

TUTORIAL - 1

1)

7 6 5 $\boxed{4}$ 3 $\boxed{2}$ $\boxed{1}$

3rd row $\underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{1} \quad \underline{0} \quad \underline{0}$

In, 2nd row, position 4, there's error.

→ 0012100101 110 11100000

снот

2)

5 bit Message = 10011

Formula: $(m+r+1) \leq 2^r$

$$5+r+1 \leq 2^r$$

$$6+r \leq 2^r$$

Least value of r that satisfies the inequality

$$\boxed{r=4}$$

\therefore Redundant bits are positioned at 1, 2, 4, 8
(powers of 2)

Total no. of bits = Data bits + Redundant bits
 $= 5 + 4 = \boxed{9}$

Here, $G_1 \rightarrow (9, 7, 5, 3, 1)$
 $G_2 \rightarrow (7, 6, 3, 2)$
 $G_4 \rightarrow (7, 6, 5, 4)$
 $G_8 \rightarrow (9, 8)$

Parity bits are at positions 1, 2, 4, 8.

• BEFORE COMPUTING REDUNDANT BITS

9	8	7	6	5	4	3	2	1
1		0	0	1		1		
P_4			P_3			P_2		P_1

• COMPUTING REDUNDANT BITS

$$\begin{array}{cccc}
 8 & 4 & 2 & 1 \\
 G_8 = \{1, 1\} & G_4 = \{0, 0, 1, 1\} & G_2 = \{0, 0, 1, 0, 1, 1, 1\} & G_1 = \{1, 0, 1, 1, 1, 1, 1, 1\}
 \end{array}$$

Here, $G_8 = \{1, 1\} \Rightarrow P_8 = 1$

$G_4 = \{0, 0, 1, 1\} \Rightarrow P_4 = 1$

$G_2 = \{0, 0, 1, 1\} \Rightarrow P_2 = 1$

$G_1 = \{1, 0, 1, 1, 1, 1, 1, 1\} \Rightarrow P_1 = 1$

• AFTER COMPUTING REDUNDANT BITS

8	7	6	5	4	3	2	1
1	1	0	0	1	1	1	1

Answer : 11001111

3)

$$G(x) = x^4 + x + 1$$

$$= x^4 + 0x^3 + x^2 + x + 1$$

$$= 10111 \Rightarrow \text{Degree } r = 4$$

Binary form after adding zeros = 110010000
 $M(x)$

Dividing it by 10111 i.e. $G(x)$,

$$\begin{array}{r}
 11100 \\
 10111 \overline{) 110010000} \\
 \underline{10111} \\
 \phi 11100000 \\
 \underline{10111} \\
 \phi 1011000 \\
 \underline{10111} \\
 000100 \\
 \underline{000000} \\
 00100 \\
 \underline{00000} \\
 0100
 \end{array}$$

Quotient : 11100

Remainder : 0100

Transmitted value = 110010100

Here, $T(x) = R(x) + M(x)$

$$T(x) = 110010100$$

4)

$$M(x) = 110011$$

$$G(x) = 1001$$

Here, Degree = $\boxed{3}$

110011000 to be divided by $G(x)$ to check if any transmission error exists.

$$\begin{array}{r}
 110011000 \\
 1001 \downarrow \\
 \hline
 \cancel{0}1011 \\
 1001 \downarrow \\
 \hline
 \cancel{0}\cancel{0}1010 \\
 1001 \downarrow \\
 \hline
 \cancel{0}\cancel{0}1100 \\
 1001 \downarrow \\
 \hline
 101
 \end{array}$$

Here, remainder is not zero.

\therefore Transmission error

There is no transmission error only when remainder of $\frac{M(x)}{G(x)}$ is zero.