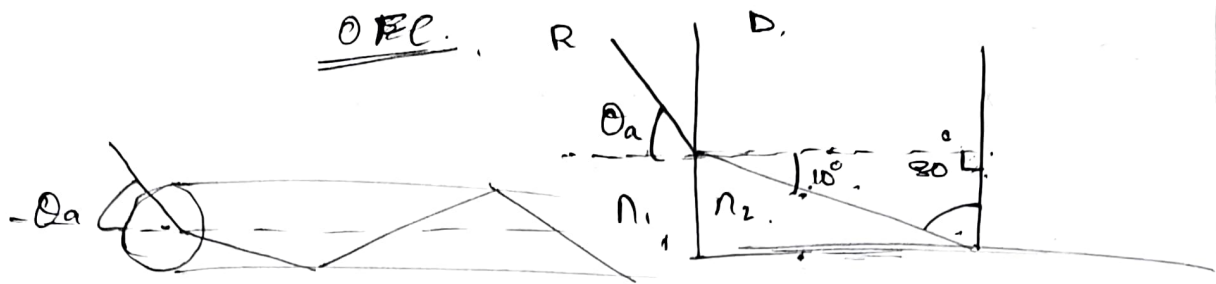


15/03/2021



$$\theta_a = \sin^{-1} \sqrt{n_1^2 - n_2^2}$$

$$n_1 \sin \theta_a = n_2 \sin 10^\circ$$

$$\theta_a = \sin^{-1} (n_2 \sin 10^\circ)$$

Q1

Consider a multimode fiber with core RI of 1.48

& a cladding with RI of 1.46.

- Cal:
- (1) Critical angle,
 - (2) NA.
 - (3) Acceptance angle.

Solution:

Critical angle $\theta_c =$

$$\theta_c = \sin^{-1} \left(\frac{1.46}{1.48} \right)$$

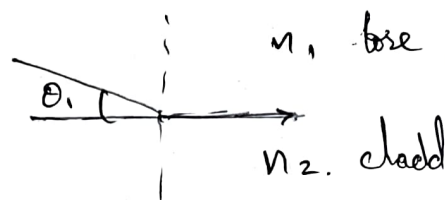
$$\theta_c = \underline{\underline{67.668^\circ \approx 80^\circ}}$$

$$\theta_a = \sin^{-1} \sqrt{n_1^2 - n_2^2}$$

$$\sin^{-1} \sqrt{1.48^2 - 1.46^2}$$

$$\theta_a = \underline{\underline{14.89^\circ}}$$

$$\rightarrow V = \frac{2\pi a \cdot N \cdot n}{\lambda}$$



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\theta_2 = 90^\circ$$

$$\sin \theta_1 = \frac{n_2}{n_1}$$

$$\theta_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$$

$$NA = \sqrt{n_1^2 - n_2^2}$$

Q2 A step index fiber with normalised freq.

$$V = 26.6 \quad @ \quad 1300 \text{ nm } \lambda$$

Radius of core: 25 μm .

$$\text{Cal: } Na = ?$$

$$\text{Core RI} = n_1$$

$$\text{Cladding RI} = n_2 = \underline{\underline{1.47}}$$

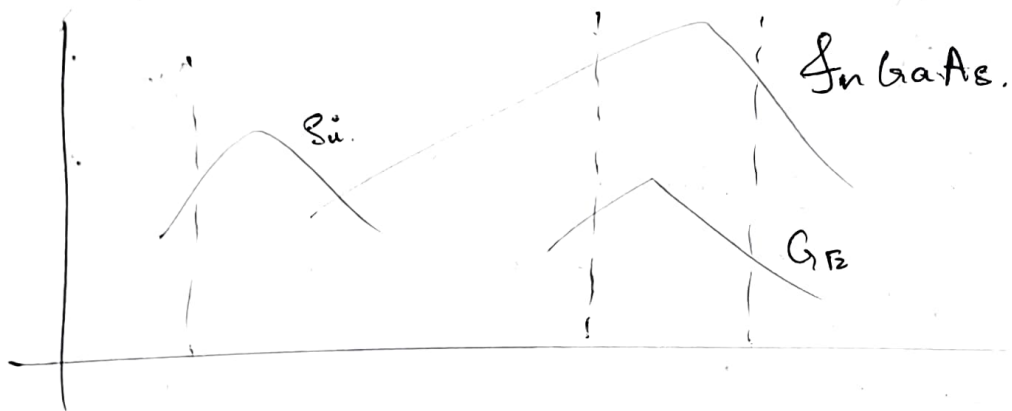
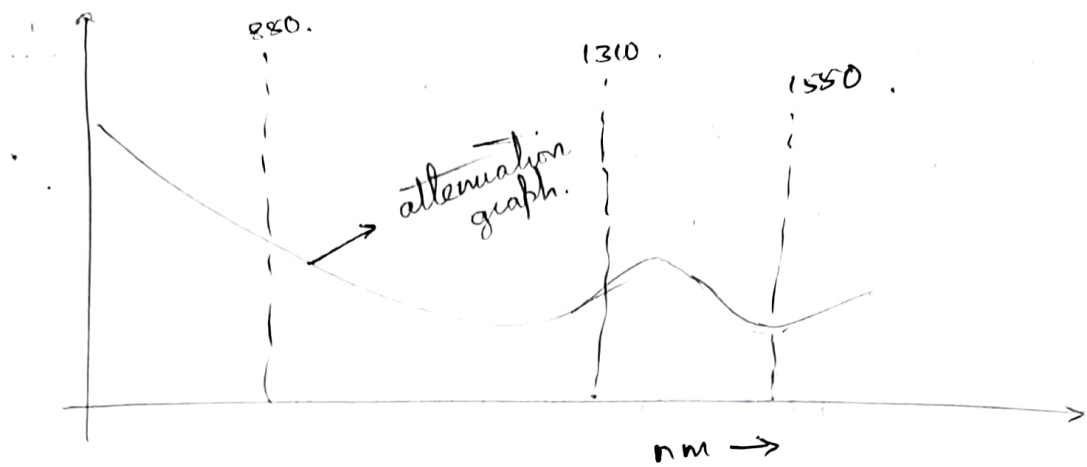
$$V = \frac{2\pi a Na}{\lambda}$$

