

## Reinforcement Learning

### Assignment 2

#### Summary

Q1) Exercise 3.4.

Please find the pdf file submitted for Question - 1.

Q2) The final value function of the equiprobable random policy. Comments added in python notebook.

```
values.round(1).reshape(5,5)
array([[ 3.3,  8.8,  4.4,  5.3,  1.5],
       [ 1.5,  3. ,  2.3,  1.9,  0.5],
       [ 0.1,  0.7,  0.7,  0.4, -0.4],
       [-1. , -0.4, -0.4, -0.6, -1.2],
       [-1.9, -1.3, -1.2, -1.4, -2. ]])
```

Q4) Optimal solutions to the grid world. Comments added in python notebook.

```
print(np.around(value_star, decimals=1))
```

```
[[22.  24.4 22.  19.4 17.5]
 [19.8 22.  19.8 17.8 16. ]
 [17.8 19.8 17.8 16.  14.4]
 [16.  17.8 16.  14.4 13. ]
 [14.4 16.  14.4 13.  11.7]]
```

```
for x in action_star:
    for y in x:
        print(y, end= ',')
    print()
```

```
[ '>' ], [ '^' ' <' 'd' ' >' ], [ '<' ], [ '^' ' <' 'd' ' >' ], [ '<' ],
[ '^' ' >' ], [ '^' ], [ '^' ' <' ], [ '<' ], [ '<' ],
[ '^' ' >' ], [ '^' ], [ '^' ' <' ], [ '^' ' <' ], [ '^' ' <' ],
[ '^' ' >' ], [ '^' ], [ '^' ' <' ], [ '^' ' <' ], [ '^' ' <' ],
[ '^' ' >' ], [ '^' ], [ '^' ' <' ], [ '^' ' <' ], [ '^' ' <' ],
```

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Q3)

- Exercise 3.15 and 3.16 (Images also added in the 'Images' folder)

### Exercise - 3.15

# Adding a constant  $c$  to all rewards.

$$V_{\pi}(s) = E_{\pi} [G_t | S_t = s]$$

$$= E_{\pi} \left[ \sum_{k=0}^{\infty} r_{t+1+k} \gamma^k \mid S_t = s \right]$$

$$\# \quad r' = r + c$$

then.

new value of states

$$V'_{\pi}(s) = E_{\pi} \left[ \sum_{k=0}^{\infty} (r_{t+1+k} + c) \gamma^k \mid S_t = s \right]$$

$$= E_{\pi} \left[ \sum_{k=0}^{\infty} r_{t+1+k} \gamma^k \mid S_t = s \right] + E_{\pi} \left[ \sum_{k=0}^{\infty} c \gamma^k \mid S_t = s \right]$$

$$= V_{\pi}(s) + \frac{c}{1-\gamma}$$

$$\text{or } V'_{\pi}(s) = V_{\pi}(s) + \frac{c}{1-\gamma}$$

$$V_c = \frac{c}{1-\gamma} \rightarrow \text{constant added to all states.}$$

It does not affect relative value of states under any policies.

### Ex - 3.16

If the task were an episodic one,  
~~then~~ then,

$$V_{\pi}(s) = E_{\pi} [G_t | S_t = s]$$

$$= E_{\pi} \left[ \sum_{k=0}^{T(s)} r_{t+1+k} \gamma^k \mid S_t = s \right]$$

$T(s)$  is the number of steps, starting from current state until the terminal state is reached.

$$V'_{\pi}(s) = E_{\pi} \left[ \sum_{k=0}^{T(s)} (r_{t+1+k} + c) \gamma^k \mid S_t = s \right]$$

$$= E_{\pi} \left[ \sum_{k=0}^{T(s)} r_{t+1+k} \gamma^k \mid S_t = s \right] + E_{\pi} \left[ \sum_{k=0}^{T(s)} c \gamma^k \mid S_t = s \right]$$

$$V'_{\pi}(s) = V_{\pi}(s) + \frac{c}{1-\gamma} \gamma^{T(s)}$$

'.' the ~~additional~~ additional term depends on  $T(s)$ , the relative value of states might change.

Example - This is because the states that are "closer" to terminal states will have low  $T(s)$  which will increase  $(\gamma)^{T(s)}$  which will decrease the additional term.

$V'_{\pi}(s)$  will have small value of additional term for states that are closer to the terminal states.  $\gamma$  might change relative valuation of states.

Q5) Equation for  $v^*$  in terms of  $q^*$

Q5 Equation for  $v^*$  in terms of  $q^*$ .

We know, 
$$v_*(s) = \max_{a \in A(s)} \mathbb{E} [R_{t+1} + \gamma V_*(s_{t+1}) \mid S_t = s, A_t = a]$$

and 
$$q_*(s, a) = \mathbb{E} [R_{t+1} + \gamma \max_{a' \in A(s')} q_*(s', a') \mid S_t = s, A_t = a]$$

$$\therefore v_*(s) = \max_{a \in A(s)} q_*(s, a).$$

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Q6)

- policy iteration and value iteration (VI) to solve the Gridworld in Example 4.1
- the fix to the bug mentioned in Exercise 4.4. (in jupyter notebook)

Q7) Exercise 4.7

Original Example

Exercise - 4.7

