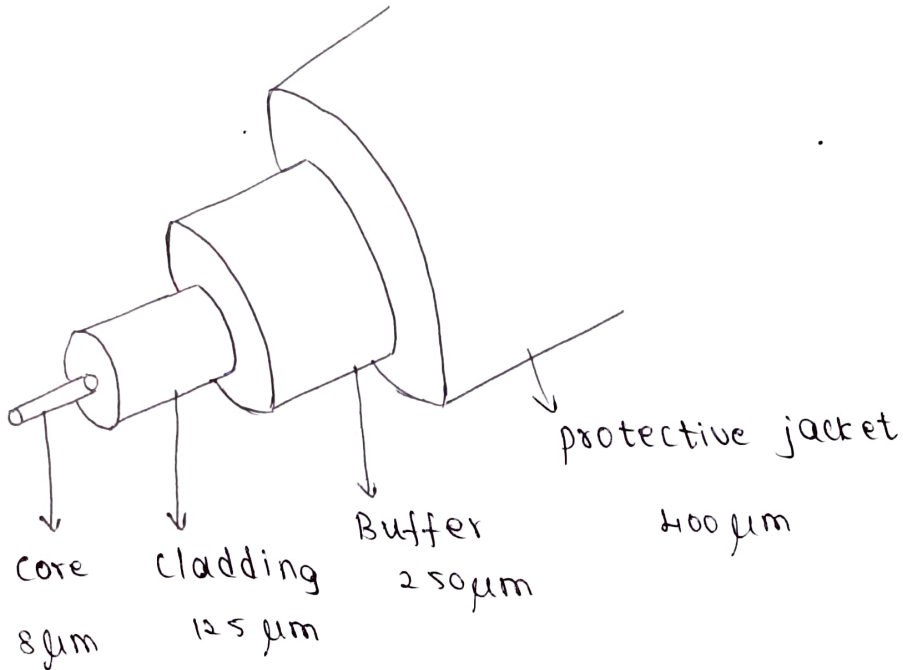


⇒ structure of optical fibres:



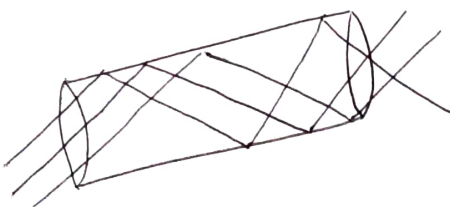
⇒ Modes :

1. Single mode:



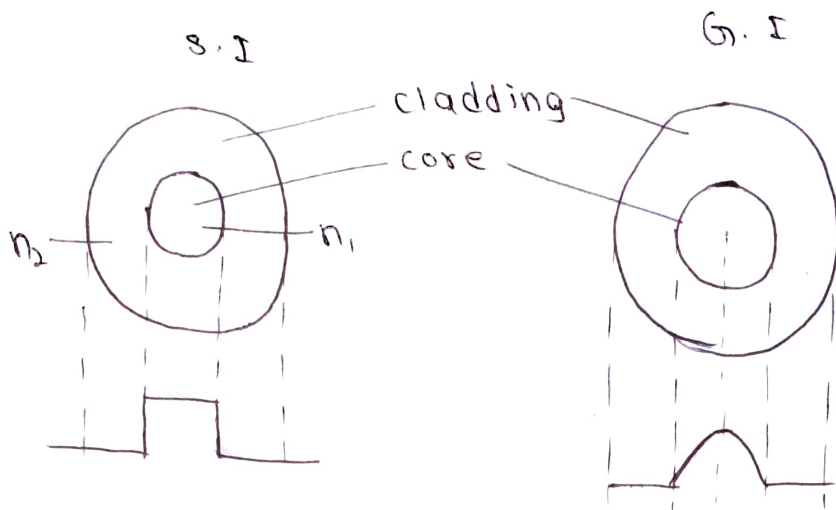
2. Multimode:

different angle of incidence



→ Based on R.I:

1. step Index:
2. Graded index:



