

Homework10_madhu

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For this document, you'll want to run the following R code chunk:

```
library(ggplot2) # graphics library
library(MASS)    # contains data sets, including Boston
library(ISLR)    # contains code and data from the textbook

## Warning: package 'ISLR' was built under R version 4.0.5

library(knitr)   # contains kable() function

options(scipen = 2) # Suppresses scientific notation

require(ISLR)
data(Carseats)
```

Part I : Exploring predictors

(Before you answer the following, make sure that the missing values, if any, have been removed from the data.)

- (a) Which of the predictors are quantitative (discrete random variables), and which are qualitative (continuous random variables)?

```
head(Carseats)
```

```
##   Sales CompPrice Income Advertising Population Price ShelfLoc Age
## 1  9.50      138     73           11         276   120      Bad  42
## 2 11.22      111     48           16         260    83      Good  65
## 3 10.06      113     35           10         269    80    Medium  59
## 4  7.40      117    100            4         466    97    Medium  55
## 5  4.15      141     64            3         340   128      Bad  38
## 6 10.81      124    113           13         501    72      Bad  78
##   Urban  US
```

```
## 1   Yes Yes
## 2   Yes Yes
## 3   Yes Yes
## 4   Yes Yes
## 5   Yes  No
## 6    No Yes

str(Carseats)

## 'data.frame':   400 obs. of  11 variables:
## $ Sales      : num  9.5 11.22 10.06 7.4 4.15 ...
## $ CompPrice  : num  138 111 113 117 141 124 115 136 132 132 ...
## $ Income     : num   73 48 35 100 64 113 105 81 110 113 ...
## $ Advertising: num   11 16 10 4 3 13 0 15 0 0 ...
## $ Population : num  276 260 269 466 340 501 45 425 108 131 ...
## $ Price      : num  120 83 80 97 128 72 108 120 124 124 ...
## $ ShelfLoc   : Factor w/ 3 levels "Bad","Good","Medium": 1 2 3 3 1 1 3 2
##              3 3 ...
## $ Age        : num  42 65 59 55 38 78 71 67 76 76 ...
## $ Education  : num   17 10 12 14 13 16 15 10 10 17 ...
## $ Urban      : Factor w/ 2 levels "No","Yes": 2 2 2 2 2 1 2 2 1 1 ...
## $ US         : Factor w/ 2 levels "No","Yes": 2 2 2 2 1 2 1 2 1 2 ...

#Carseats = na.omit(Carseats)
```

[Quantitative predictors: Sales, Population, Age, CompPrice, Income, Advertising, Price, Education. Qualitative predictors: ShelfLoc, Urban, US]

(b) What is the range of each quantitative predictor? You can answer this using the `range()` function.

```
apply(Carseats[,1:11], 2, range)

##      Sales  CompPrice Income Advertising Population Price ShelfLoc Age
## [1,] " 0.00" " 77"      " 21" " 0"          " 10"      " 24" "Bad"   "25"
## [2,] "16.27" "175"      "120" "29"          "509"      "191" "Medium" "80"
##      Education Urban US
## [1,] "10"      "No"  "No"
## [2,] "18"      "Yes" "Yes"
```

[Above table shows the min and max value of each quantitative predictor.]

(c) What is the mean and standard deviation of each quantitative predictor?

```
options(width = 95)
apply(Carseats[, -c(7,10,11)], 2, mean)

##      Sales  CompPrice      Income Advertising  Population      Price
## 7.496325 124.975000  68.657500   6.635000  264.840000 115.795000
## 53.322500
## Education
## 13.900000
```

```
apply(Carseats[, -c(7,10,11)], 2, sd)
```

```
##      Sales    CompPrice      Income Advertising  Population      Price
Age
##    2.824115    15.334512    27.986037     6.650364    147.376436    23.676664
16.200297
##   Education
##    2.620528
```

[Above both table shows the mean and standard deviation of each quantitative predictor.]

