exercise 04 notebook

November 5, 2019

1 Programming assignment 2: Linear regression

```
[1]: import numpy as np

from sklearn.datasets import load_boston
from sklearn.model_selection import train_test_split
```

1.1 Your task

In this notebook code skeleton for performing linear regression is given. Your task is to complete the functions where required. You are only allowed to use built-in Python functions, as well as any numpy functions. No other libraries / imports are allowed.

1.2 Exporting the results to PDF

Once you complete the assignments, export the entire notebook as PDF and attach it to your homework solutions. The best way of doing that is 1. Run all the cells of the notebook. 2. Export/download the notebook as PDF (File -> Download as -> PDF via LaTeX (.pdf)). 3. Concatenate your solutions for other tasks with the output of Step 2. On a Linux machine you can simply use pdfunite, there are similar tools for other platforms too. You can only upload a single PDF file to Moodle.

Make sure you are using nbconvert Version 5.5 or later by running jupyter nbconvert --version. Older versions clip lines that exceed page width, which makes your code harder to grade.

1.3 Load and preprocess the data

I this assignment we will work with the Boston Housing Dataset. The data consists of 506 samples. Each sample represents a district in the city of Boston and has 13 features, such as crime rate or taxation level. The regression target is the median house price in the given district (in \$1000's).

More details can be found here: http://lib.stat.cmu.edu/datasets/boston

```
[2]: X , y = load_boston(return_X_y=True)

# Add a vector of ones to the data matrix to absorb the bias term
# (Recall slide #7 from the lecture)
X = np.hstack([np.ones([X.shape[0], 1]), X])
# From now on, D refers to the number of features in the AUGMENTED dataset
# (i.e. including the dummy '1' feature for the absorbed bias term)

# Split into train and test
test_size = 0.2
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=test_size)
```

1.4 Task 1: Fit standard linear regression

1.5 Task 2: Fit ridge regression

```
Regression targets.

reg_strength : float
    L2 regularization strength (denoted by lambda in the lecture)

Returns
-----
w : array, shape [D]
    Optimal regression coefficients (w[0] is the bias term).

"""
# TODO
I = np.identity(X.shape[1])
w = np.dot(np.dot(np.linalg.inv(np.dot(X.T,X) + reg_strength*I),X.T),y)
return w
```

1.6 Task 3: Generate predictions for new data

1.7 Task 4: Mean squared error

```
[6]: def mean_squared_error(y_true, y_pred):
    """Compute mean squared error between true and predicted regression targets.

Reference: https://en.wikipedia.org/wiki/Mean_squared_error
```

```
Parameters
------
y_true: array
    True regression targets.

y_pred: array
    Predicted regression targets.

Returns
-----
mse: float
    Mean squared error.

"""
# TODO
mse = np.sum(np.square(y_pred - y_true))/y_true.shape[0]
return mse
```

1.8 Compare the two models

The reference implementation produces * MSE for Least squares ≈ 23.98 * MSE for Ridge regression ≈ 21.05

You results might be slightly (i.e. $\pm 1\%$) different from the reference soultion due to numerical reasons.

```
[7]: # Load the data
    np.random.seed(1234)
     X , y = load_boston(return_X_y=True)
     X = np.hstack([np.ones([X.shape[0], 1]), X])
     test size = 0.2
     X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=test_size)
     # Ordinary least squares regression
     w_ls = fit_least_squares(X_train, y_train)
     y_pred_ls = predict_linear_model(X_test, w_ls)
     mse_ls = mean_squared_error(y_test, y_pred_ls)
     print('MSE for Least squares = {0}'.format(mse_ls))
     # Ridge regression
     reg_strength = 1
     w_ridge = fit_ridge(X_train, y_train, reg_strength)
     y_pred_ridge = predict_linear_model(X_test, w_ridge)
     mse_ridge = mean_squared_error(y_test, y_pred_ridge)
     print('MSE for Ridge regression = {0}'.format(mse_ridge))
```

```
MSE for Least squares = 23.96457138495337
MSE for Ridge regression = 21.0349312159183
```

[]:[