



IIT ROORKEE



NPTEL ONLINE  
CERTIFICATION COURSE

# Charging Infrastructure

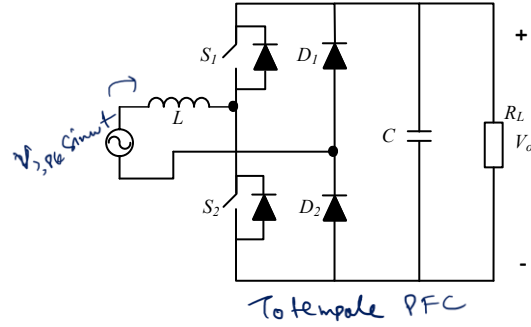
## Lecture-21

### Flyback based PFC Converter

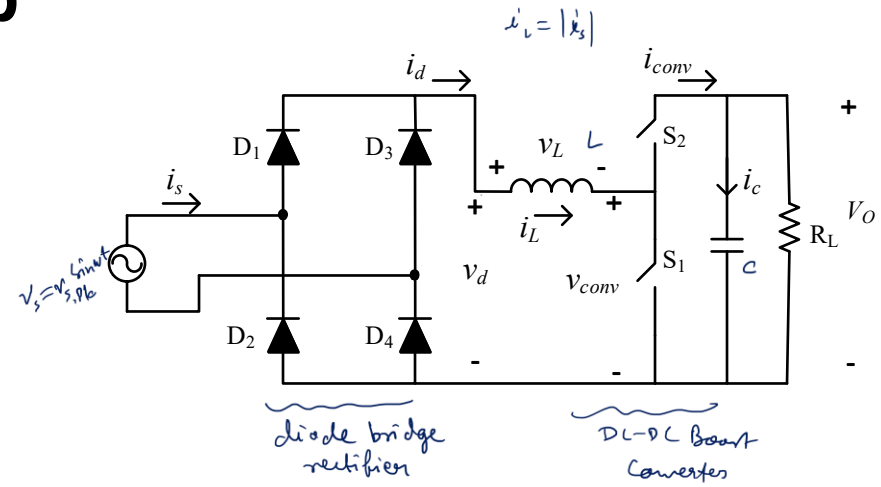
Dr. Apurv Kumar Yadav  
Department of Electrical Engineering



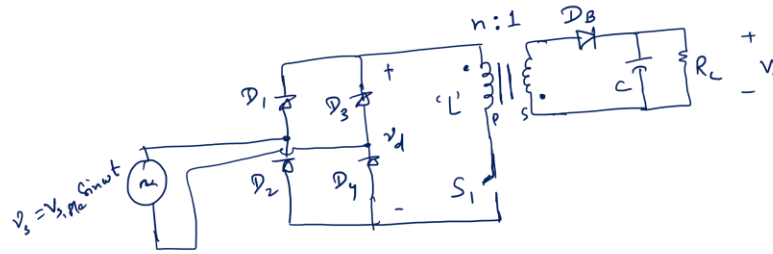
# Recap



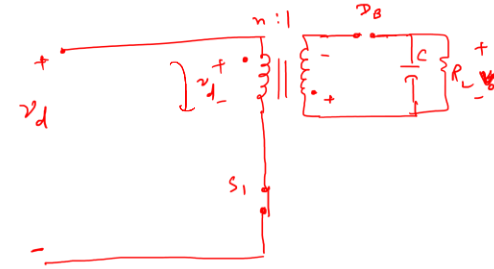
DCM mode



# Flyback based PFC Converter



⇒



$$v_d = |v_s|$$

$d(t) \rightarrow$  duty ratio of switch ' $S_1$ ' that varies with time ' $t$ '