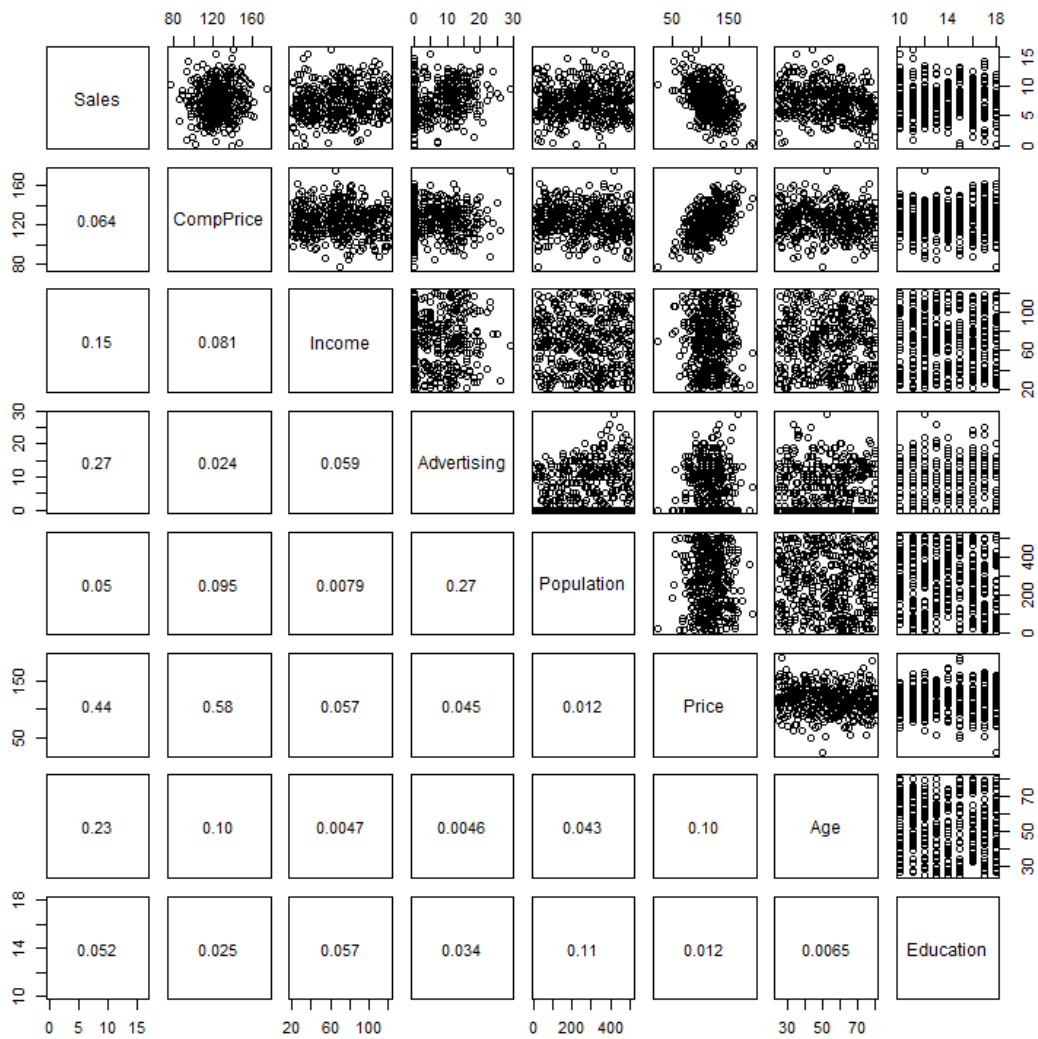
- (d) Using the full data set, investigate the predictors *graphically*, using scatterplots or other tools of your choice. Create some plots highlighting the relationships among the predictors. Comment on your findings.

```
#pairs(Carseats[,1:11])
```

```
panel.cor <- function(x, y, digits = 2, prefix = "", cex.cor, ...)
{
  usr <- par("usr"); on.exit(par(usr))
  par(usr = c(0, 1, 0, 1))
  r <- abs(cor(x, y))
  txt <- format(c(r, 0.123456789), digits = digits)[1]
  txt <- paste0(prefix, txt)
  if(missing(cex.cor)) cex.cor <- 0.4/strwidth(txt)
  text(0.5, 0.5, txt, cex = pmax(1, cex.cor * r))
}
```

```
#pairs(Carseats[,c("Sales", "CompPrice", "Income", "Advertising", "Population",
"Price", "ShelveLoc", "Age", "Education", "Urban", "US")], lower.panel =
panel.cor)
numericdata <- Carseats[, -c(7,10,11)]
#pairs(m)

pairs(numericdata, lower.panel = panel.cor)
```



```
options(width = 80)
round(cor(Carseats[, -c(7,10,11)]), 2)

##           Sales CompPrice Income Advertising Population Price   Age
## Education
## Sales      1.00      0.06   0.15      0.27      0.05 -0.44 -0.23
##            -0.05
## CompPrice  0.06      1.00  -0.08     -0.02     -0.09  0.58 -0.10
##            0.03
## Income     0.15     -0.08   1.00      0.06     -0.01 -0.06  0.00
##            -0.06
## Advertising 0.27     -0.02   0.06      1.00      0.27  0.04  0.00
##            -0.03
## Population 0.05     -0.09  -0.01      0.27      1.00 -0.01 -0.04
##            -0.11
## Price      -0.44      0.58  -0.06      0.04     -0.01  1.00 -0.10
##            0.01
```

```
## Age      -0.23    -0.10    0.00      0.00    -0.04 -0.10    1.00
0.01
## Education -0.05     0.03   -0.06     -0.03    -0.11  0.01    0.01
1.00

#c=subset(Carseats, select=-ShelveLoc)
#b=subset(c, select=-US)
#a=subset(b, select=-Urban)
#cor(a)
```

