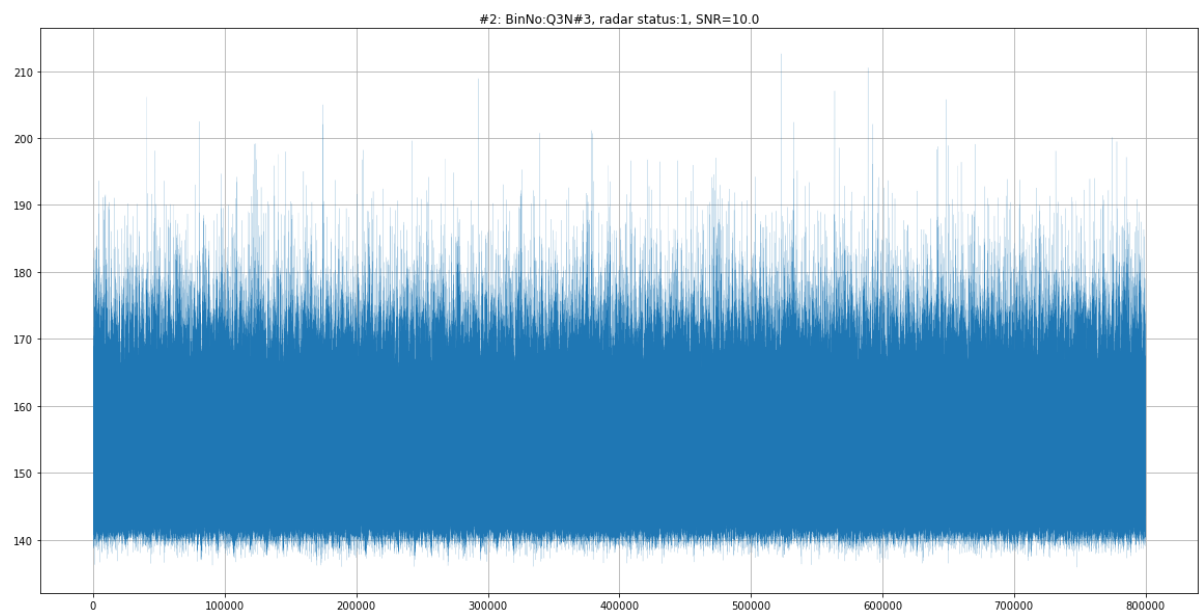
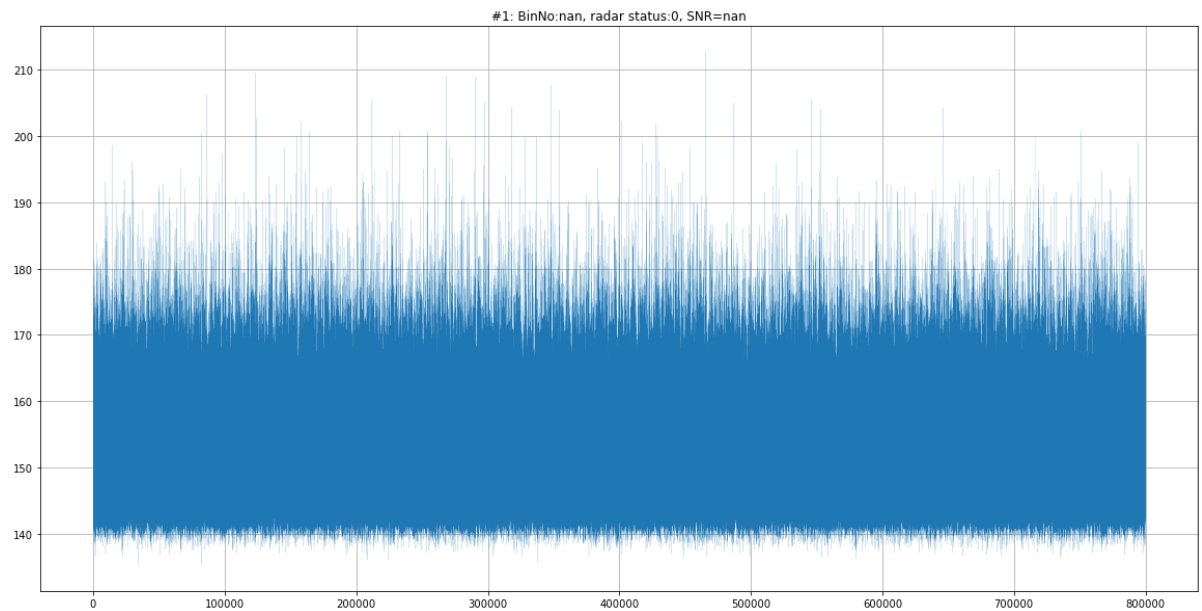
***DONE QUICKLY