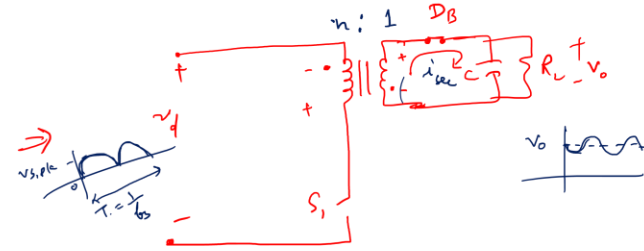
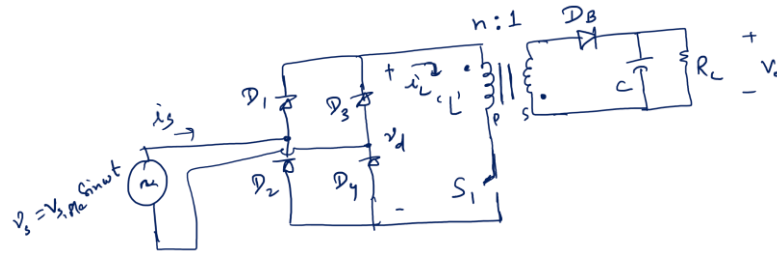
$S_1 \rightarrow$  is switching with frequency  $\omega_{sw}$   
 $\Rightarrow \omega_{sw} \gg \omega_s$

$\Rightarrow$  during  $\frac{d(t)T_s}{\text{period}} \Rightarrow$  the ' $S_1$ ' is ON  
 $\Rightarrow v_L = |v_s|$

# Flyback based PFC Converter

$$(1-d(t))I_s$$

$$I_s = \frac{1}{f_{sw}}$$



$(1-d(t))I_s \rightarrow$  the  $S_1$  is off  $\Rightarrow D_B$  is forward biased  
 $\Rightarrow$  Core is deenergized, as the flux in the core comes back

$$\Rightarrow V_L = -nV_o$$

$\Rightarrow$  Then, apply volt-sec balance in half-line cycle

$$\frac{1}{T/2} \left[ \int_0^{T/2} \left[ d(t) \cdot I_s \cdot |V_s| + (1-d(t)) \cdot I_s \cdot (-nV_o) \right] \cdot dt \right] = 0$$

$$\Rightarrow d(t) \cdot I_s \cdot |V_s| - nV_o \cdot (1-d(t)) I_s = 0$$

# Flyback based PFC Converter

$$|v_s| \cdot d(t) = n v_o (1 - d(t))$$

$$\Rightarrow |v_s| d(t) + n v_o d(t) = n v_o$$

$$\Rightarrow d(t) = \frac{n v_o}{|v_s| + n v_o}$$

$$\Rightarrow d(t) = \frac{1}{1 + \frac{|v_s|}{n v_o}}$$

$$\Rightarrow d(t) = \frac{1}{1 + \frac{v_{s, pk} \sin \omega t}{n v_o}}$$

# Flyback based PFC Converter

DCM operation of flyback based PFC converter

$$\Rightarrow d(t) < (1 - d(t))$$

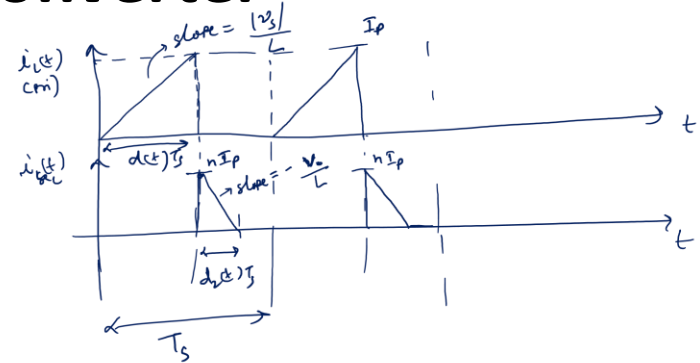
$d(t)T_s$  period

$$|v_s(t)| = \frac{L I_p}{d(t)T_s}$$

$$\Rightarrow I_p = \frac{d(t)T_s |v_s(t)|}{L}$$

$I_p$  varies with  $|v_s(t)|$

$$\begin{aligned} \Rightarrow \angle i_L T_s &= \frac{1}{T_s} \times \frac{1}{2} \times \frac{d(t)T_s |v_s(t)|}{L} \times d(t)T_s \\ &= \frac{1}{2} \frac{d^2(t)T_s |v_s(t)|}{L} \end{aligned}$$



( $L \rightarrow$  referred to primary side)