*

$$\frac{n_1 - n_2}{n_1}$$

$$\frac{n_1^2 - n_2^2}{2n_1^2}$$

* parameters: Gbps

Tbps

* pulse spreading: more

less

* Attenuation: less
(0.3

more

(many no of light rays)
0.6 - 1

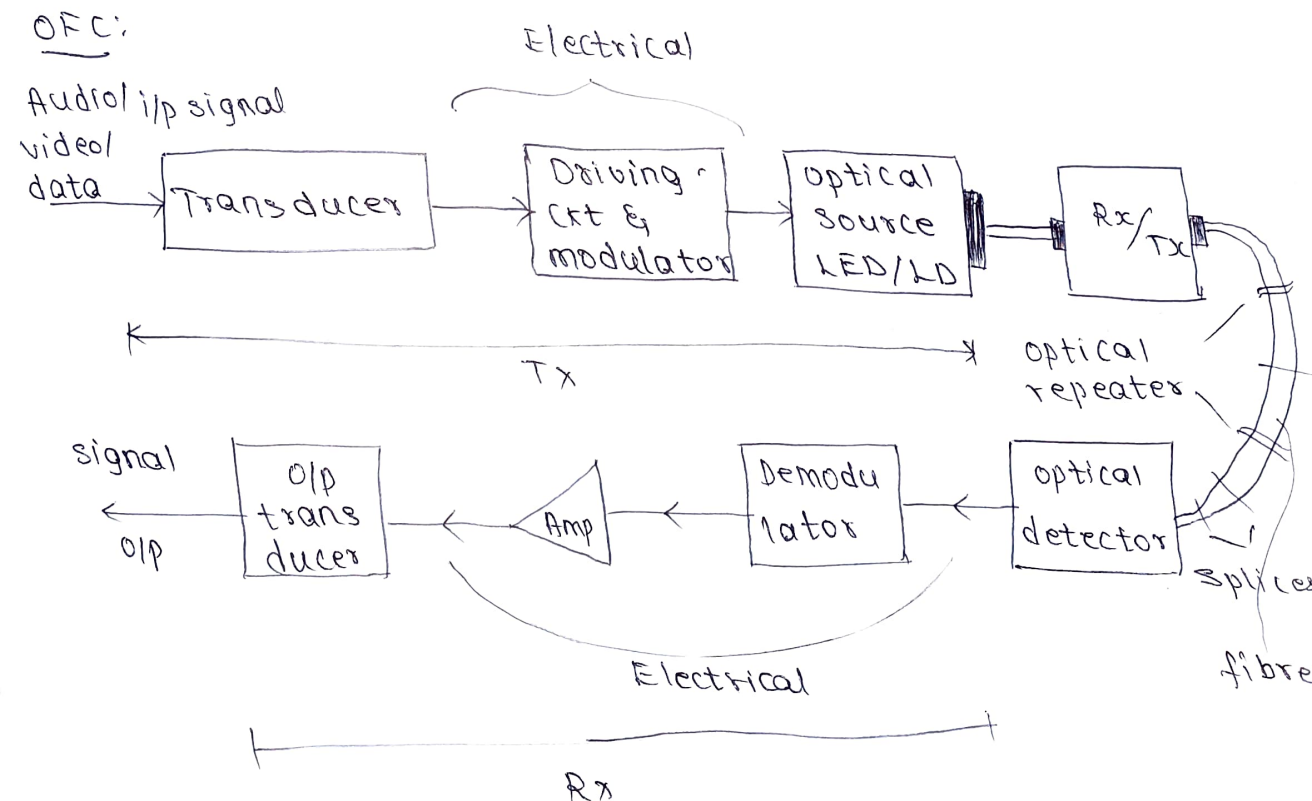
* R.I is max at the centre.

Single mode

Multi model

| | | |
|------------------------|--------------------|--------------------------------|
| * No of mode: | single (one) | many |
| * Core dia: | smaller | longer (50-200 μm) |
| * Optical sources: | lasers | LED |
| * Coupling efficiency: | Intramodel | Intermodel |
| * Coupling efficiency: | 40-50% | 50-60% |
| * N.A : | smaller | larger |
| * splicing : | very difficult | easier |
| * B.W product : | higher | smaller |
| * Application: | Long distance comm | Broadband. |

OFC:



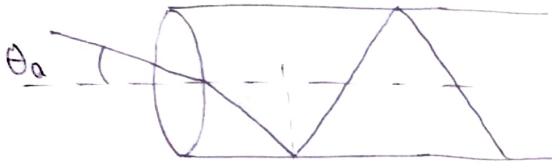
⇒ Fibre materials:

- * Flexible
- * high tensile strength
- * Temperature resistance
- * low cost
- * Transparent

Silica

Plastic fibres $\begin{cases} \text{PMMA} \\ \text{PF} \end{cases}$

15-3-21



θ_a - acceptance angle

$$\theta_a = \sin^{-1} \sqrt{n_1^2 - n_2^2}$$

⇒ Problems:

1. Multimode silica fibre, core R.I, $n_1 = 1.48$, cladding R.I = 1.46. Calculate the critical angle θ_c , numerical aperture NA & Acceptance angle θ_a .