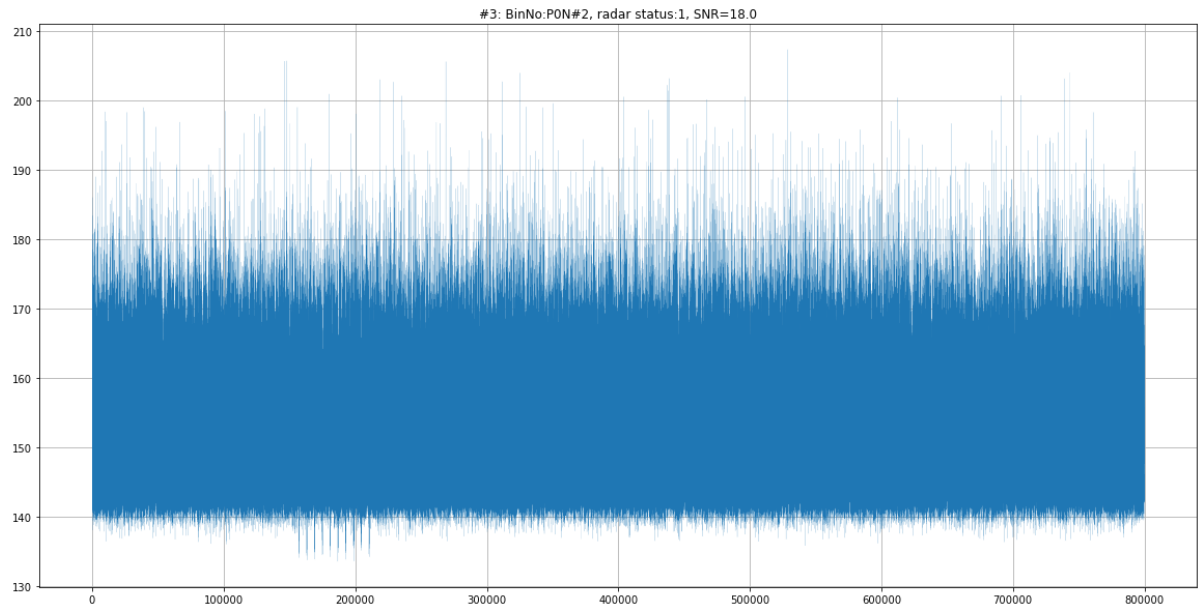
Below we plot three waveforms in the time domain.

The first has only noise, the second has a relatively low SNR and the third a relatively higher SNR. Note that the signal can be detected and it seems that only noise is present.


```
In [7]: noExamples=3
startFrom=1
for sigIndex in range(startFrom,startFrom+noExamples):
    #sigIndex=6 # Matlab index 6
    print('***Doing for sigIndex=', sigIndex)
    plt.figure(figsize=(20,10))
    plt.plot(-10*np.log(np.absolute(subsetSignals[sigIndex][0:-1])),linewidth
h=0.1)
    plt.title('#'+str(sigIndex)+': BinNo:'+str(subsetInfo['BinNo'][sigIndex
])+', radar status:'+str(subsetInfo['radarStatus'][sigIndex])+', SNR='+str(sub
setInfo['SNR'][sigIndex]))
    plt.grid()
print('***DONE!')
```

```
***Doing for sigIndex= 1  
***Doing for sigIndex= 2  
***Doing for sigIndex= 3  
***DONE!
```





Below we Plot Three Waveforms in the Frequency vs Time Domain.