[Above scatter plots shows the relationship among the predictors. As we can see price and sales has the most correlation between all the variables.]

- (e) Suppose that we wish to predict sales of car seats (in each location) (that is, the random variable Sales) on the basis of the other variables. Do your plots suggest that any of the other variables might be useful in predicting Sales? Justify your answer

[The other variables might be useful in predicting Sales is price variable. We can predict that if there is a increase in the price sales decreases.]

Part II: Splitting the sample into training and sample

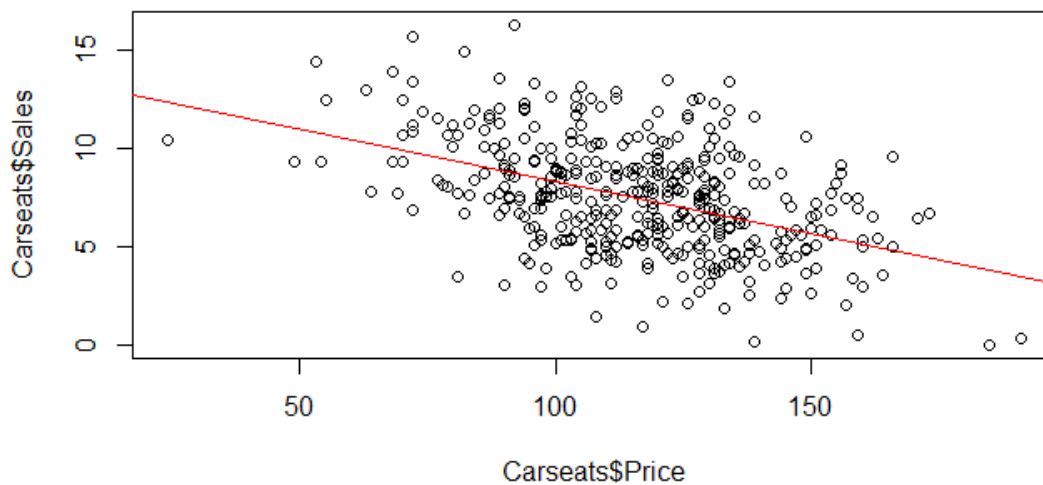
For this problem, continue using the Carseats data set.

- a) Construct a scatterplot of Sales vs Price.

```
attach(Carseats)

fit.slm <- lm(Sales~Price , data=Carseats)
#qplot(data = Carseats, x = Sales, y = Price)

plot(Carseats$Price,Carseats$Sales)
abline(fit.slm, col="red")
```



[As we can see from the scatter plot if we increases the price of carseats the sale of carseats decreases.]

