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$\Delta_r S^\ominus > 0$ if there is a net formation of gas in a reaction, and
 < 0 if there is a net consumption of gas

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General observation : Systems tend to evolve s. t. energy decreases in the process, but total energy of universe remains constant

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so we need better criteria for spontaneity that depend only on the system

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Legendre transform : changing the natural variables :

$$y(x) = mx + c; \quad c(m) = -xm + y; \quad m = \frac{dy}{dx}$$

$$\text{Information from } (x, y) \equiv \text{Information from } (m, c)$$

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Try with $U \equiv U(S, V); \quad \left(\frac{\partial U}{\partial S}\right)_V T, \quad \therefore \text{Legendre transform,}$

$$f = -S \left(\frac{\partial U}{\partial S}\right)_V + U = U - TS$$

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most negative value of dw , and hence the max. energy that can be obtained from system as work, is

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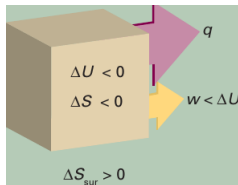
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to generate enough entropy in surroundings

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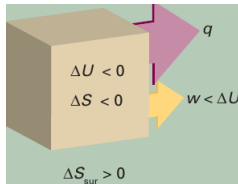
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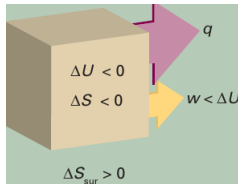
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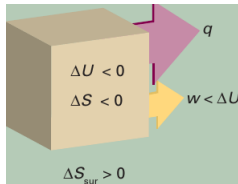
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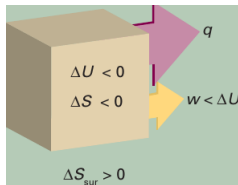
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TS = energy stored as thermal motion, unavailable part of U

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some energy (no more than the value of $T\Delta S$)

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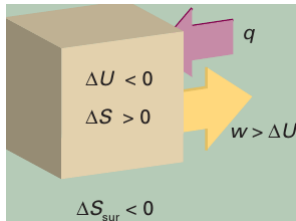
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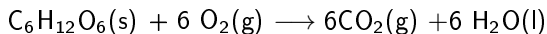
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Nature is providing a tax refund



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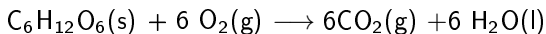


$$\Delta_r U^\ominus = -2808 \text{ kJ mol}^{-1} \text{ and } \Delta_r S^\ominus = 259.1 \text{ J K}^{-1}\text{mol}^{-1}$$

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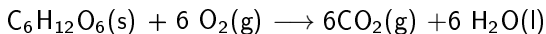
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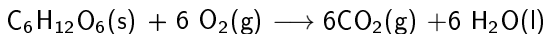
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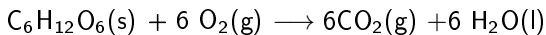
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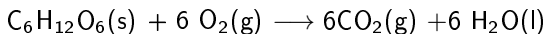
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system can draw in energy from the surroundings (reducing their entropy) and make it available for work

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$$\Delta_r G^\ominus = \sum_{\text{products}} \nu \Delta_f G^\ominus - \sum_{\text{reactants}} \nu \Delta_f G^\ominus$$

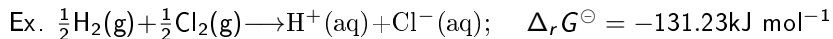
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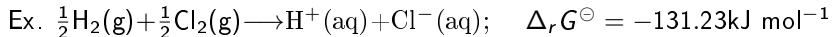
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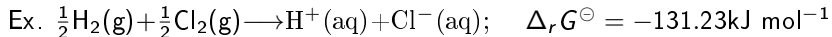
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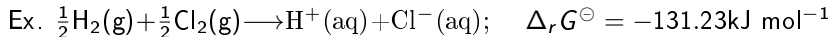