$$Na = \frac{V \lambda}{2\pi a} = \underline{\underline{0.2201}}$$

$$Na = \sqrt{n_1^2 - n_2^2}$$

$$n_1 = \underline{\underline{1.486}}$$

16/03/2021



Q1) A typical relation RI difference for an OFC designed for long distance Tx is 1%. Estimate the (1) NA. (2) θ_a in air also calculate the θ_c at core cladding interface. For the fiber where $n_1 = 1.46$.

$$n_1 = 1.46$$

$$n_2 = ?$$

$$NA = ?$$

$$\theta_a =$$

$$\theta_c =$$

$$\Delta n = 1\% = \frac{1}{100}$$

$$NA = n_1 \sqrt{2 \Delta n}$$

$$NA = 1.46 \sqrt{2 \times 0.01} = \underline{\underline{0.206}}$$

$$NA = \sqrt{n_1^2 - n_2^2}$$

$$\frac{n_1 - n_2}{n_1} = \frac{1}{100}$$

$$n_2 = \underline{\underline{1.4454}}$$

$$\theta_c = \underline{\underline{81.89^\circ}}$$

Core & cladding loss.

P → Power.

$$L_{vm} = \frac{\alpha_1 P_{core}}{P} + \frac{\alpha_2 P_{clad}}{P}$$

$$L_{vm} = \alpha_1 + (\alpha_2 - \alpha_1) \frac{P_{clad}}{P}$$

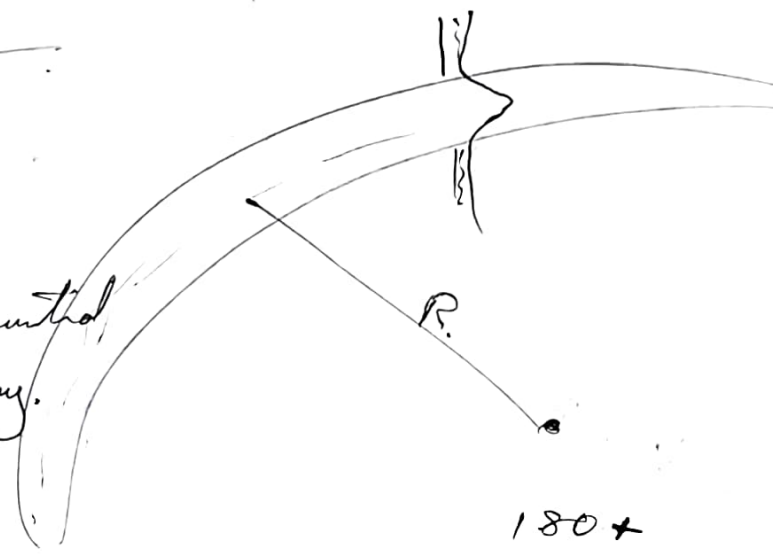
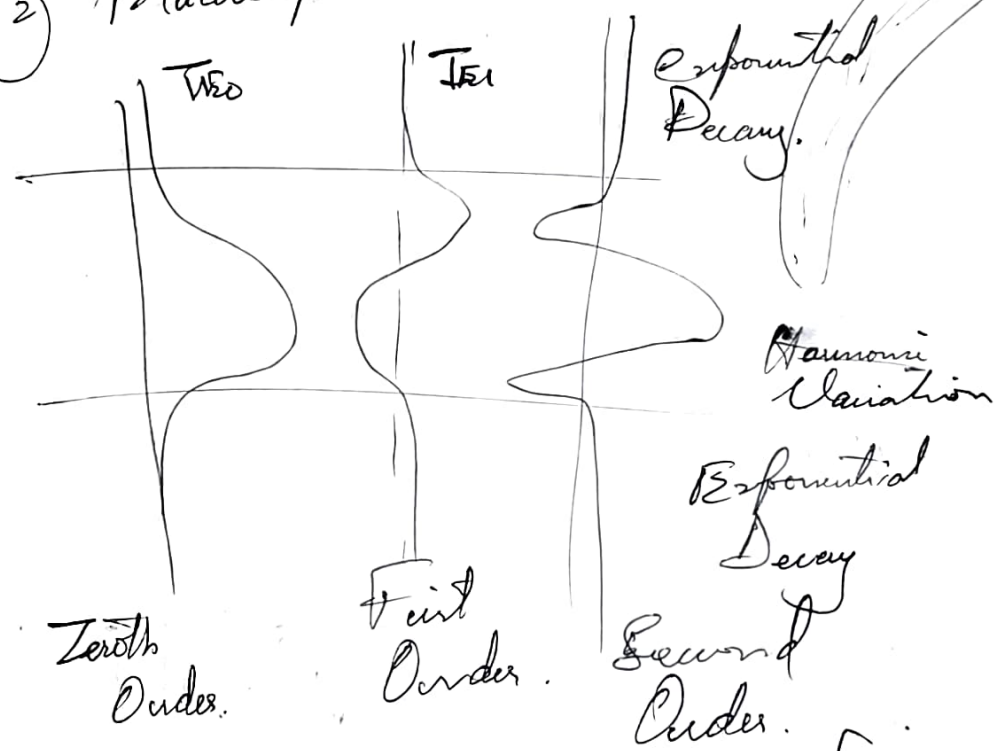
$$L(\omega) = \alpha_1 + (\alpha_2 - \alpha_1) \frac{k^2 n^2(o) - n^2(\omega)}{n^2(o) - n_2^2}$$

as/2021.

Bending Loss.

① Macroscopic Bending Loss.

② Microscopic — α —



$$N_{eff} = N_A \left\{ 1 - \frac{\alpha + 2}{2\alpha\Delta} \left[\frac{2a}{R} + \left(\frac{3}{2n_2 K R} \right)^{2/3} \right] \right\}$$

$$N_{eff} = \frac{\alpha}{\alpha + 2} (n_1 K a)^2 \Delta$$