→ $n_2 = 1.46$

$n_1 = 1.48$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\theta_2 = 90^\circ$$

$$\theta_1 = \theta_c$$

$$\sin \theta_c = \frac{n_2}{n_1}$$

$$\theta_c = 80.56^\circ$$

$$\theta_a = \sin^{-1} \sqrt{n_1^2 - n_2^2}$$

$$= \sin^{-1} \sqrt{1.48^2 - 1.46^2}$$

$$= \sin^{-1} (0.242)$$

$$\theta_a = 14.03^\circ$$

$$N.A = 0.242$$

Normalised freq variable, $V = \frac{2\pi a}{\lambda} (NA)$

2. A step Index fibre has a normalised freq $V = 26.6$ at 1300nm wavelength, core radius is $25\mu\text{m}$, calculate NA, core R.I for given cladding R.I $n_2 = 1.47$.

→

$$V = \frac{2\pi a}{\lambda} (NA)$$

$$26.6 = \frac{2\pi \times 25 \times 10^{-6} \times NA}{1300 \times 10^{-9}}$$

$$N.A = \frac{26.6 \times 1300 \times 10^{-9}}{2\pi \times 25 \times 10^{-6}}$$

$$NA = 0.22$$

$$N.A = \sqrt{n_1^2 - n_2^2} = 0.22$$

$$n_1^2 - n_2^2 = 0.04846$$

$$n_1^2 = 0.04846 + 1.47^2$$

$$n_1^2 = 2.209, n_1 = 1.486$$

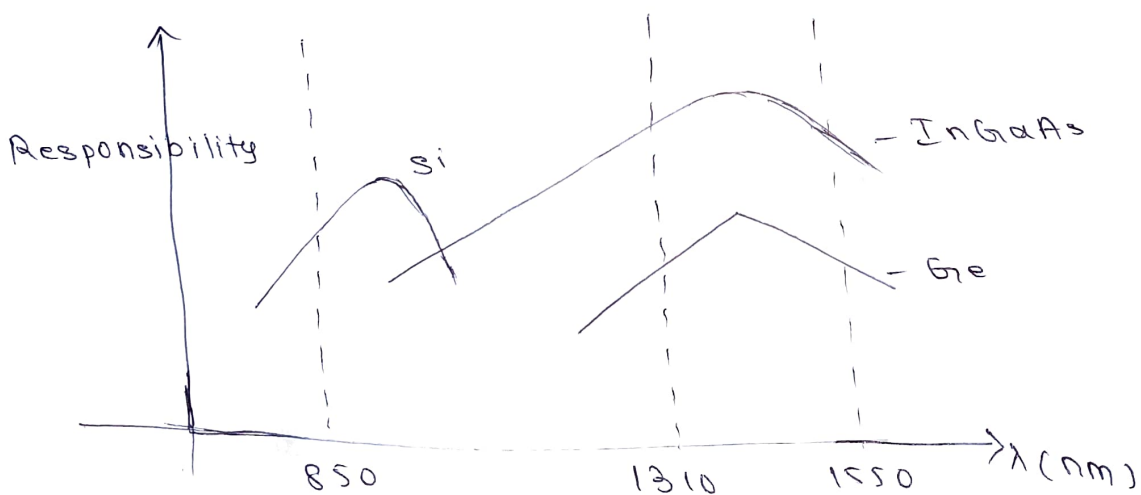
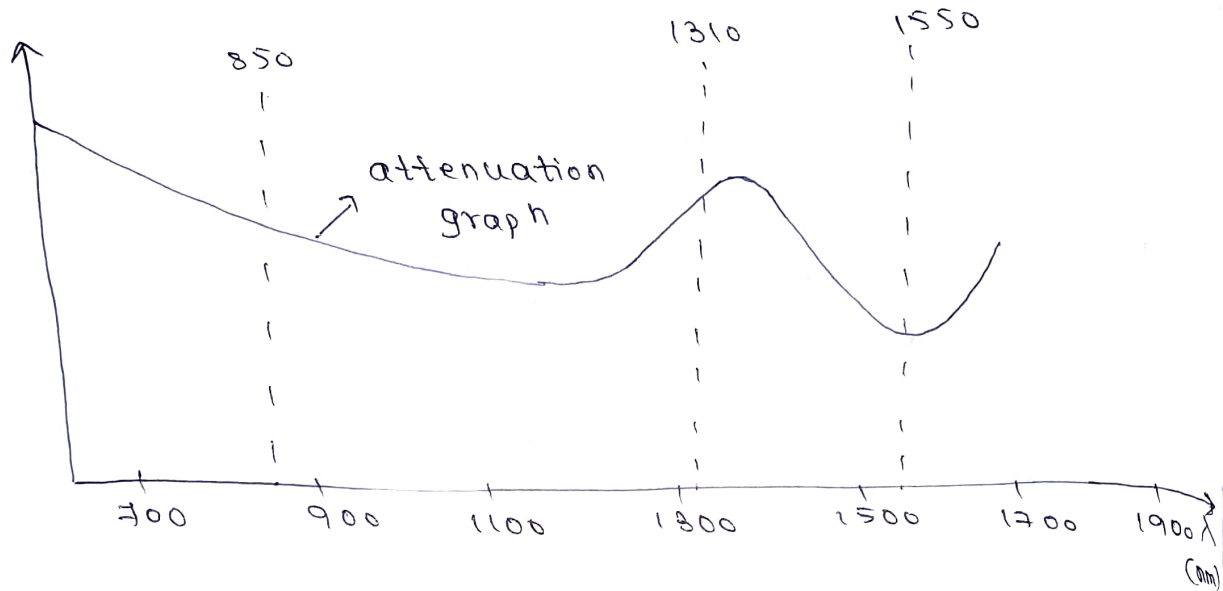
⇒ EM spectrum:

