

Statistic Test.

①

1) ANOVA

Var 1	Var 2	Var 3
Sum of x 500	530	440
N = 30		

$$C_x = \frac{\sum(x)^2}{N} = \frac{(500 + 530 + 440)^2}{30} = \frac{(1470)^2}{30}$$

$$= \frac{2160900}{30} = 72,030$$

Sum of Squares.

$$S_{sr} = \sum x^2 - C_x = (26,742 + 28,586 + 20,422) - 72,030$$

$$S_{sr} = 3720$$

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Sum of Squares among group:

$$SSA = \frac{(\sum x^2)}{n} - C_x$$

$$\left(\frac{(500)^2}{10} + \frac{(530)^2}{10} + \frac{(440)^2}{10} \right) - 72,030$$

A	B	C
729	3969	2704
1849	1849	3600
4096	2704	1369
3844	3364	1600
1936	2916	529
2916	2500	1521
3249	4225	3025
2401	2809	2704
9681	1849	1849
4761	2401	1521
$\sum x^2$ 35,382	28,586	20,422
26,742		

$$\left(\frac{250,000}{10} + \frac{280,900}{10} + \frac{193,600}{10} \right) - C_x$$

$$= 25,000 + 28,090 + 19,360$$

$$= 72,450 - 22,030$$

$$SSA = 420$$

Sum of Squares within

(3)

$$SSW = SST - SSA$$
$$= 3720 - 420$$

$$SSW = 3300$$

Mean of Sum of Squares among group:

$$M_{SSA} = \frac{SSA}{K-1} = \frac{420}{3-1} = \frac{420}{2} = 210$$

Mean of Sum of Squares within

$$M_{SSW} = \frac{SSW}{N-K} = \frac{3300}{30-3} = \frac{3300}{27} = 122.22$$

$$F\text{-Ratio} : \frac{M_{SSA}}{M_{SSW}} = \frac{210}{122.22} = 1.72$$

F table

$$1.72 = 3.10$$

2) Anova for Slope

(4)

F	E	U
10.76	12.72	11.88
15.05	13.91	5.86
17.01	6.43	13.46
5.07	11.99	9.9
19.5	18.79	3.95
8.16	20.73	3.44
10.38	9.6	7.11
6.75	17.4	15.7
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Σx 92.68	110.77	71.3

Σx^2

115.77 115.77	161.79	141.13
226.50	193.48	34.33
289.34	41.34	181.17
25.70	125.21	98.01
380.25	353.06	15.60
66.58	429.73	11.83
107.74	92.16	50.58
45.56	302.76	246.49
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1,257.44	1699.53	779.11

8

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$N = 24$

$K = 8$

$$C_x = \frac{\sum (x)^2}{N} = \frac{(92.68 + 110.77 + 71.3)^2}{24} \quad (5)$$

$$= \frac{75,487.56}{24} = 3,145.31$$

$$SSr = \sum x^2 - C_x = (1257.44 + 1699.53 + 779.11) - 3,145.31$$

$$= 3736.08 - 3,145.31$$

$$SSr = 590.77$$

$$SSA = \frac{(\sum x^2)}{n} - C_x$$

$$= \frac{(92.68)^2}{8} + \frac{(110.77)^2}{8} + \frac{(71.3)^2}{8} - 3,145.31$$

$$= (1073.69 + 1533.74 + 635.46)$$

$$= 97.58$$

$$SSW = SST - SSP$$

⑥

$$= 590.77 - 97.58$$

$$= 493.19$$

$$M_{SSP} = \frac{SSP}{k-1} = \frac{97.58}{3-1} = \frac{97.58}{2} = 48.79$$

$$M_{SSW} = \frac{SSW}{N-k} = \frac{493.19}{24-3} = \frac{493.19}{21} = 23.48$$

$$F_{ratio} = \frac{M_{SSP}}{M_{SSW}} = \frac{48.79}{23.48} = 0.02$$

⑧ T-Test

$$\mu = 105$$

$$\bar{x} = 125$$

$$\alpha = 5$$

$$\sigma = 14$$

$$n = 25$$

$$H_0 = \mu = 105$$

$$H_a = \mu > 105$$

$$\frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}}$$

$$t = \frac{125 - 105}{\frac{14}{\sqrt{25}}}$$

$$= \frac{20}{\frac{14}{5}} = \frac{20}{2.8} = \underline{7.14}$$

Degree of freedom = 24

one tailed t table = 1.71 \rightarrow 7.14 does not fall under 1.71.