$$F(\alpha_m) = \left[1 + \pi \Delta^2 \left(\frac{b}{a} \right)^4 \frac{E_g}{E_y} \right]^2$$

$E_g \rightarrow$ Young's Modg
fiber.

$E_y \rightarrow$ — " —
Factor.

① Mean optical power launched into a 8 km length of OFC is 12 mW & of power is 3 mW.
Find overall signal attenuation dB & in Nepers

For a 10 km link of same fibres, compare attenuation loss if there are splices located at 1 km intervals each having an attenuation loss of 1 dB.

Sol:

$$Z = 8 \text{ km}$$

$$P_{\text{in}} = 12 \text{ mW}$$

$$P_{\text{out}} = 3 \text{ mW}$$

$$\alpha = \frac{1}{Z} \ln \left(\frac{P_{\text{in}}}{P_{\text{out}}} \right)$$

$$= \frac{1}{8000} \ln \left(\frac{12}{3} \right)$$

$$= \frac{1}{8000} \ln(4) = 173 \times 10^{-6} \text{ nepers}$$

$$10 \log_{10}(\alpha) = 173 \times 10^{-6}$$

$$\alpha = 1 \text{ Neper}$$

$$\alpha_p = \frac{10}{Z} \log_{10} \left[\frac{P_{\text{in}}}{P_{\text{out}}} \right] \text{ dB/km}$$

$$= \frac{10}{8} \log_{10}(4) = 0.752 \text{ dB/km}$$

For 10 km line

$$10 \times 0.752 + 7$$

$$7.52 + 9$$

$$\underline{\underline{16.52 \text{ dB}}}$$

$$L_{sc} = \frac{154.2 \times \omega^2}{46.6 \times 100} \exp\left(\frac{4.63}{x}\right)$$

x - mole fraction.

$$L_{scattering} = \frac{8\pi^3}{3\lambda^4} (\eta^2 - 1)^2 K_B T_g B_T. \quad \text{Neper.}$$

Q3) A multimode SI Fibres find number of modes for single mode. Cal core dia of the fibre is replaced with single mode Fibres.

