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State Finished

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Time taken 30 mins 1 sec

Grade 6.50 out of 10.00 (65%)

Question 1

Correct

Mark 1.00 out of 1.00

Which of the following statements is correct?

- ☐ a. $\sum_{n=1}^{\infty} \cos n$ is divergent and the series $\sum_{n=1}^{\infty} (\cos n)/n^2$ is divergent.
- ☐ b. $\sum_{n=1}^{\infty} \cos n$ is convergent and the series $\sum_{n=1}^{\infty} (\cos n)/n^2$ is divergent.
- ☒ c. $\sum_{n=1}^{\infty} \cos n$ is divergent and the series $\sum_{n=1}^{\infty} (\cos n)/n^2$ is convergent. ✓
- ☐ d. $\sum_{n=1}^{\infty} \cos n$ is convergent and the series $\sum_{n=1}^{\infty} (\cos n)/n^2$ is convergent.

The correct answer is:

$\sum_{n=1}^{\infty} \cos n$ is divergent and the series $\sum_{n=1}^{\infty} (\cos n)/n^2$ is convergent.

Question 2

Correct

Mark 1.00 out of 1.00

. Evaluate $\lim_{x \rightarrow 0} \frac{\log x}{\cot x}$

Answer: 0



The correct answer is: 0

Question 3

Correct

Mark 1.00 out of 1.00

Find $\lim (xe^{-nx})$ for $x \in \mathbb{R}, x \geq 0$.

Answer: 

The correct answer is: 0

Question 4

Correct

Mark 1.00 out of 1.00

Find $\lim (nx / (1 + n^2x^2))$ for all $x \in \mathbb{R}$.

Answer: 

The correct answer is: 0

Question 5

Partially correct

Mark 0.50 out of 1.00

Let s_n be a sequence of real numbers on a bounded set S , where $\liminf s_n \neq \limsup s_n$. Which of the following is true?

- ☐ $\lim s_n$ does not exist.
- ☐ s_n has an infinite number of dominant terms.
- ☒ $\liminf s_n < \limsup s_n$ ✓
- ☐ s_n is not Cauchy.
- ☒ There exists a convergent subsequence. ✓

The correct answers are:

$\lim s_n$ does not exist.

s_n is not Cauchy.

$\liminf s_n < \limsup s_n$

There exists a convergent subsequence.

Question 6

Not answered

Marked out of 1.00

Let $a, b \in \mathbb{R}$ and $a < b$. Which of the following statement(s) is/are true?

- ☐ There exists a continuous function $f:(a,b) \rightarrow [a,b]$ such that f is onto.
- ☐ There exists a continuous function $f:[a,b] \rightarrow (a,b)$ such that f is onto.
- ☐ There exists a continuous function $f:(a,b) \rightarrow [a,b]$ such that f is one-one.
- ☐ There exists a continuous function $f:[a,b] \rightarrow (a,b)$ such that f is one-one.

The correct answers are:

There exists a continuous function $f:[a,b] \rightarrow (a,b)$ such that f is one-one.,

There exists a continuous function $f:(a,b) \rightarrow [a,b]$ such that f is one-one.,

There exists a continuous function $f:(a,b) \rightarrow [a,b]$ such that f is onto.

Question 7

Incorrect

Mark 0.00 out of 1.00

Let A and B be bounded non-empty sets. Which of the following statements would be equivalent to saying that $\sup(A) = \inf(B)$

- ☐ a. There exists $a \in A$ and $b \in B$ such that $a \leq b$. However, for any $\epsilon > 0$, there does not exist $a \in A$ and $b \in B$ for which $a + \epsilon \leq b$.
- ☐ b. For every $a \in A$ and every $b \in B$, we have $a \leq b$. Also, for every $\epsilon > 0$ there exists $a \in A$ and $b \in B$ such that $b - a < \epsilon$.
- ☐ c. For every $a \in A$ there exists a $b \in B$ such that $a + \epsilon < b$. Also, for every $b \in B$ there exists an $a \in A$ such that $b + \epsilon < a$.
- ☒ d. For every $a \in A$ there exists a $b \in B$ such that $a + \epsilon < b$. ❌

The correct answer is:

For every $a \in A$ and every $b \in B$, we have $a \leq b$. Also, for every $\epsilon > 0$ there exists $a \in A$ and $b \in B$ such that $b - a < \epsilon$.

Question 8

Correct

Mark 1.00 out of 1.00

What is the cardinality of the set of real numbers in the closed interval $[0, 1]$?

- ☐ Countable
- ☐ Finite
- ☒ Uncountable ✔
- ☐ Countably infinite

The correct answer is:

Uncountable

Question 9

Correct

Mark 1.00 out of 1.00

The value of $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$

Answer: ✔

The correct answer is: 2.72

Question 10

Incorrect

Mark 0.00 out of 1.00

Let A and B be bounded non-empty sets. Which of the following statements would be equivalent to saying that $\inf(A) \leq \inf(B)$?

- ☐ a. For every $a \in A$ and every $b \in B$, we have $a \leq b$.
- ☐ b. For every $b \in B$ and $\epsilon > 0$ there exists an $a \in A$ such that $a < b + \epsilon$.
- ☐ c. There exists $a \in A$ and $b \in B$ such that $a < b$.
- ☒ d. For every $a \in A$ there exists a $b \in B$ such that $a \leq b$ ✖

The correct answer is:

For every $b \in B$ and $\epsilon > 0$ there exists an $a \in A$ such that $a < b + \epsilon$.