16-3-21

850 nm - short wavelength

1310 nm - O band

1550 nm - Higher wavelength.



→ Relative Index diff

$$\Delta n = n_1 - n_2$$

$$\Delta n_1 = \frac{n_1 - n_2}{n_1}$$

$$\rightarrow NA = n_1 \sqrt{2\Delta}$$

3. A typical relative refractive index diff for an optical fibre designed for long distance transmission, ^{is 1%} estimate the NA and the solid acceptance angle in airy for the fibre when the core index is 1.46. Also calculate the critical angle at the core cladding interface within the fibre.

→ For small angles $E = \pi \theta_a^2 = \pi \sin^2 \theta_n$.
solid acceptance angle

$$\times \Delta = 1\% = 0.01$$

$$\begin{aligned} \times NA &= n_1 \sqrt{2\Delta} \\ &= 1.46 \sqrt{2 \times 0.01} \end{aligned}$$

$$N.A. \approx 0.206.$$

$$\cancel{0.206}^2 = \cancel{1.46}^2 - n_2^2$$

$$\times n_2 = 1.445$$

$$\times \sin \theta_c = \frac{n_2}{n_1}$$

$$\theta_c = 81.77^\circ$$

$$\begin{aligned} \times \theta_a &= \sin^{-1} \sqrt{n_1^2 - n_2^2} \\ &= \sin^{-1} (0.206) \\ &= 11.91^\circ \end{aligned}$$

/ 17-3-21

4. A multimode step index fibre with a core dia $80 \mu\text{m}$ & R.I of 1.5% is operating at a wavelength of $0.85 \mu\text{m}$. If the core R.I is 1.48 Estimate the normalised freq. for the fibre & the no. of guided modes.