- b) Use the `sample()` command to construct `train`, a vector of observation indexes to be used for the purpose of training your model. This will partition the data set into the *training* set and the *testing* set.
- Describe what the `sample()` function as used above actually does.

#Splitting data into training and testing sets using 75% of sample size.

```
sampleSize <- floor(0.75 * nrow(numericdata))
set.seed(123)
trainingSet <- sample(seq_len(nrow(numericdata)), size = sampleSize)
trainingSet1 <- numericdata[trainingSet, ]
testingSet1 <- numericdata[-trainingSet, ]
head(trainingSet1)
```

##	Sales	CompPrice	Income	Advertising	Population	Price	Age	Education
## 179	10.66	104	71	14	89	81	25	14
## 14	10.96	115	28	11	29	86	53	18
## 195	7.23	112	98	18	481	128	45	11
## 306	8.03	115	29	26	394	132	33	13
## 118	8.80	145	53	0	507	119	41	12
## 299	10.98	148	63	0	312	130	63	15

```
head(testingSet1)
```

##	Sales	CompPrice	Income	Advertising	Population	Price	Age	Education
## 1	9.50	138	73	11	276	120	42	17
## 3	10.06	113	35	10	269	80	59	12
## 6	10.81	124	113	13	501	72	78	16

## 8	11.85	136	81	15	425	120	67	10
## 15	11.17	107	117	11	148	118	52	18
## 17	7.58	118	32	0	284	110	63	13

[When used in `sample(n, size)` syntax, the `sample` function produces a random sample of size `size` from `1:n`. Sampling is done without replacement]

- c) Validate the partition you obtained for the data. Do you see any issues?
- *Hint:* this problem is *not* asking you to balance the training data set. It is instead asking you to determine *whether* balancing might be required. To determine that, you should use a hypothesis test! Which test? In R, there is *one function* you need to call to get the output for the comparison of two samples. Explain the answer; justify your conclusion.

```
t.test(trainingSet1,testingSet1)

##
## Welch Two Sample t-test
##
## data: trainingSet1 and testingSet1
## t = 0.32889, df = 1402.1, p-value = 0.7423
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -6.447885 9.045493
## sample estimates:
## mean of x mean of y
## 82.27737 80.97856
```

[As we can see the mean of training set is 82.27737 and the mean of testing set is 80.97856. There is no more difference in the mean of both the sets. I think there will be no need to balance the dataset.]

Part III: fitting and evaluting a multiple linear regression model

This question should be answered using the `Carseats` data set. Use your **training** data set for fitting the model.

- (a) Fit a multiple regression model to predict Sales using Price, Urban, and US.

```
lm.fit = lm(Sales ~ Price+Urban+US, data= Carseats)

summary(lm.fit)

##
## Call:
## lm(formula = Sales ~ Price + Urban + US, data = Carseats)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.9206 -1.6220 -0.0564  1.5786  7.0581
##
```

```
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13.043469   0.651012  20.036 < 2e-16 ***
## Price       -0.054459   0.005242 -10.389 < 2e-16 ***
## UrbanYes    -0.021916   0.271650  -0.081  0.936
## USYes       1.200573    0.259042   4.635 0.00000486 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.472 on 396 degrees of freedom
## Multiple R-squared:  0.2393, Adjusted R-squared:  0.2335
## F-statistic: 41.52 on 3 and 396 DF, p-value: < 2.2e-16

kable(summary(lm.fit)$coef, digits = c(3, 3, 3, 4), format = "markdown")
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	13.043	0.651	20.036	0.0000
Price	-0.054	0.005	-10.389	0.0000
UrbanYes	-0.022	0.272	-0.081	0.9357
USYes	1.201	0.259	4.635	0.0000

