

# Optimization module

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# Abstract

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The objective of this document is to provide a structure for all future documentation for all products.

In this paper, we illustrate some of the optimization techniques which has been implemented namely:

- Travelling salesman problem
- Transportation problem

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## 1 Travelling Salesman Problem

The travelling salesman problem (TSP) is about given a list of cities and the distances between each pair of cities, what is the shortest possible route that visits each city exactly once and returns to the origin city

*Data Used:*

$$i \in I$$

$$j \in I$$

$$D_{ij}$$

*Decision variables:*

$$X_{ij} = \begin{cases} 1, & \text{if salesman travels from } i \text{ to } j \\ 0, & \text{otherwise} \end{cases}$$

$$U_i \in \text{Integer}$$

$$U_j \in \text{Integer}$$

*Objective function:*

$$\min \sum_{i \in I} \sum_{j \in I} X_{ij} \times D_{ij} \quad (1)$$

*s.t.*

Each node should be entered and exited exactly once

$$\sum_i X_{ij} = 1$$

$$\forall j \quad (2) \quad \sum_{d \in D} X_{sd} \leq Q_s$$

$$\forall s \quad (6)$$

$$\sum_j X_{ij} = 1$$

$$\forall i \quad (3)$$

For a demand node, units shipped must be greater than or equal to the demand quantity

Eliminate subtours

$$U_i - U_j + N \times X_{ij} = N - 1 \quad \forall i \in 1, 2..N - 1 \quad j \in 2..N \quad (4) \quad \sum_{s \in S} X_{sd} \geq Q_d \quad \forall d \quad (7)$$

## 2 Transportation Problem

Transportation problem is about goods being transported from a set of sources to a set of destinations subject to the supply and demand of the sources and destination respectively such that the total cost of transportation is minimized. It is also sometimes called as Hitchcock problem

*Data Used:*

$$s \in S$$

$$d \in D$$

$$C_{sd}, Q_s, Q_d$$

*Decision variables:*

$$X_{sd} \in \text{Integer}$$

*Objective function:*

$$\min \sum_{s \in S} \sum_{d \in D} X_{sd} \times C_{sd} \quad (5)$$

*s.t.*

For a supply node, units shipped must be less than or equal to the supply quantity

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## Nomenclature

$i$	Source city
$j$	Destination city
$I$	Set of cities
$N$	Total number of cities ( $I$ )
$D_{ij}$	Distance between source city $i$ and destination city $j$
$X_{ij}$	Binary flag, sales man travels from source city $i$ to destination city $j$
$U_i$	Integer, artificial variable for source city $i$
$U_j$	Integer, artificial variable for destination city $j$