$$\rightarrow \lambda = 0.85 \mu\text{m}, \Delta = 1.5\%$$

$$n_1 = 1.48$$

$$\Delta = \frac{n_1 - n_2}{n_1}$$

$$0.015 = \frac{1.48 - n_2}{1.48}$$

$$n_2 = 1.45$$

$$* \quad N.A = n_1 \sqrt{2\Delta} = 1.48 \sqrt{2 \times 0.015}$$

$$= 0.256$$

$$* \quad V = \frac{2\pi a}{\lambda} (NA)$$

$$= \frac{2 \times \pi \times 40 \mu \times 0.256}{0.85 \mu}$$

$$V = 75.69 \quad \text{normalised freq variable}$$

$$* \quad \text{No. of modes}, \quad \frac{V^2}{2} = 2864.48$$

Single mode
 $V = 2.405$

5. ~~A multimode step index fibre~~

~~Find the number of modes~~

5. Calculate the core diameter if the fibre is replaced with single mode fibre.

$$\rightarrow \quad V = \frac{2\pi a}{\lambda} (NA)$$

$$V = 2.405$$

$$2.405 = \frac{2\pi a (0.256)}{0.85 \mu}$$

$$a = 1.27 \mu m$$

$$\text{Core diameter} = 2a = 2.54 \times 10^{-6} m$$

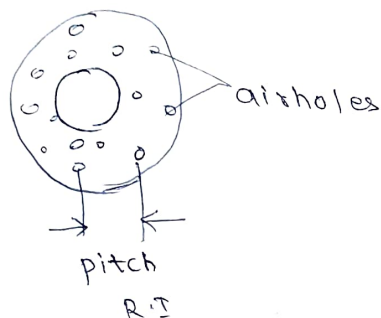
* Number of modes (single mode) $\approx \frac{V^2}{4}$

crystal

⇒ Photonic fibre:

* also called as fiber Holey fibers.

→ R.I depends on the dia of the air holes



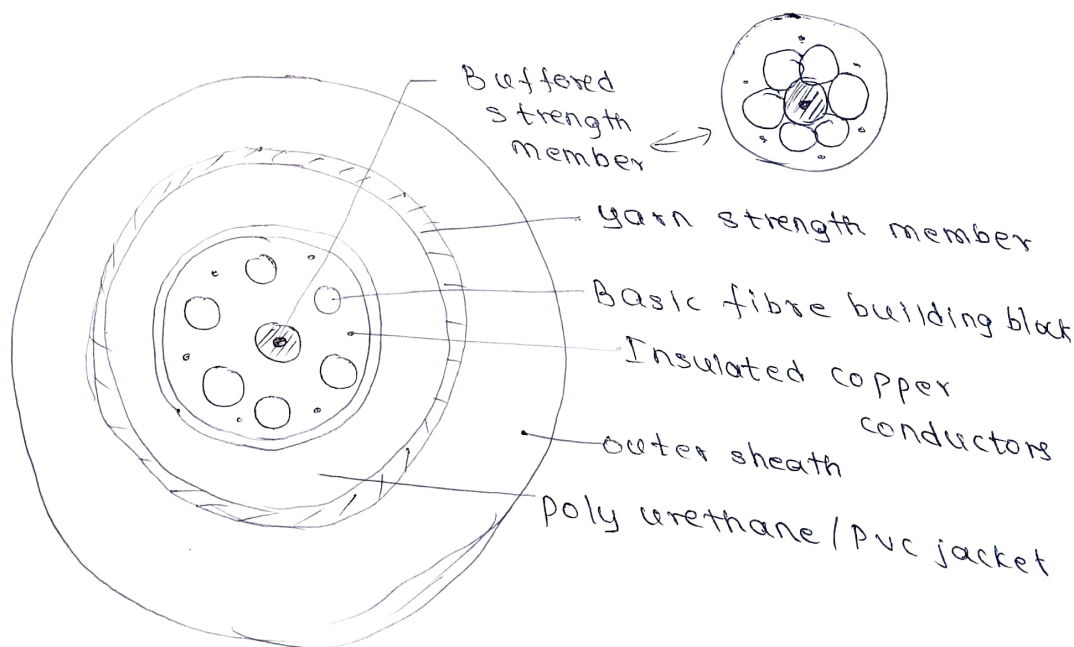
→ small diff b/w core & cladding ($n_{\text{air}} = 1$, $n_{\text{silica}} = 1.45$)

Adv:

→ Highly effective to darkening effect.

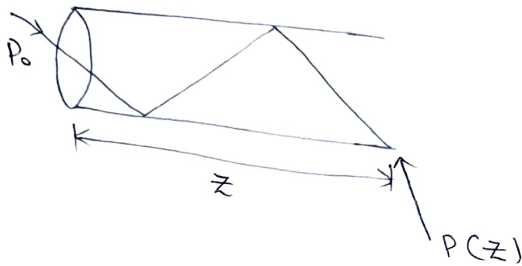
→ It supports single mode

⇒ Fibre optic cables:



SIGNAL DEGRADATION IN FIBRES

→ Attenuation:



$$P(z) = P(0) e^{-\alpha_P \cdot z}$$

$$\alpha_P = \frac{1}{z} \ln \left(\frac{P(0)}{P(z)} \right)$$

→ Absorption Loss:

- * By atomic effects in glass composition.
- * dissipation of optical power
- * Extrinsic absorption & intrinsic absorption.