Again the first has only noise, the second has a relatively low SNR and the third a relatively higher SNR. Note that now the signal is resolved cells of time and frequency the signal can be seen as non-random cell patterns on top of the 'sea of noise'. It is hardly noticeable in the second case (SNR=10 dB), but still it can be seen like a 'cat scratch' in the lower left quadrant of the spectrogram. In the case of the third spectrogram, the signal is much easier to see because of the higher SNR and also because the specific waveform used is short and 'shines more' above the noise 'sea level'

```

In [11]: from scipy import signal
Nfft=128
groupby=16 # no. of consectuive FFTs over which to take max

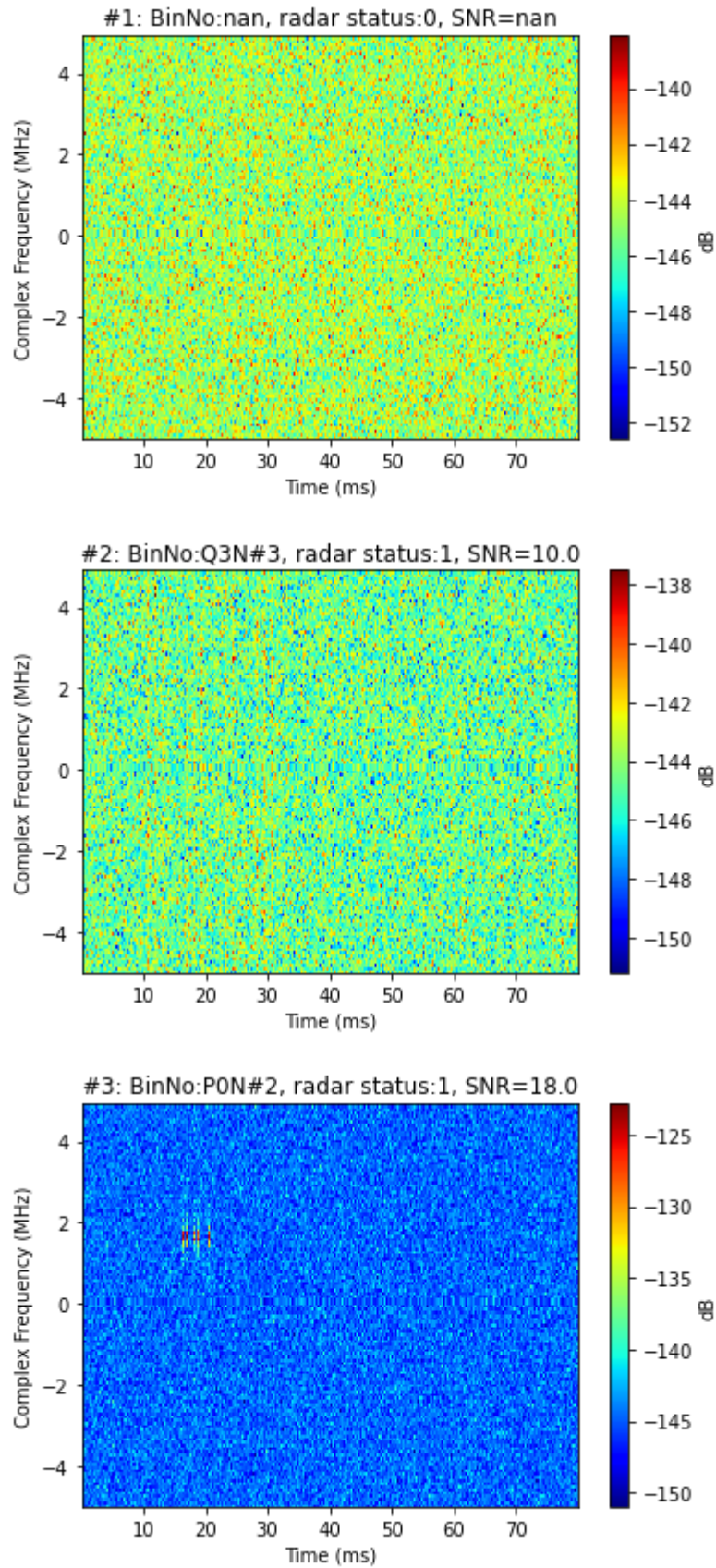
noExamples=3
startFrom=1
for sigIndex in range(startFrom,startFrom+noExamples):
    f, t0, S0 = signal.spectrogram(subsetSignals[sigIndex], fs=10e6, nperseg=Nfft,
    t, scaling='spectrum', return_onesided=False)
    #
    S0[0:1, :] = S0[1:2, :]
    L = S0.shape[1]/groupby
    S1 = np.reshape(S0[:, :int(L)*groupby], (Nfft,int(L),groupby))
    S = np.amax(S1, axis=-1)
    t = t0[groupby-1::groupby]

    print('S.shape=', S.shape)
    #S[0:1, :] = np.mean(S[70:80,:], axis=0)
    #S[0:1, :] = S[1:2, :]
    fshi = np.fft.fftshift(f/1e6)
    Sshi = np.fft.fftshift(10.*np.log10(S), axes=0)
    #print('Sshi.shape=', Sshi.shape)
    #
    #fig = plt.figure(figsize=(10,10))
    fig = plt.figure()
    cax = plt.pcolormesh(t*1e3, fshi, Sshi, cmap='jet')
    plt.title('#'+str(sigIndex)+': BinNo:'+str(subsetInfo['BinNo'][sigIndex])+',
    radar status:'+str(subsetInfo['radarStatus'][sigIndex])+', SNR:'+str(subsetInf
    o['SNR'][sigIndex]))
    plt.xlabel('Time (ms)')
    plt.ylabel('Complex Frequency (MHz)')
    fig.colorbar(cax).set_label('dB')

    print('***DONE!')