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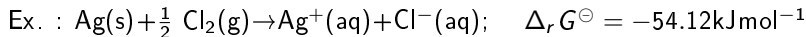
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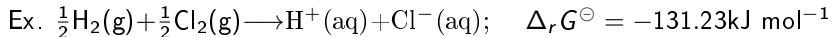
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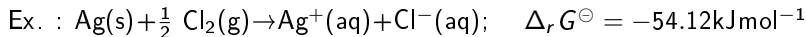
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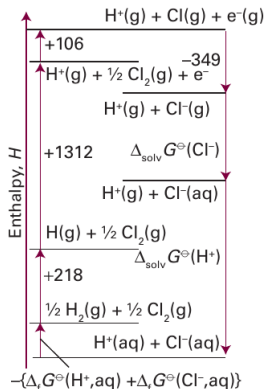
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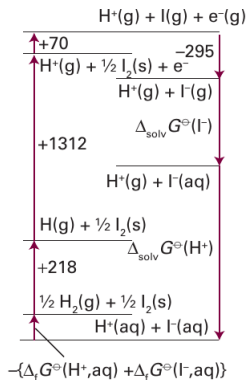
$$\Delta_f G^\ominus(\text{Ag}^+, \text{aq}) = -54.12 + 131.23 = 77.11 \text{ kJ mol}^{-1}$$

thermodynamic cycle:

solvation of (a) chloride and (b) iodide ions:



$\Delta_f G^\ominus$ of an ion X is not determined by properties of X alone but includes contributions from dissociation, ionization, and hydration of hydrogen



Gibbs energy of solvation of individual ions

$$\Delta_f G^\ominus(Cl^-, aq) = 1287 \text{ kJ mol}^{-1} + \Delta_{solv} G^\ominus(H^+) + \Delta_{solv} G^\ominus(Cl^-)$$

Born equation :

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$\Delta_{\text{sol}} G^{\ominus}$ = work of transferring an ion from a vacuum into solvent

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Ex. : $\Delta_{\text{solv}} G^{\ominus} (\text{Cl}^{-1}) - \Delta_{\text{solv}} G^{\ominus} (\text{I}^{-1})$

$$= -\left(\frac{1}{181} - \frac{1}{220}\right) \times (6.86 \times 10^4 \text{ kJ mol}^{-1}) = -67 \text{ kJ mol}^{-1}$$

Chemical potential : $\mu = \left(\frac{\partial G}{\partial n_i} \right)_{p, T, n_j, j \neq i}$

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For irreversible processes, $dS > \frac{1}{T}dU + \frac{p}{T}dV - \frac{\mu}{T}dN$

analysis of one-component, two-phase isolated system :

definition of an isolated system : the following must be constant

1. internal energy, U
2. total volume, V
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and

$$dS = dS^{(1)} + dS^{(2)} = \frac{1}{T^{(1)}}dU^{(1)} + \frac{1}{T^{(2)}}dU^{(2)} + \frac{p^{(1)}}{T^{(1)}}dV^{(1)} + \frac{p^{(2)}}{T^{(2)}}dV^{(2)} - \frac{\mu^{(1)}}{T^{(1)}}dN^{(1)} - \frac{\mu^{(2)}}{T^{(2)}}dN^{(2)}$$

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3. thermal and mechanical equilibrium, flexible, permeable, diathermal wall

$$\implies T^{(1)} = T^{(2)} \text{ and } p^{(1)} = p^{(2)}$$

impermeable, rigid, diathermal wall \Rightarrow

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$$\therefore dU^{(1)} + dU^{(2)} = 0 \implies dU^{(1)} = -dU^{(2)} = dU \text{ (say)}$$

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if $dU > 0$ (flow of energy from phase 2 to phase 1),

then $T^{(1)} < T^{(2)}$, i.e. energy must flow from higher to lower temperature for thermal equilibrium to be reached

At $T^{(1)} = T^{(2)}$ (thermal equilibrium), $dS = 0$

Since there is no work involved, the energy here is heat

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if $dV > 0$ (wall moves away from phase 1 to phase 2),

then $p^{(1)} > p^{(2)}$, i.e. mechanical equilibrium requires movement of the wall from higher pressure to lower pressure region

When $p^{(1)} = p^{(2)}$ (mechanical equilibrium), $dS = 0$

thermal and mechanical equilibrium, flexible, permeable, diathermal wall

$$\Rightarrow \begin{array}{l} T^{(1)} = T^{(2)} \\ p^{(1)} = p^{(2)} \end{array}$$

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if $dN > 0$ (mass moves from phase 2 to phase 1)

then $\mu^{(2)} > \mu^{(1)}$, i.e., mass moves spontaneously
from higher to lower chemical potentials

When $\mu^{(1)} = \mu^{(2)}$ (chemical equilibrium), $dS = 0$