→ Scattering loss:

22-3-21

$$\alpha_{uv} = \frac{154.2 \times 10^{-2}}{46.6 \times + 66} \exp \left(\frac{4.63}{\lambda} \right)$$

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→ Scattering loss:

$$\alpha_{scat} = \frac{8\pi^3}{3\lambda^4} (\eta^2 - 1)^2 K_B T_f \beta_T \text{ Nepers.}$$

1. Mean optical power launched into a 8km length of optical fibre is $12 \mu\text{W}$ & o/p power is $3 \mu\text{W}$. Find overall signal attenuation in dB & Nepers.

b) For 10km optical lane, using same fibre compare attenuation loss if there are ~~power~~ splices located at 1km intervals each having attn loss of 1dB.

$$\rightarrow a) * \quad P(z) = P(0) e^{-\alpha_p \cdot z}$$

$$\alpha_p = \frac{1}{z} \ln \left(\frac{P(0)}{P(z)} \right)$$

$$= \frac{1}{8 \times 10^3} \ln \left(\frac{12 \times 10^{-6}}{3 \times 10^{-6}} \right)$$

$$= +1.73 \times 10^{-4} \text{ Nepers.}$$

$$* \alpha_p = \frac{10}{z} \log \left(\frac{P(0)}{P(z)} \right)$$

$$= \frac{10}{8} \times \log \left(\frac{12 \times 10^{-6}}{3 \times 10^{-6}} \right)$$

$$= 0.75 \text{ dB/km.}$$

b) loss per km, $\alpha_p = 0.75 \text{ dB/km}$

10 km $\alpha_p = 7.5 \text{ dB/km}$.

