

Systems Thinking

Assignment 1

NOTE: Any kind of copying or plagiarism, within peers or online sources will lead to a strict penalty. Please give proper steps and explanations for all the questions, highlighting final results.

Deadline: 18/09/2024 11.59 PM

Questions

1. *Do Laplace Transformation of the Following:*

- Ramp function

$$y(t) = \begin{cases} 0, & \text{if } t < 0 \\ At, & \text{if } t > 0 \end{cases}$$

- Sinusoidal function

$$y(t) = \begin{cases} 0, & \text{if } t < 0 \\ A \sin wt, & \text{if } t > 0 \end{cases}$$

- Pulse Functions

$$y(t) = \begin{cases} \frac{A}{t_0}, & \text{if } 0 < t < t_0 \\ 0, & \text{if } t < 0, t_0 < t \end{cases}$$

- Given Function

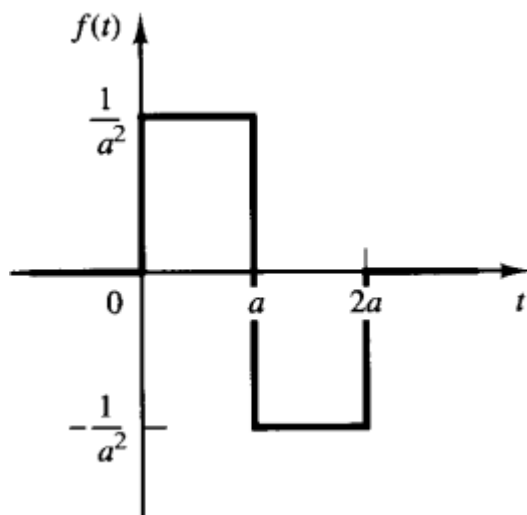
$$y(t) = \begin{cases} 0, & \text{if } t < 0 \\ te^{-3t}, & \text{if } t \geq 0 \end{cases}$$

- Given Function, θ is constant

$$y(t) = \begin{cases} 0, & \text{if } t < 0 \\ \sin(\omega t + \theta), & \text{if } t \geq 0 \end{cases}$$

2. *Given $\mathcal{L}[f(t)] = \frac{1}{s(s+1)}$, What is $\lim_{t \rightarrow \infty} f(t)$?*

