

Sliding Window Technique

This technique shows how a nested for loop in some problems can be converted to a single for loop to reduce the time complexity.

Example :-

Given an array of integers of size 'n'.

Calculate the maximum sum of 'k' consecutive elements in the array.

Input : arr[] = {100, 200, 300, 400}

k = 2

output = 700

Input : arr[] = {1, 4, 2, 10, 23, 3, 1, 0, 20}

k = 4

output = 39

We get maximum sum by adding subarray {4, 2, 10, 23} of size 4.

Input : arr[] = {2, 3}

k = 3

output = Invalid

There is no subarray of size 3 as size of whole array is 2.

So, let's analyze the problem with **Brute Force Approach**.

We start with first index and sum till **k-th** element.

We do it for all possible consecutive blocks or groups of k elements.

This method requires nested for loop, the outer for loop starts with the starting element of the block of k elements and the inner or the nested loop will add up till the k-th element.

Consider the below implementation :

```
class Test {  
    // Returns maximum sum in a subarray of size k.  
    static int maxSum(int arr[], int n, int k)  
    {  
        // Initialize result  
        int max_sum = Integer.MIN_VALUE;
```

```

// Consider all blocks starting with i.
for (int i = 0; i < n - k + 1; i++) {
    int current_sum = 0;
    for (int j = 0; j < k; j++)
        current_sum = current_sum + arr[i + j];

    // Update result if required.
    max_sum = Math.max(current_sum, max_sum);
}

return max_sum;
}

public static void main(String[] args)
{
    int arr[] = { 1, 4, 2, 10, 2, 3, 1, 0, 20 };
    int k = 4;
    int n = arr.length;
    System.out.println(maxSum(arr, n, k));
}
}

```

Sliding Window Technique

The technique can be best understood with the window pane in bus, consider a window of length **n** and the pane which is fixed in it of length **k**.

Consider, initially the pane is at extreme left i.e., at 0 units from the left.

Now, co-relate the window with array `arr[]` of size **n** and pane with `current_sum` of size **k** elements.

Now, if we apply force on the window such that it moves a unit distance ahead.

The pane will cover next **k** consecutive elements.

Consider an array `arr[] = {5, 2, -1, 0, 3}` and value of **k** = 3 and **n** = 5

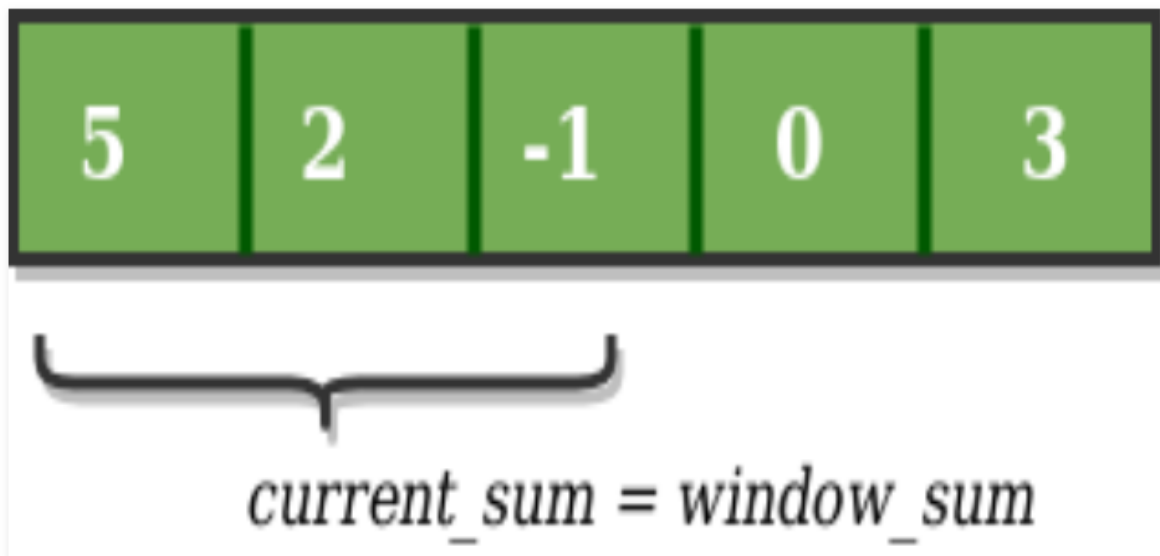
Applying sliding window technique :

1. We compute the sum of first **k** elements out of **n** terms using a linear loop and store the sum in variable `window_sum`.
2. Then we will graze linearly over the array till it reaches the end and simultaneously keep track of maximum sum.
3. To get the current sum of block of **k** elements just subtract the first element from the previous block and add the last element of the current block .