For 10km = 9 splices

$$\alpha_{\text{Total}} = \alpha_p + \alpha_p (\text{splicing})$$

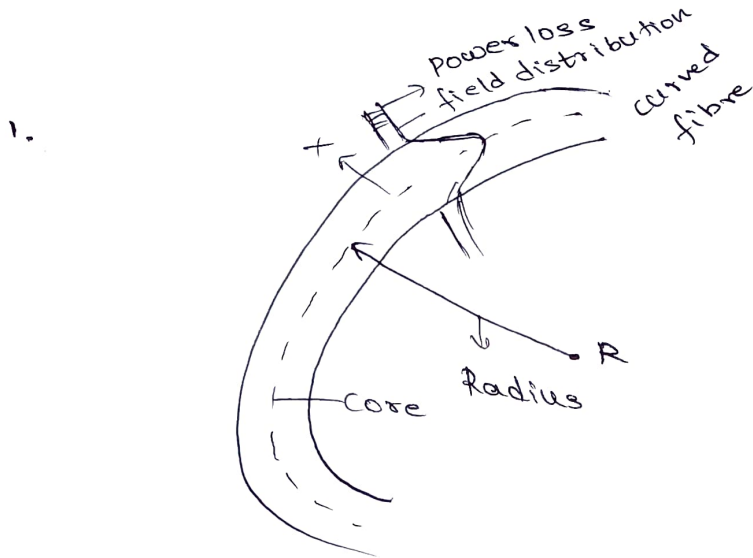
$$= 7.5 + 9 \times 1$$

$$\alpha_{\text{Total}} = 16.5 \text{ dB}$$

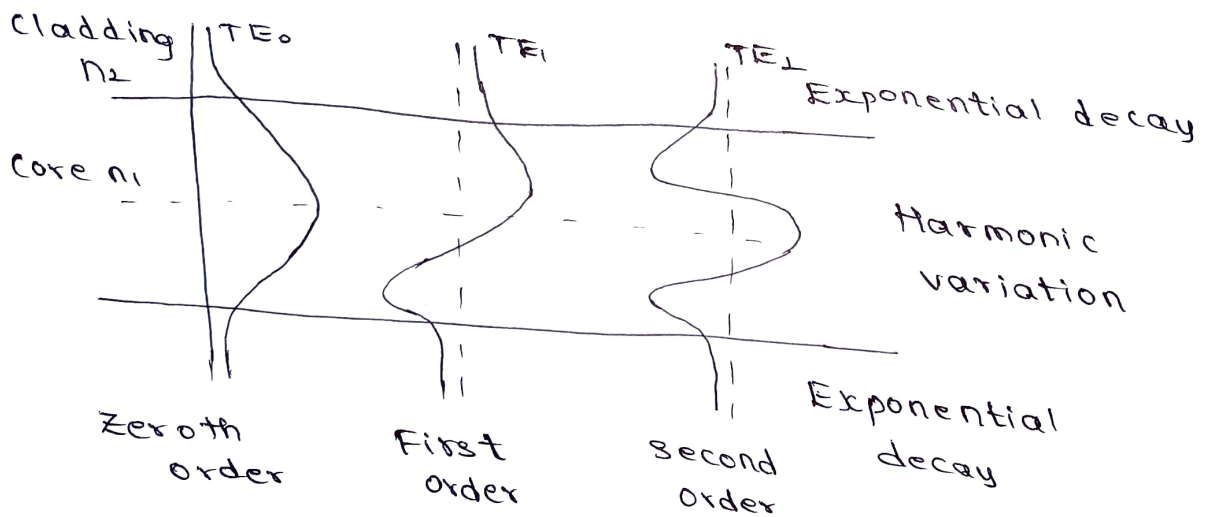
⇒ Bending Loss:

25-3-21

1. Macroscopic B.L
2. Microscopic B.L



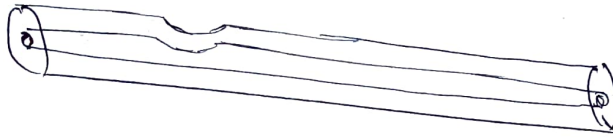
→ Radius decreases, loss increases



$$N_{eff} = N_0 \left\{ 1 - \frac{d+2}{2d\Delta} \left[\frac{2a}{R} + \left(\frac{3}{2n_1 k R} \right)^{2/3} \right] \right\}$$

$$N_0 = \frac{d}{d+2} (n_1 k a)^2 \Delta$$

2. Microscopic B.L



→ also called as packaging loss

$$F(\alpha_m) = \left[1 + \pi \Delta^2 \left(\frac{b}{a} \right)^4 \underbrace{\frac{E_s}{E_j}} \right]^2$$

young's modulus

b - outer radius

⇒ Core and cladding loss:

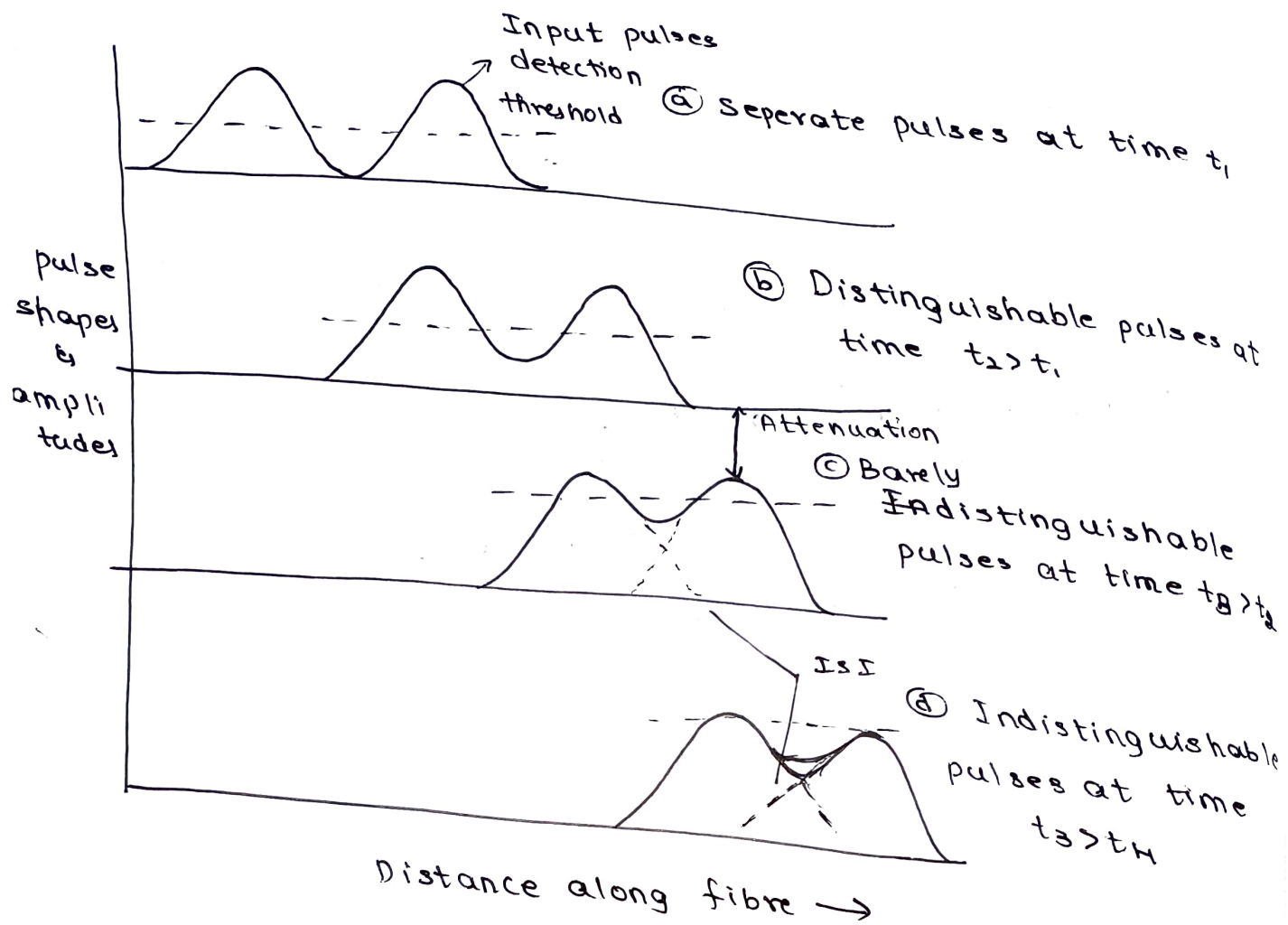
$$\alpha_{\text{um}} = \frac{\alpha_1 P_{\text{core}}}{P} + \frac{\alpha_2 P_{\text{clad}}}{P}$$