# Flyback based PFC Converter

$$I_{L, T_s} = \frac{|v_{s, \text{avg}}|}{R_e} \quad \Rightarrow \quad R_e = \frac{2L}{d^2 T_s} \longrightarrow \textcircled{1}$$

$$\Rightarrow P_o = \frac{V_o^2}{R_L}$$

$$\Rightarrow P_{in} = \frac{V_{s, \text{pk}}^2}{2 R_e}$$

Assume, the lossless converter

$$\Rightarrow P_o = P_{in}$$

$$\Rightarrow \frac{R_L}{R_e} = \frac{2V_o^2}{V_{s, \text{pk}}^2} \longrightarrow \textcircled{2}$$

$$\Rightarrow \text{from } \textcircled{1} \text{ \& } \textcircled{2} \\ \frac{R_L \cdot T_s \cdot d^2(t)}{2L} = \frac{2V_o^2}{V_{s, \text{pk}}^2}$$

$$\Rightarrow d^2(k) = \frac{4 V_o^2}{V_{s, pk}^2} \frac{L}{R_L T_s}$$

$$\Rightarrow d(k) = \sqrt{\frac{4 V_o^2}{V_{s, pk}^2} \cdot \frac{L}{R_L T_s}}$$

$$\Rightarrow d(k) = \frac{2 V_o}{V_{s, pk}} \sqrt{\frac{L}{R_L T_s}} \longrightarrow \textcircled{3}$$

In worst case scenario

$$d(k) = \frac{1}{1 + \frac{V_{s, pk}}{n V_o}} \longrightarrow \textcircled{4}$$

Substitute  $\textcircled{4}$  in  $\textcircled{3}$

$$\Rightarrow \frac{1}{1 + \frac{V_{s, pk}}{n V_o}} = \frac{2 V_o}{V_{s, pk}} \sqrt{\frac{L}{R_L T_s}}$$

$$\Rightarrow L = \frac{n^2 R_L T_s}{4 \left(1 + \frac{n V_o}{V_{s, pk}}\right)^2} \Rightarrow L_{critical}$$

$\Rightarrow L < L_{critical} \rightarrow$  DCM operation

$\Rightarrow L > L_{critical} \rightarrow$  CCM operation



$$L_{\text{critical}} = \frac{n^2 R_L T_s}{4 \left( 1 + \frac{n \hat{v}_o}{V_{s, \text{pk}}} \right)^2}$$

↙  
referred to primary side

$L < L_{\text{critical}} \rightarrow$  DCM is possible  
 if we can ensure, the  $\hat{v}$  value to be smaller than the minimum  $L_{\text{critical}}$  value, then we can always ensure the DCM operation

$$L_{\text{critical, min}} \Rightarrow R_L \text{ is min \& } V_{s, \text{pk}} \text{ is at Min.}$$

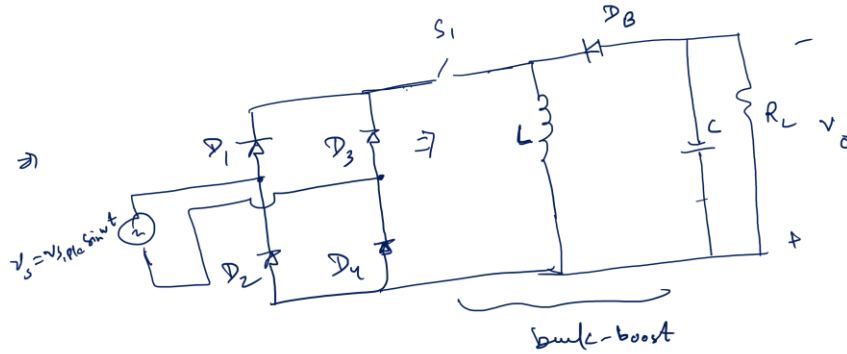
↓  
full load power

$L_{\text{critical, min}}$  has to be calculated for peak power demand and at Min. value input  $\hat{v}$  voltage

$$L < L_{\text{critical, min}} \Rightarrow \text{DCM is ensured}$$

### Advantage

- ① Isolation is incorporated
- ② voltage follower mode



- ⇒ buck-boost or Flyback operated in DCM has the resistive effective input impedance and thus, the current drawn from the source will be having sinusoidal variation.

# Thank You

