

SECTION: A

1. Prove that $\|u+v\| = \|u-v\|$ if and only if u and v are orthogonal to each other.
2. Show that $\|u+v\|^2 = \|u\|^2 + \|v\|^2 + 2\langle u, v \rangle$
3. Show that $\langle u+v, u-v \rangle = \|u\|^2 - \|v\|^2$
4. Show that $d(u, v) = \sqrt{\|u\|^2 + \|v\|^2}$ if and only if u and v are orthogonal to each other.
5. Prove that $\|u\|^2 + \|v\|^2 = (1/2)\|u+v\|^2 + (1/2)\|u-v\|^2$ [2+2+2+2+2=10]

[Here $\langle u, v \rangle$]**SECTION: B**

1. Use Gauss Jordan Method to find the inverse of the matrix

$$\begin{pmatrix} 0 & -1 & 1 & 0 \\ 2 & 1 & 0 & 2 \\ 1 & -1 & 3 & 0 \\ 0 & 1 & 1 & -1 \end{pmatrix}$$

2. Using induction, prove that for all $n \geq 1$, $(A_1 + A_2 + \dots + A_n)^T = A_1^T + A_2^T + \dots + A_n^T$
3. Express $M = \begin{pmatrix} b & c \\ 1 & 0 \end{pmatrix}$, ($b \neq 0, c \neq 0$) as a product of elementary matrices

[5+5+5=15]

END