$$\alpha_{\text{um}} = \alpha_1 + (\alpha_2 - \alpha_1) \frac{P_{\text{clad}}}{P}$$

$$\alpha(r) = \alpha_1 + (\alpha_2 - \alpha_1) \frac{n^2(0) - n^2(r)}{n^2(0) - n_2^2}$$

⇒ Dispersion :

31-3-21



1. Calculate radius of curvature R at which the no. of modes decreases by 50% in a graded index fibre.
 $d = 2$, $n_2 = 1.5$, $\Delta = 0.01$, $a = 25 \mu\text{m}$ & wavelength of the guided light is $1.3 \mu\text{m}$

$$N_{\infty} = \frac{d}{d+2} (n_1 k a)^2 \Delta$$

$$N_{eff} = N_{\infty} \left\{ 1 - \frac{4}{4 \times 0.01} \right\}$$

$$N_{eff} = N_{\infty} \left\{ 1 - \frac{d+2}{2d\Delta} \left[\frac{2a}{R} + \left(\frac{3}{2n_2 k R} \right)^{2/3} \right] \right\}$$

$$\frac{N_{\infty}}{2} = N_{\infty} \left\{ 1 - \frac{4}{4 \times 0.01} \left[\frac{2 \times 25 \times 10^{-6}}{R} + \left(\frac{3}{2 \times 1.5 \times 4.83 \times 10^6 \times R} \right)^{2/3} \right] \right\}$$

$$\frac{1}{2} = 1 - 100 \left[\frac{50 \times 10^{-6}}{R} + \frac{3.499 \times 10^{-5}}{R^{2/3}} \right]$$

$$\frac{1}{2} = 1 - 100 \left[\frac{50 \times 10^{-6} \times R^{2/3} + 3.499 \times 10^{-5} R}{R^{5/3}} \right]$$

$$R^{5/3} = 2R^{5/3} - 0.01R^{2/3} + 6.998 \times 10^{-3} R$$

$$= 2 - 0.01R^{-1} + 6.998 \times 10^{-3} R^{-2/3}$$

$$R = 1.03 \text{ cm}$$

12-4-21

⇒ Dispersion:

- i) material
 - ii) w.g
 - iii) polarisation-mode
- } Intramodal

→ Group vel $v_g = \frac{d\omega}{d\beta}$

→ Group delay, $\tau_g = \frac{1}{v_g} = \frac{1}{\omega} \frac{d\beta}{d\omega}$

⇒ I/p o/p signals