```

```
S.shape= (128, 446)  
S.shape= (128, 446)  
S.shape= (128, 446)  
***DONE!
```



```

In [12]: from scipy import signal
nruns=20
pca0 = 1
#noExamples=3
#startFrom=6
Nfft=128
groupby=16 # no. of consectuive FFTs over which to take max
#find signals with high SNR, e.g. SNR=20 dB
#highSNRIndex=np.where(subsetInfo.SNR==20)
#find signals with high SNR, e.g. SNR=10 dB

# [10. 12. 14. 16. 18. 20.]
#IselWaves=np.where(np.isnan(subsetInfo.SNR)) #Noise Only
#IselWaves=np.where(subsetInfo.SNR==10)
#IselWaves=np.where(subsetInfo.SNR==14)
#IselWaves=np.where(subsetInfo.SNR==16)
#IselWaves=np.where(subsetInfo.SNR==18)
IselWaves=np.where(subsetInfo.SNR==20)

idx=1
for I in np.nditer(IselWaves):
    if idx > nruns: break
    sigIndex=int(I)
    print('***-----')
    print('***Doing for sigIndex=', sigIndex, 'I=', I)
    print('...NSD   :', subsetInfo['NoisePowerdBmPerMHz'][sigIndex])
    print('...SNR   :', subsetInfo['SNR'][sigIndex])
    print('...BinNo  :', subsetInfo['BinNo'][sigIndex])
    #
    f, t0, S0 = signal.spectrogram(subsetSignals[sigIndex], fs=10e6, nperseg=Nfft
t, scaling='spectrum', return_onesided=False)
    #
    S0[0:1, :] = S0[1:2, :]
    L = S0.shape[1]/groupby
    S1 = np.reshape(S0[:, :int(L)*groupby], (Nfft,int(L),groupby))
    S = np.amax(S1, axis=-1)
    t = t0[groupby-1::groupby]

    print('S.shape=', S.shape)
    #S[0:1, :] = np.mean(S[70:80,:], axis=0)
    #S[0:1, :] = S[1:2, :]
    fshi = np.fft.fftshift(f/1e6)
    Sshi = np.fft.fftshift(10.*np.log10(S), axes=0)
    #print('Sshi.shape=', Sshi.shape)

    if 0: #Controls the printing of the Spectograms
        fig = plt.figure()
        cax = plt.pcolormesh(Sshi.T.dot(Sshi), cmap='jet')
        plt.title('Run# '+str(idx)+' '+str(subsetInfo['BinNo'][sigIndex])+ ' TIME')
        plt.xlabel('Time (ms)')
        plt.ylabel('Complex Frequency (MHz)')
        fig.colorbar(cax).set_label('dB')
        #
        fig = plt.figure()
        cax = plt.pcolormesh(Sshi.dot(Sshi.T), cmap='jet')
        plt.title('Run# '+str(idx)+' '+str(subsetInfo['BinNo'][sigIndex])+ ' TIME')

