

Assignment 0

| | |
|--------|--|
| MONK-1 | $(a_1 = a_2) \vee (a_5 = 1)$ |
| MONK-2 | $a_i = 1$ for exactly two $i \in \{1, 2, \dots, 6\}$ |
| MONK-3 | $(a_5 = 1 \wedge a_4 = 1) \vee (a_5 \neq 4 \wedge a_2 \neq 3)$ |

- **The hardest one is Monk2**

- Monk1: a_3 , a_4 and a_6 don't have influence on the decision. Only 4 possible combinations, therefore the tree only needs a depth of three to decide all the outcomes
- Monk2: all the attributes are independent, all the possible combinations are needed. Depth of six
- Monk3: As monk1 need only depths of three, but it has the misclassification noise, which makes it harder to read.

Assignment 1

- **Entropies** of the three datasets:

| DATASET | ENTROPY |
|---------|---------|
| MONK-1 | 1.0 |
| MONK-2 | 0.9561 |
| MONK-3 | 0.9998 |

Assignment 2

- **Uniform distributions have higher entropy** since all the datapoints are picked with equal probability, hence the randomness increases
- **Non-uniform distributions have lower entropy** since the randomness is lower
- Example the entropy of a normal dice (uniform) is equal to 2.58, which is higher than the entropy of a fake dice (non-uniform) that is 2.16

Assignment 3

- The attribute that should be used for splitting at the root node is the one with the **higher information gain**, since an higher information gain means an higher entropy reduction after the splitting.

| Dataset | a1 | a2 | a3 | a4 | a5 | a6 |
|---------|---------|---------|---------|---------|---------|---------|
| MONK-1 | 0.07527 | 0.00584 | 0.00471 | 0.02631 | 0.28703 | 0.00076 |
| MONK-2 | 0.00376 | 0.00246 | 0.00106 | 0.01566 | 0.01728 | 0.00625 |
| MONK-3 | 0.00712 | 0.29374 | 0.00083 | 0.00289 | 0.25591 | 0.00708 |

Assignment 4

- Looking at the equation, the entropy of the subset S_k decrease when the information gain is maximized
- When the information gain increases, the entropy decreases
- By picking the attribute which maximize the information gain, we will have the higher entropy reduction.
- We know that a low entropy implies lower randomness in the dataset, i.e. more certainty about the classification

Assignment 5

- Errors for the three full trees

| Dataser | E_{train} | E_{test} |
|---------|--------------------|-------------------|
| MONK-1 | 0 | 0.1713 |
| MONK-2 | 0 | 0.3079 |
| MONK-3 | 0 | 0.0556 |

Assignment 6

- By pruning a tree we reduce its complexity. This implies lower variance and higher bias than the original tree
- Pruning too much will implies to have a too simple model, which will have a too high bias
- We must find a trade-off

Assignment 7