The below representation will make it clear how the window slides over the array.

This is the initial phase where we have calculated the initial window sum starting from index 0 .

At this stage the window sum is 6. Now, we set the `maximum_sum` as `current_window` i.e 6.



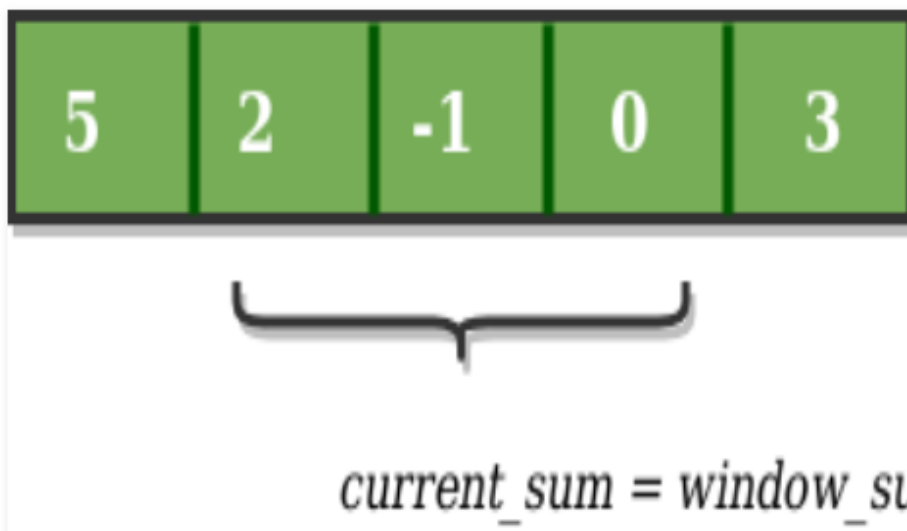
Now, we slide our window by a unit index. Therefore, now it discards 5 from the window and adds 0 to the window.

Hence, we will get our new window sum by subtracting 5 and then adding 0 to it.

So, our window sum now becomes 1.

Now, we will compare this window sum with the `maximum_sum`.

As it is smaller we won't change the `maximum_sum`.

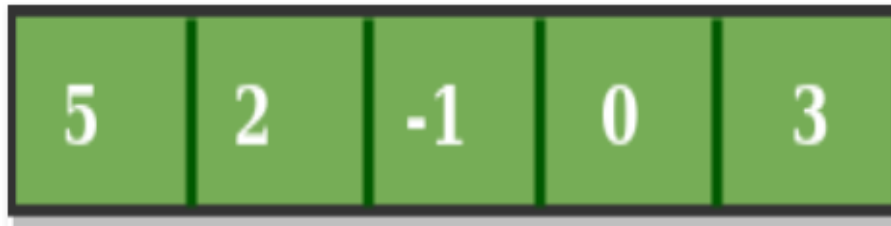


Similarly, now once again we slide our window by a unit index and obtain the new window sum to be 2.

Again we check if this current window sum is greater than the `maximum_sum` till now.

Once, again it is smaller so we don't change the `maximum_sum`.

Therefore, for the above array our `maximum_sum` is 6.



$$\text{current_sum} = \text{window_sum} + (-2) + (3)$$

// Java code for O(n) solution for finding maximum sum of a subarray of size k

```
class Test {  
  
    // Returns maximum sum in a subarray of size k.  
    static int maxSum(int arr[], int n, int k)  
    {  
        // n must be greater  
        if (n < k) {  
            System.out.println("Invalid");  
            return -1;  
        }  
  
        // Compute sum of first window of size k  
        int max_sum = 0;  
        for (int i = 0; i < k; i++)  
            max_sum += arr[i];  
  
        // Compute sums of remaining windows by  
        // removing first element of previous  
        // window and adding last element of  
        // current window.  
        int window_sum = max_sum;  
        for (int i = k; i < n; i++) {  
            window_sum += arr[i] - arr[i - k];  
            max_sum = Math.max(max_sum, window_sum);  
        }  
  
        return max_sum;  
    }  
  
    public static void main(String[] args)
```

```
{  
    int arr[] = { 1, 4, 2, 10, 2, 3, 1, 0, 20 };  
    int k = 4;  
    int n = arr.length;  
    System.out.println(maxSum(arr, n, k));  
}  
}
```