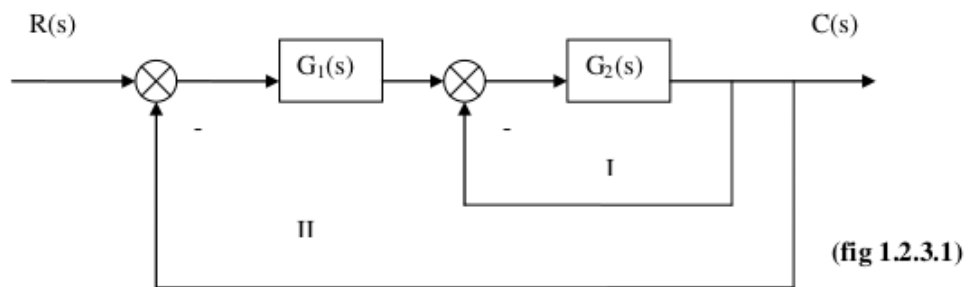
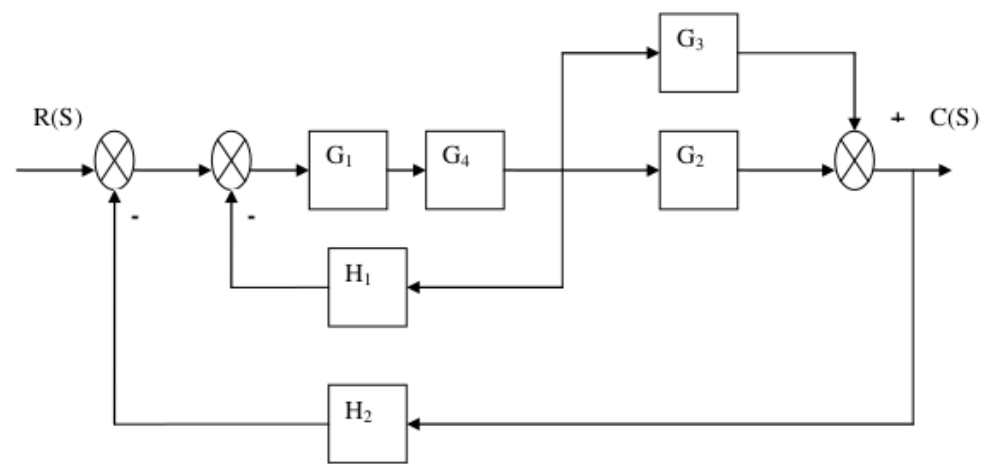
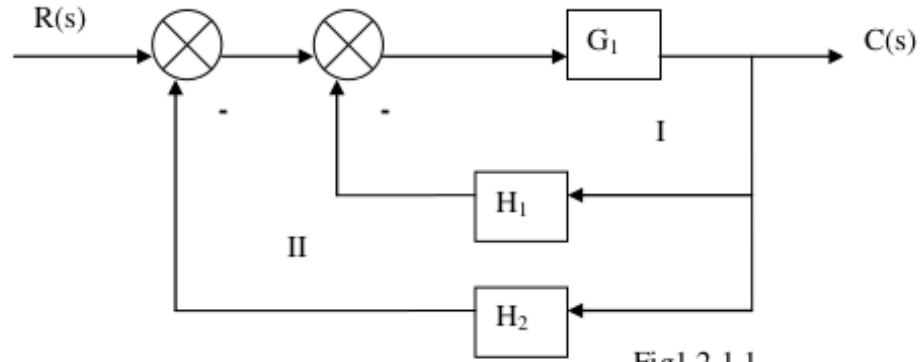
3. *Find the Laplace Transform of the Function Given Below and Also Find the Limiting Value as a Approaches Zero:*



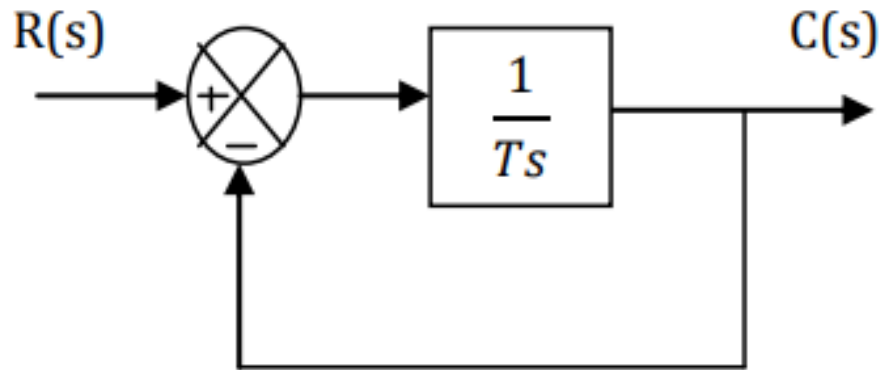
4. *Find Time Domain Functions for the Following:*

- $Y(s) = \frac{2s}{(s+1)(s+2)}$
- $Y(s) = \frac{2s}{(s+1)^2(s+2)}$
- $Y(s) = \frac{2}{3s^4}$
- $Y(s) = \frac{3s+2}{s^2+25}$
- $Y(s) = \frac{1}{3-4s} + \frac{3-2s}{s^2+49}$
- $Y(s) = \frac{4(s-1)}{(s-1)^2+4}$

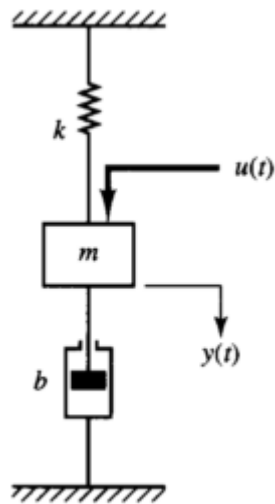
5. Find Transfer Functions of Following Systems:



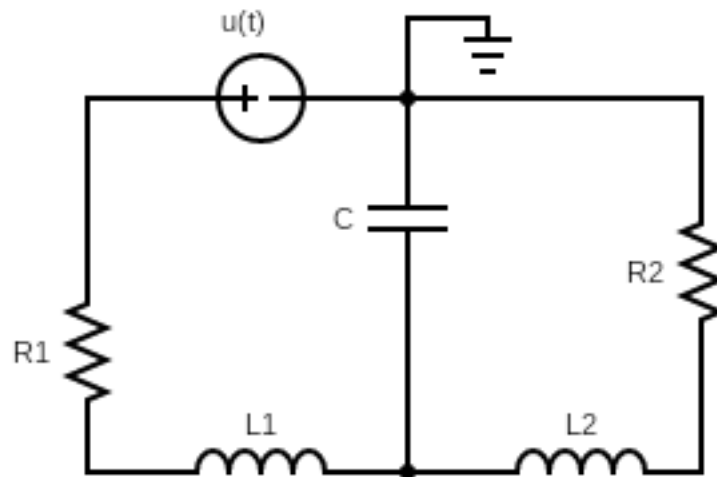
6. *Derive the Expressions and Draw the Response of First Order System for Unit Step Input:*



7. *Consider the Following Mechanical System. Assume That It's a Linear System. Derive Its State Equation and Output Equation:*



8. *Give a State-Space Model for the given electrical network. Give proper State and Output equations. Voltage across R2 is the output of the system.*

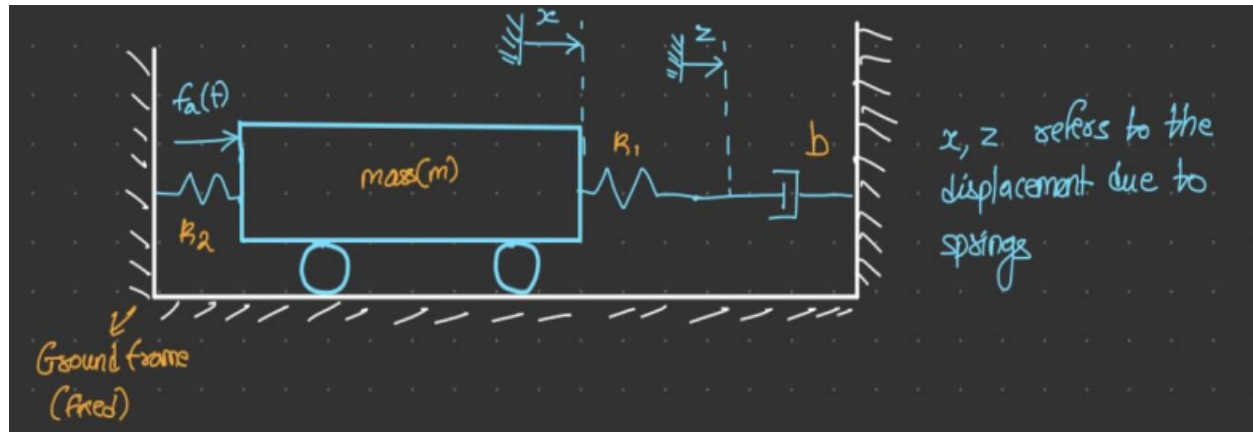


9. *Construct a state model for a system given by the differential equation:*

$$\frac{d^3y}{dt^3} + 6\frac{d^2y}{dt^2} + 11\frac{dy}{dt} + 6y + u = 0$$

Also, give block diagram for the state representation.

10. *Derive the state space model for the mechanical system shown in the figure considering $f_a(t)$ as the input and z as the output.*



11. *Consider a system having open loop transfer function*

$$G(s) = \frac{150(s+1)}{(s+5)(s+3)}$$

For the above unity feedback system, find the steady-state errors for the inputs

- (i) $tu(t)$
- (ii) $t^2u(t)$

where $u(t)$ is the step input.

12. *Prove the following relation. Here A, B, C, D denote the usual state variables for the state space equations and $G(s)$ denotes a single input - single output transfer function.*

$$G(s) = C(sI - A)^{-1}(B + D)$$