```

```

plt.xlabel('Time (ms)')
plt.ylabel('Complex Frequency (MHz)')
fig.colorbar(cax).set_label('dB')
#

if 1: #Controls the printing of the Spectograms
    fig = plt.figure()
    cax = plt.pcolormesh(t*1e3, fshi, Sshi, cmap='jet')
    plt.title('Run# '+str(idx)+' '+str(subsetInfo['BinNo'][sigIndex])+' TIME')
    plt.xlabel('Time (ms)')
    plt.ylabel('Complex Frequency (MHz)')
    fig.colorbar(cax).set_label('dB')
    #

if 1: #Controls the printing of the stem with the PCAs
    ##u, s, vh = np.linalg.svd(Sshi, full_matrices=False);
    #u, s, vh = np.linalg.svd(Sshi.T, full_matrices=False);
    u, s, vh = np.linalg.svd(Sshi.T.dot(Sshi), full_matrices=False);
    aux = 100*np.sort(s)[::-1]/np.sum(s)
    print(aux[0+pca0:10])
    fig = plt.figure()
    #plt.stem(np.log10(s[0+pca0:50]))
    plt.stem(aux[0+pca0:50])
    plt.title('Run# '+str(idx)+' '+str(subsetInfo['BinNo'][sigIndex])+' FREQ')

    print('...#%02d'%sigIndex,':','Min =', 10.*np.log10(min(S.flat
t)),'\n.....Max =', 10.*np.log10(max(S.flat)))
    idx += 1;
    # end of for()

print('***DONE!')
```

```

***-----
***Doing for sigIndex= 35 I= 35
...NSD   : -109
...SNR   : 20.0
...BinNo : P0N#2
S.shape= (128, 446)
[0.00232399 0.00022074 0.00020754 0.00019675 0.00019444 0.00019216
 0.00018671 0.00018247 0.000178   ]
...#35 : Min = -151.02472837414226
.....Max = -120.08953140163626
***-----
***Doing for sigIndex= 58 I= 58
...NSD   : -109
...SNR   : 20.0
...BinNo : Q3N#3

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
  plt.stem(aux[0+pca0:50])

S.shape= (128, 446)
[0.00028152 0.00024076 0.00023615 0.00022128 0.00021119 0.00019971
 0.00019233 0.00018658 0.00018577]

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
  plt.stem(aux[0+pca0:50])

...#58 : Min = -151.3335135591741
.....Max = -131.94023891783357
***-----
***Doing for sigIndex= 65 I= 65
...NSD   : -109
...SNR   : 20.0
...BinNo : P0N#1
S.shape= (128, 446)
[0.00058672 0.00023749 0.00020762 0.00019967 0.00019248 0.00018561
 0.00018214 0.00018023 0.00017686]
...#65 : Min = -151.03655666254565
.....Max = -135.06969963599408
***-----
***Doing for sigIndex= 68 I= 68
...NSD   : -109
...SNR   : 20.0
...BinNo : Q3N#1
S.shape= (128, 446)