```
my.output <- summary(lm.fit)
```

- (b) Provide an interpretation of each coefficient in the model. Be careful—some of the variables in the model are qualitative!

[The coefficient of Price is -0.054, which is close to 0 numerically and is not statistically significant. Holding all else in the model constant, Price does not appear to have much association with Sales. In other words, when price increases by \$1000, the number of cars sold decrease by 54,459.] [Also urban cars does not appear to have much association with sales because the coefficient of urban is -0.022. A store's sale is not affected by whether or not it is in a Urban area.] [The coefficient of US is 1.201. This indicates that, all else in the model held constant, cars manufactured in the USA carry a sales tag that is on average \$1.201 thousand dollars higher than cars manufactured outside the USA. The coefficient is statistically significant at the 0.05 level. A store in the US sales 1200 more cars (in average) than a store that is abroad.]

- (c) Write out the model in equation form, being careful to handle the qualitative variables properly.

[The model may be written as

$$\text{Sales} = 13.0434689 + (-0.0544588) \times \text{Price} + (-0.0219162) \times \text{Urban} + (1.2005727) \times \text{US} + \varepsilon$$

with Urban=1 if the store is in an urban location and 0 if not, and US=1 if the store is in the US and 0 if not.]

- (d) For which of the predictors can you reject the null hypothesis $H_0: \beta_j = 0$?

[We can reject the null hypothesis for the “Price” and “US” variables because P value are too much less for these two variables.]

- (e) On the basis of your response to the previous question, fit a smaller model that only uses the predictors for which there is evidence of association with the outcome.

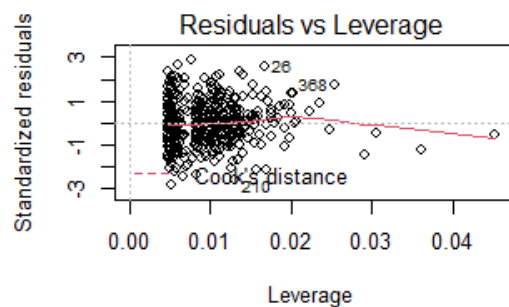
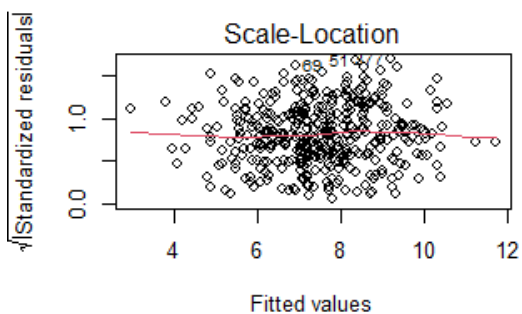
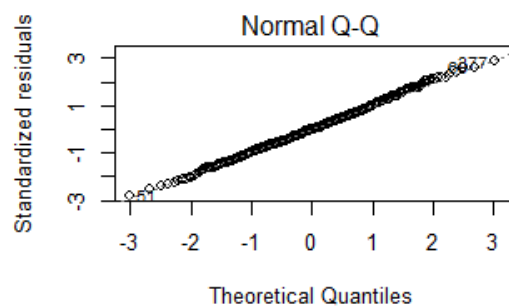
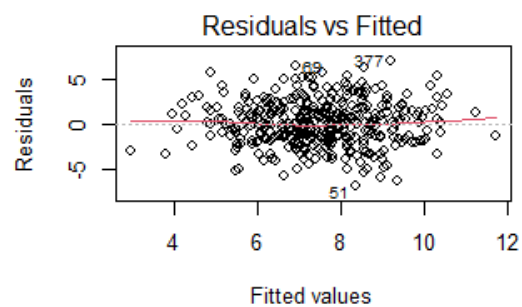
```
lm.fit2 = lm(Sales ~ Price+US, data= Carseats)
summary(lm.fit2)

##
## Call:
## lm(formula = Sales ~ Price + US, data = Carseats)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.9269 -1.6286 -0.0574  1.5766  7.0515
##
## Coefficients:
##              Estimate Std. Error t value    Pr(>|t|)
## (Intercept)  13.03079    0.63098   20.652 < 2e-16 ***
## Price        -0.05448    0.00523  -10.416 < 2e-16 ***
## USYes         1.19964    0.25846   4.641 0.00000471 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.469 on 397 degrees of freedom
## Multiple R-squared:  0.2393, Adjusted R-squared:  0.2354
## F-statistic: 62.43 on 2 and 397 DF,  p-value: < 2.2e-16

