

End-Sem: EC2.205-Radio Frequency based Sensors design: Principles and Applications

Time: 2 Hrs.

Max. Marks: 45

Question 1 Attempt all 4 questions

(5×4=20)

- a) Define S-parameters and explain the physical significance of S_{11} , S_{12} , S_{21} , and S_{22} . A two-port network has $S_{11} = 0.95$, $S_{22} = 0.1$. Explain how Port 1 behaves significantly differently from Port 2 regarding impedance matching and power handling.?
- b) What is the physical significance of the Standing Wave Ratio (SWR) in transmission lines? How is it related to the reflection coefficient? An RF transmission line has a reflection coefficient $|\Gamma| = 0.3$. Calculate the Standing Wave Ratio (SWR).?
- c) Explain the factors that influence the choice of a transmission line in high-frequency applications.?
- d) Derive the differential form of Faraday's Law from its integral form using Stokes' theorem. Then, explain its physical meaning regarding a changing magnetic field producing an induced electric field in different media (free space vs dielectric).?

Stokes' Theorem (Statement)

Stokes' Theorem states that the line integral of a vector field around a closed curve is equal to the surface integral of the curl of the vector field over the surface bounded by the curve.

Mathematically:

$$\oint_C \vec{F} \cdot d\vec{r} = \iint_S (\nabla \times \vec{F}) \cdot d\vec{A}$$

Where:

- C = Closed curve or boundary of the surface S
- \vec{F} = Vector field
- $d\vec{r}$ = Infinitesimal element along the curve C
- $\nabla \times \vec{F}$ = Curl of the vector field
- $d\vec{A}$ = Infinitesimal area vector of the surface S

Question 2: Attempt any two of the following questions

(10×2=20)

a) The characteristic impedance Z_0 of a microstrip line is:

$$Z_0 = \begin{cases} \frac{60}{\sqrt{\epsilon_{eff}}} \ln \left(\frac{8h}{w} + \frac{w}{4h} \right) & w/h \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_{eff}} [w/h + 1.393 + 0.667 \ln(w/h + 1.444)]} & w/h \geq 1 \end{cases}$$

A VNA with 50Ω source impedance is connected to a 250Ω load through a lossless quarter-wave microstrip line. Given specifications: frequency $f = 10$ GHz, substrate height $h = 1$ mm, $\epsilon_r = 4.4$, $\epsilon_{eff} = 3.2$ and $w/h \leq 1$.

Answer the following: (i) Find the required Z_0 of the quarter-wave microstrip line to match the source and load impedances. (ii) Calculate the width w of the quarter wave microstrip line (iii) the physical length l , and (iv) the electrical length for $w/h \leq 1$.

(b) A short-circuited coaxial transmission line is shown in Figure 1, given:

$$Z_0 = 65 + j38 \, \Omega, \quad \gamma = 0.7 + j2.5 \, \text{m}^{-1}, \quad l = 0.8 \, \text{m}.$$

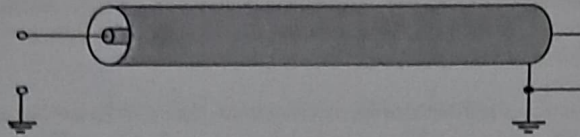


Figure 1: Short-circuited coaxial transmission line.

- i. Calculate the input impedance of the short-circuited coaxial transmission line.
- ii. Now, assume that the coaxial transmission line is lossless, while all other transmission line parameters remain unchanged. Determine the new values of γ and Z_0 . Also, compute the minimum length of this lossless line required to transform the short-circuit termination into an open circuit at the input.
- iii. Again, assume a lossless line, but now let the length of the coaxial line be $l = x$ while all other transmission line parameters remain unchanged. Plot the imaginary part of the input impedance versus the electrical length. Determine whether the input impedance behaves as an inductor or a capacitor over electrical length and specify the electrical length where each behavior occurs.

[Useful formula]

$$\tanh(x + jy) = \frac{\tanh(x) + j \tanh(y)}{1 + j \tanh(x) \tanh(y)}$$

(c) (i) Define and explain the following terms in the context of RF sensors: For each term, provide: The formula (if applicable), the physical significance, and the factors that affect the term.

- a) Sensitivity
- b) Selectivity
- c) Response Time
- d) Insertion Loss
- e) Quality Factor (Q).
- f) Bandwidth.
- g) Resonance frequency.

(ii) An RF sensor operates at a frequency of 3 GHz with a sensor bandwidth of 150 MHz. The sensor is connected to a transmission line with the following parameters:

- Operating Frequency (f_0) = 3 GHz
- Sensor Bandwidth (BW) = 150 MHz
- Load Impedance (Z_L) = 75 Ω
- Characteristic Impedance (Z_0) = 50 Ω
- Input Power = -10 dBm
- Output Power = -12 dBm.

Find the following:

- h) Quality Factor (Q) of the sensor.
- i) Return Loss (RL) of the sensor.
- j) Insertion loss

Question 3: Multiple Choice Questions (MCQs)

(Note: Each question has only one correct answer)

(i) Which of the following materials will have the smallest skin depth for the same RF frequency?

- a) Copper (high conductivity)
- b) Carbon (low conductivity)
- c) Air
- d) Glass

(ii) Which of the following primary constants determines the characteristic impedance of a transmission line?

- a) Resistance (R) and Inductance (L)
- b) Capacitance (C) and Conductance (G)
- c) Resistance (R) and Capacitance (C)
- d) Resistance (R), Inductance (L), Capacitance (C), and Conductance (G).

(iii) What does the recovery time of an RF sensor represent?

- a) The time it takes for the sensor to detect an incoming RF signal
- b) The time required for the sensor to return to its baseline state after the signal is removed
- c) The delay between input and output power measurement
- d) The duration the sensor remains active after power is turned off

(iv) Which of the following is a direct result of signal reflection caused by impedance mismatch in a transmission line?

- a) Increase in modulation index
- b) Formation of standing waves on the transmission line
- c) Reduction in signal frequency
- d) Improvement in signal quality

(v) An RF sensor detects electromagnetic (EM) waves primarily by:

- a) Measuring the amplitude of the incident electric field only
- b) Detecting the frequency and phase of the EM wave
- c) Measuring the temperature fluctuations caused by the wave
- d) Generating an opposite EM wave to cancel out the incoming wave

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