```



```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00149946 0.00023857 0.00022552 0.00021438 0.00020129 0.00019603
 0.00019054 0.00018435 0.00018042]
```

```
...#68 : Min = -151.48232264681317
```

```
.....Max = -131.4430502721453
```

```
***-----
```

```
***Doing for sigIndex= 91 I= 91
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#2
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
S.shape= (128, 446)
```

```
[0.0014196 0.00020548 0.00020319 0.00019533 0.00019233 0.00018925
 0.00018322 0.0001826 0.00017847]
```

```
...#91 : Min = -150.86594370624715
```

```
.....Max = -122.10499582954179
```

```
***-----
```

```
***Doing for sigIndex= 111 I= 111
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#2
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
S.shape= (128, 446)
```

```
[0.00028613 0.00025746 0.00022483 0.00020191 0.00019263 0.00018966
 0.00018868 0.00018645 0.00018143]
```

```
...#111 : Min = -151.81896662484968
```

```
.....Max = -134.30213818061887
```

```
***-----
```

```
***Doing for sigIndex= 114 I= 114
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#1
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
S.shape= (128, 446)
```

```
[0.00097962 0.0002291 0.00020788 0.00020138 0.00019358 0.00018798
0.00018559 0.00017924 0.00017562]
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
...#114 : Min = -151.19106127468288
```

```
.....Max = -133.5301606458608
```

```
***-----
```

```
***Doing for sigIndex= 115 I= 115
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#1
```

```
S.shape= (128, 446)
```

```
[0.00114792 0.00020157 0.00019883 0.00019626 0.00018989 0.00018381
0.00018349 0.00017746 0.00017502]
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
...#115 : Min = -151.44744722793197
```

```
.....Max = -132.7352663963266
```

```
***-----
```

```
***Doing for sigIndex= 117 I= 117
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#2
```

```
S.shape= (128, 446)
```

```
[0.00157415 0.00024911 0.00022108 0.0002062 0.0002032 0.00018783
0.00018305 0.00018187 0.0001738 ]
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```

...#117 : Min = -151.07777991582591
.....Max = -125.53220642980008
***-----
***Doing for sigIndex= 119 I= 119
...NSD   : -109
...SNR    : 20.0
...BinNo  : P0N#1
S.shape= (128, 446)
[0.00059376 0.00022143 0.00021401 0.00020229 0.00019418 0.00018841
 0.00018659 0.00018389 0.00018114]

```

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual lines on a stem plot will be added as a LineCollection instead of individual lines. This significantly improves the performance of a stem plot. To remove this warning and switch to the new behaviour, set the "use_line_collection" keyword argument to True.

```
plt.stem(aux[0+pca0:50])
```

```

...#119 : Min = -151.26911147179163
.....Max = -135.12135248267165
***-----
***Doing for sigIndex= 124 I= 124
...NSD   : -109
...SNR    : 20.0
...BinNo  : Q3N#2
S.shape= (128, 446)

```

<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual lines on a stem plot will be added as a LineCollection instead of individual lines. This significantly improves the performance of a stem plot. To remove this warning and switch to the new behaviour, set the "use_line_collection" keyword argument to True.

```
plt.stem(aux[0+pca0:50])
```

```

[0.0004879 0.0002956 0.00023166 0.00020239 0.00019962 0.00019502
 0.00019155 0.00018967 0.00018455]
...#124 : Min = -150.87422512197674
.....Max = -131.52685010457566
***-----
***Doing for sigIndex= 125 I= 125
...NSD   : -109
...SNR    : 20.0
...BinNo  : Q3N#1
S.shape= (128, 446)

```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00372633 0.0002212 0.00020698 0.00020187 0.00019325 0.00018656
0.00018463 0.00017852 0.00017655]
```

```
...#125 : Min = -151.38356171593816
```

```
.....Max = -127.53079386440504
```

```
***-----
```

```
***Doing for sigIndex= 139 I= 139
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#1
```

```
S.shape= (128, 446)
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00094953 0.00021976 0.00020538 0.00020013 0.00019493 0.00018718
0.00018442 0.00018219 0.00017843]
```

```
...#139 : Min = -150.7372754920851
```

```
.....Max = -133.06277251375909
```

```
***-----
```

```
***Doing for sigIndex= 141 I= 141
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#2
```