H_a is accepted.

6) Z-test

⑦

Given \Rightarrow mean $\mu = 15$ miles.

\bar{x} - Sample mean

μ - population mean

$$SD = 14$$

$$n \text{ Sample} = 169$$

$$\bar{x} = 16 \text{ miles.}$$

$$H_0 \rightarrow \mu = 15$$

$$\alpha = 0.10$$

$$H_a \rightarrow \mu > 15$$

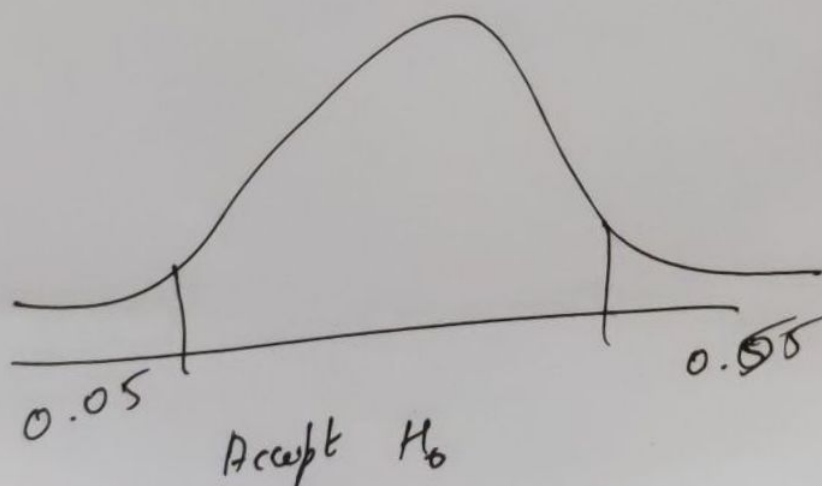
$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}} = \frac{16 - 15}{14 / \sqrt{169}}$$

$$Z = \frac{1}{1.07} = 0.93$$

$$\alpha = 0.10$$

$$p(Z = -1.39) = 0.823$$

$$p = 0.823 > 0.10$$



③ F - Distribution.

M1

M2

20.2	408.04
20.9	436.81
22.3	497.29
22.8	519.84
21.5	462.25
23.0	529
22.4	501.76
21.4	457.96
21.2	449.44
21.3	453.69

22.1	488.41
21.3	453.69
20.1	404.01
22.5	506.25
20.2	408.04
20.3	412.09
20.4	416.16
21.1	445.21
20.8	432.64
20.4	416.16

217 4716.08
 Σx $\Sigma(x)^2$

209.2 4382.66

$$S_{SSR} = \Sigma x^2 - C_x = \frac{9698.74}{20} - 9082.32$$

$$S_{SSR} = 16.42$$

$$C_x = \frac{\Sigma(x)^2}{N} = \frac{(217 + 209.2)^2}{20} = 9082.32$$

$$S_{ST} = \frac{(\sum x^2)}{n} - G$$

$$= \frac{(217)^2}{10} + \frac{(209.2)^2}{10} - 9082.3$$

$$= ~~43.4~~ *$$

$$(4708.9 + 4376.46) - 9082.32$$

$$S_{ST} = 3.04$$

$$S_{SW} = S_{ST} - S_{SA}$$

$$= ~~9082.32~~^{16.42} - 3.04$$

$$= 13.38$$

$$M_{SSA} = \frac{S_{SA}}{k-1} = 3.04$$

$$M_{SSW} = \frac{13.38}{8} = 1.67$$

$$F\text{-ratio} = 1.82$$

F table

$$\left. \begin{array}{l} \text{Mean of machine 1} = 21.7 \\ \text{machine 2} = 20.92 \end{array} \right\} > 20$$

$$\text{Mean of population} = 20$$



$$H_0 = 20$$

$$H_a > 20$$

Groups Vs Sample

$$2-1=1 \quad 20-2=18$$

$$\alpha = 0.05$$

$$Df \Rightarrow \begin{pmatrix} 18 & 1 \end{pmatrix} \\ d_1 \quad d_2$$

$$F_{table} \text{ value} = 4.41 \quad \begin{matrix} \text{Critical} \\ \text{value} \end{matrix}$$

$$F_{ratio} = 1.82$$

we accept H_0 as F_{ratio}
is less than
4.41