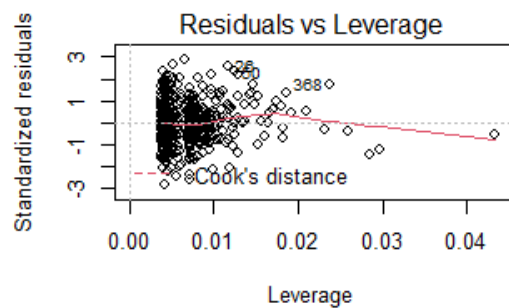
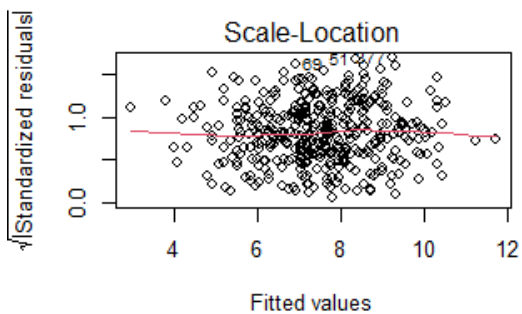
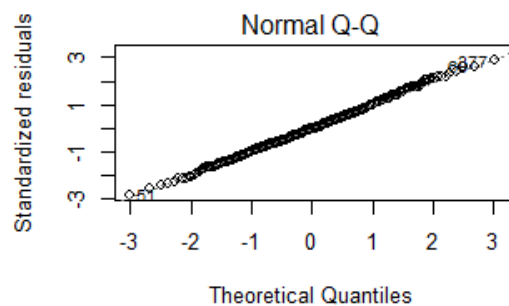
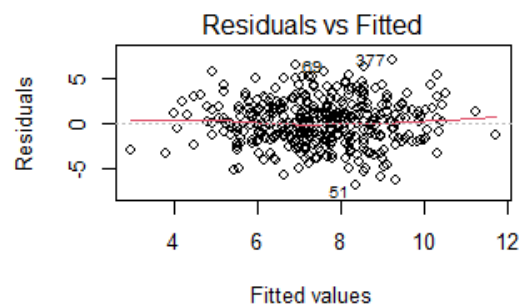
my.output1 <- summary(lm.fit2)
```

- (f) How well do the models in (a) and (e) fit the data?

```
par(mfrow = c(2, 2))
plot(lm.fit)
```



```
par(mfrow = c(2, 2))
plot(lm.fit2)
```



[Based on their respective R-square values(in summary tables), these two models are mediocre (only 24% change in response explained).] [Based on the RSE and R^2 of the linear regressions, they both fit the data similarly, with linear regression from (e) fitting the data slightly better.]

(g) Using the model from (e), obtain 95% confidence intervals for the coefficient(s).

```
confint(lm.fit2)
```

```
##              2.5 %      97.5 %
## (Intercept) 11.79032020 14.27126531
## Price       -0.06475984 -0.04419543
## USYes       0.69151957  1.70776632
```

(h) Compute the *training MSE* and the *testing MSE*.

```
mean(my.output$residuals^2)
```

```
## [1] 6.052087
```

```
mean(my.output1$residuals^2)
```

```
## [1] 6.052186
```

[MSE for training and testing dataset are almost the same.]

Part IV: adding interaction terms

Use the * symbols to fit linear regression models with interaction effects. Do any interactions appear to be statistically significant?