```
S.shape= (128, 446)
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00147385 0.00023513 0.0002092 0.00019916 0.00019195 0.00018956
0.00018602 0.00018301 0.0001774 ]
```

```
...#141 : Min = -151.3084014549656
```

```
.....Max = -121.11324542589622
```

```
***-----
```

```
***Doing for sigIndex= 147 I= 147
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#3
```

```
S.shape= (128, 446)
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00023904 0.0002188 0.00020509 0.00019901 0.00019633 0.00019169
0.00018638 0.00018121 0.00017851]
```

```
...#147 : Min = -151.71647924571732
```

```
.....Max = -131.90681479594087
```

```
***-----
```

```
***Doing for sigIndex= 167 I= 167
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#1
```

```
S.shape= (128, 446)
```

<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

```
[0.00103332 0.00023766 0.00023341 0.00019999 0.00019372 0.00019179
 0.00018909 0.00018516 0.00018325]
```

```
...#167 : Min = -151.25604488973826
```

```
.....Max = -131.0912792080857
```

```
***-----
```

```
***Doing for sigIndex= 178 I= 178
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#3
```

<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual lines on a stem plot will be added as a LineCollection instead of individual lines. This significantly improves the performance of a stem plot. To remove this warning and switch to the new behaviour, set the "use_line_collection" keyword argument to True.

```
plt.stem(aux[0+pca0:50])
```

```
S.shape= (128, 446)
```

```
[0.00023161 0.00019792 0.0001898 0.00018805 0.00018505 0.00018181
 0.0001789 0.00017713 0.00017481]
```

<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have been opened. Figures created through the pyplot interface (`matplotlib.pyplot.figure`) are retained until explicitly closed and may consume too much memory. (To control this warning, see the rcParam `figure.max_open_warning`).

```
fig = plt.figure()
```

<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual lines on a stem plot will be added as a LineCollection instead of individual lines. This significantly improves the performance of a stem plot. To remove this warning and switch to the new behaviour, set the "use_line_collection" keyword argument to True.

```
plt.stem(aux[0+pca0:50])
```

```
...#178 : Min = -151.38530436436767
```

```
.....Max = -134.32642947361796
```

```
***-----
```

```
***Doing for sigIndex= 183 I= 183
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#2
```

```
S.shape= (128, 446)
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.00030974 0.00024871 0.00021824 0.00020223 0.00019935 0.00019302
0.00018828 0.00018378 0.00017726]
```

```
...#183 : Min = -151.24298325530708
```

```
.....Max = -133.47340456090927
```

```
***-----
```

```
***Doing for sigIndex= 184 I= 184
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : P0N#2
```

```
S.shape= (128, 446)
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
[0.001358 0.00021907 0.00020433 0.00019646 0.0001938 0.00019228
0.00018693 0.00018027 0.00017898]
```

```
...#184 : Min = -151.502286502086
```

```
.....Max = -124.96510235620038
```

```
***-----
```

```
***Doing for sigIndex= 196 I= 196
```

```
...NSD : -109
```

```
...SNR : 20.0
```

```
...BinNo : Q3N#2
```

```
S.shape= (128, 446)
```

```
[0.000642 0.00024194 0.0001981 0.00019632 0.00018952 0.00018555
0.00018321 0.00017891 0.00017742]
```

```
<ipython-input-12-e930dbe3b524>:62: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo-
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:76: RuntimeWarning: More than 20 figures have
been opened. Figures created through the pyplot interface (`matplotlib.pyplot.
figure`) are retained until explicitly closed and may consume too much memo-
ry. (To control this warning, see the rcParam `figure.max_open_warning`).
```

```
fig = plt.figure()
```

```
<ipython-input-12-e930dbe3b524>:78: UserWarning: In Matplotlib 3.3 individual
lines on a stem plot will be added as a LineCollection instead of individual
lines. This significantly improves the performance of a stem plot. To remove
this warning and switch to the new behaviour, set the "use_line_collection" k-
eyword argument to True.
```

```
plt.stem(aux[0+pca0:50])
```

```
...#196 : Min = -151.40688066030864
```

```
.....Max = -125.26483775092797
```

```
***DONE!
```