$$V = \frac{2\pi a}{\lambda} (Na)$$

No. of modes for single mode is $\frac{V^2}{4}$

$$\frac{V^2}{4} = 1$$

$$V^2 = 4$$

$$V = \underline{\underline{2.414}}$$

$$\frac{V^2}{4} = 1$$

$$V^2 = 1 \times 4 = 2$$

$$2.414 = \frac{2\pi a}{\lambda} (Na)$$

$$d = \underline{\underline{2.113 \times 10^{-6} m}} = \underline{\underline{2.113 \mu m}}$$

$$V = 2.405$$

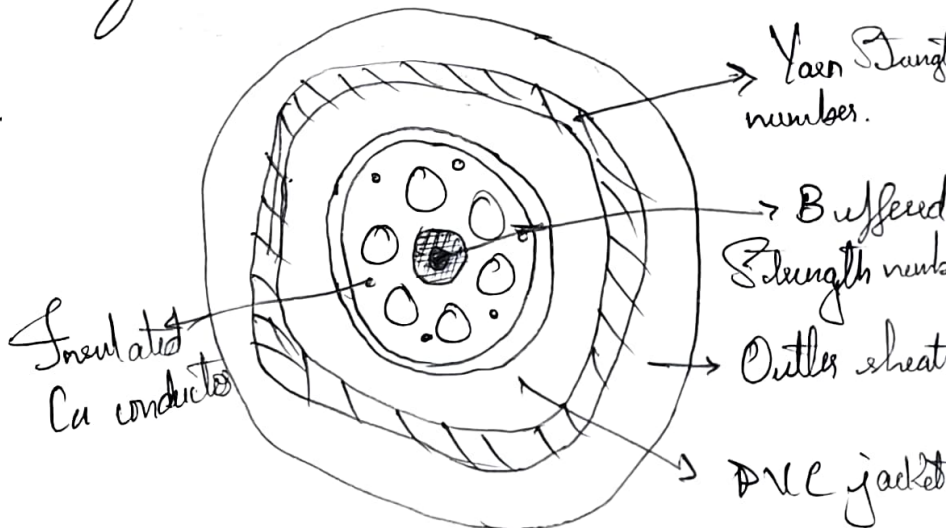
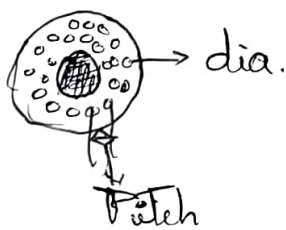
$$V = \frac{2\pi a}{\lambda} (Na)$$

$$a = \underline{\underline{1.27 \mu m}}$$

$$d = \underline{\underline{2.55 \mu m}}$$

$$\left\{ \text{GRIN } V = \frac{\pi a}{\lambda} (Na) \right.$$

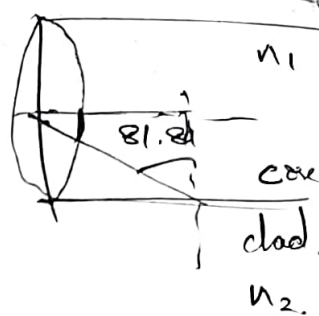
Photonic Fibres. Fiber Holey Fibres.
Core & cladding are made of same material.



$$O_c = \sin^{-1} \left(\frac{n_2}{n_1} \right)$$

$$O_a = \sin^{-1} \sqrt{1.46^2 - 1^2}$$

$$n_a = 1$$



$$n_1 \sin O_a = n_2 \sin O_c$$

$$\sin O_a = \frac{n_2}{n_1} \sin 81.8^\circ$$

$$O_a =$$

$$\sin O_a = 1.46 \sin (90 - 81.8^\circ)$$

$$O_a = 11.886^\circ$$

$$\epsilon = \pi O_a^2 = \pi \sin^2 O_a \rightarrow \text{Solid acceptance angle.}$$

$$\epsilon = 37.3409, 443.83, 0.13327$$

17/03/2021

Q2. A multimode step index fiber with a core dia of 80 μm & refractive index diff of 1.5% is operating at a $\lambda = 0.85 \mu\text{m}$. If $n_1 = 1.48$, estimate the "V" for fiber & no of guided modes.

Sol: Given: $a = 80 \mu\text{m}$

$$\Delta n = 1.5\% = 0.015$$

$$\lambda = 0.85 \mu\text{m}$$

$$n_1 = 1.48$$

$$V = ?$$

$$V = \frac{2\pi a N_a}{\lambda}$$

$$\frac{n_1 - n_2}{n_1} = 0.015$$

$$n_2 = 1.4578$$

$$N_a = \sqrt{n_1^2 - n_2^2} = 0.258$$

$$V = \frac{2\pi a N_a}{\lambda} = \frac{2\pi \times 80 \times 0.258}{0.85} = 151.02$$

$$\frac{V^2}{2} = 2850.88$$