```
data("Carseats", package = "ISLR")
```

```
lm.fit3 <- lm(Sales ~ Price * US, data = Carseats)
```

```
summary(lm.fit3)
```

```
##
```

```
## Call:
```

```
## lm(formula = Sales ~ Price * US, data = Carseats)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max
```

```
## -6.9299 -1.6375 -0.0492  1.5765  7.0430
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept) 12.974798   0.953079  13.614 < 2e-16 ***
```

```
## Price       -0.053986   0.008163  -6.613 1.22e-10 ***
```

```
## USYes       1.295775   1.252146   1.035  0.301
```

```
## Price:USYes -0.000835   0.010641  -0.078  0.937
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Residual standard error: 2.472 on 396 degrees of freedom
## Multiple R-squared:  0.2393, Adjusted R-squared:  0.2335
## F-statistic: 41.52 on 3 and 396 DF,  p-value: < 2.2e-16
```

[The average of the price if the carseat is from the US is decreased with -0.000835 this amount.]

Hints & shortcuts & some more code

Exploring a new data set

One of the following may be helpful as you explore the data set:

```
View(Carseats)
help(Carseats)
str(Carseats)
```

Loops and selections from data frames

You may want to consider some of the following functions or commands as you write code to solve the exam.

```
tmp_data_set <- mtcars
tmp_col <- tmp_data_set[,1]
tmp_rows <- tmp_data_set[c(1,2,3,5),]
sapply(tmp_data_set[,1:7], max) # applies a function (in this case, `max`) to
all of the indicated columns of the data frame

##      mpg      cyl    disp      hp    drat      wt      qsec
## 33.900   8.000 472.000 335.000  4.930   5.424  22.900
```

Getting a 'nice' printout of the coefficients table

Run the following R chunk.

```
kable(coef(summary(lm.fit)), digits = c(4, 5, 2, 4))
```

Overlaying a linear regression line on a data scatterplot with ggplot

Here is a ggplot command that overlays a linear regression line on a scatterplot of PREDICTORNAME vs. RESPONSENAME. Of course, you should edit the xlab and ylab arguments to produce more meaningful axis labels.

Run the following R chunk.

```
qplot(data = NAMEDATASET, x = PREDICTORNAME, y = RESPONSENAME,
      xlab = "type name of predictor variable here", ylab = "type name of
response variable here") + stat_smooth(method = "lm")
```

You can use this code to get a plot to answer the following type of a question: does the linear model appear to fit the data well?

Computing the MSE

Once you run `lm` and save `your.output <- summary(lm)`, the mean squared error is given by `mean(your.output$residuals^2)`. You could write a function to calculate this, e.g.:

```
mse <- function(my.output)
  mean(my.output$residuals^2)
```

You can also use the `MSE` function for the predicted and true values, which you previously saved as `y_predicted` and `y_true`:

```
MSE(y_predicted, y_true)
```

Of course, you have to remember that there is a *training MSE* and a *testing MSE*, computed on the two different subsets of the sample data.

Fitting linear regression with interaction effects

To illustrate how one fits a model with interaction effects, let's run some simple code on a different data set:

```
data("Auto", package = "ISLR")
lm.fit <- lm(mpg ~ cylinders * displacement + displacement * weight, data =
Auto)
summary(lm.fit)

##
## Call:
## lm(formula = mpg ~ cylinders * displacement + displacement *
##     weight, data = Auto)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.2934  -2.5184  -0.3476   1.8399  17.7723
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   52.623409829  2.237444964  23.519  < 2e-16 ***
## cylinders      0.760640513  0.766949203   0.992   0.322
## displacement -0.073512773  0.016694640  -4.403 1.38e-05 ***
## weight       -0.009888167  0.001329428  -7.438 6.69e-13 ***
## cylinders:displacement -0.002986051  0.003425720  -0.872   0.384
## displacement:weight  0.000021277  0.000005002   4.254 2.64e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.103 on 386 degrees of freedom
```

```
## Multiple R-squared:  0.7272, Adjusted R-squared:  0.7237  
## F-statistic: 205.8 on 5 and 386 DF,  p-value: < 2.2e-16
```

The model fitted is

$\text{mpg} = 52.62 + 0.76 \text{ cylinders} + -0.07 \text{ displacement} + -0.01 \text{ weight} + -0.003 \text{ cylinders} * \text{displacement} + 0 \text{ displacement} * \text{weight}.$

Pro-tip: In the above line, I used an in-line `r` chunk!

As we learned in the lecture, when using interaction terms, we follow the *hierarchical model* rule.

From the output, we see that interaction between displacement and weight is statistically significant, while the interaction between cylinders and displacement is not.