

LAB SHEET 02

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ROLL NO: EE23B039

A. Implementation of convolution

1. Generate a random impulse response sequence $h[n]$, $0 \leq n \leq m$ where $h[n] \sim u[a,b]$.
2. Generate a random input sequence $x[n]$, $0 \leq n \leq m$ where $x[n] \sim u[c,d]$
3. Write a function to compute the output sequence $y[n] = x[n] * h[n] = \sum_{k=0}^{\infty} (x[k] h[n-k])$ for $n = 0, 1, 2 \dots n+m$. Function name as conv_EE23B039.
4. Plot $y[n]$ vs n .
5. Verify your result using conv command.
6. Repeats the exercise for a few more randomly generated $x[n]$ and $h[n]$.

```
%Declaring the variables
m = 7; %Max value
a = -2; % lower bound
b = 2; % upper bound
c = -1; %lower bound
d = 1; % upper bound
```

Question 1 :

```
h_n = a + (b-a).*rand(1,m+1);
```

Question 2:

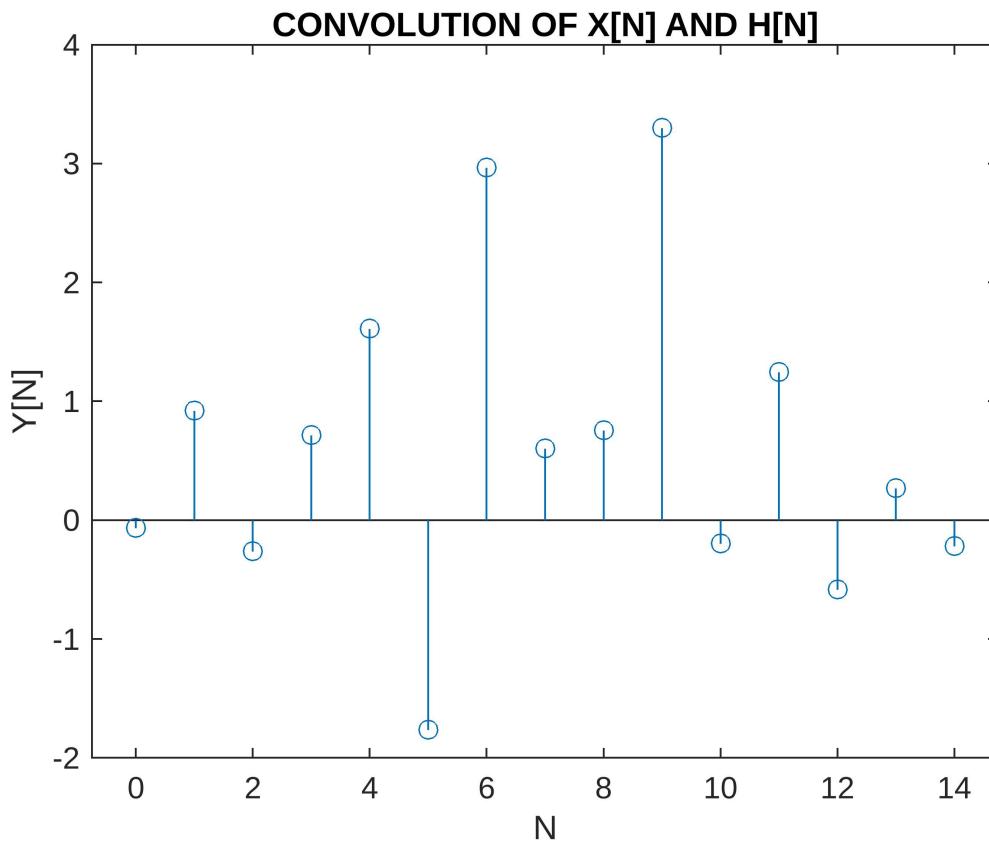
```
x_n = c + (d-c).* rand(1,m+1);
```

Question 3:

```
y_n1 = CONV_EE23B039(x_n,h_n);
```

Question 4:

```
n = 0:1:2*m;
stem(n,y_n1);
xlabel("N");
ylabel("Y[N]");
title("CONVOLUTION OF X[N] AND H[N]")
```



question 5:

```

y_n2 = conv(x_n,h_n);
if(y_n1 == y_n2)
    disp("True");
else
    disp("False");
end

```

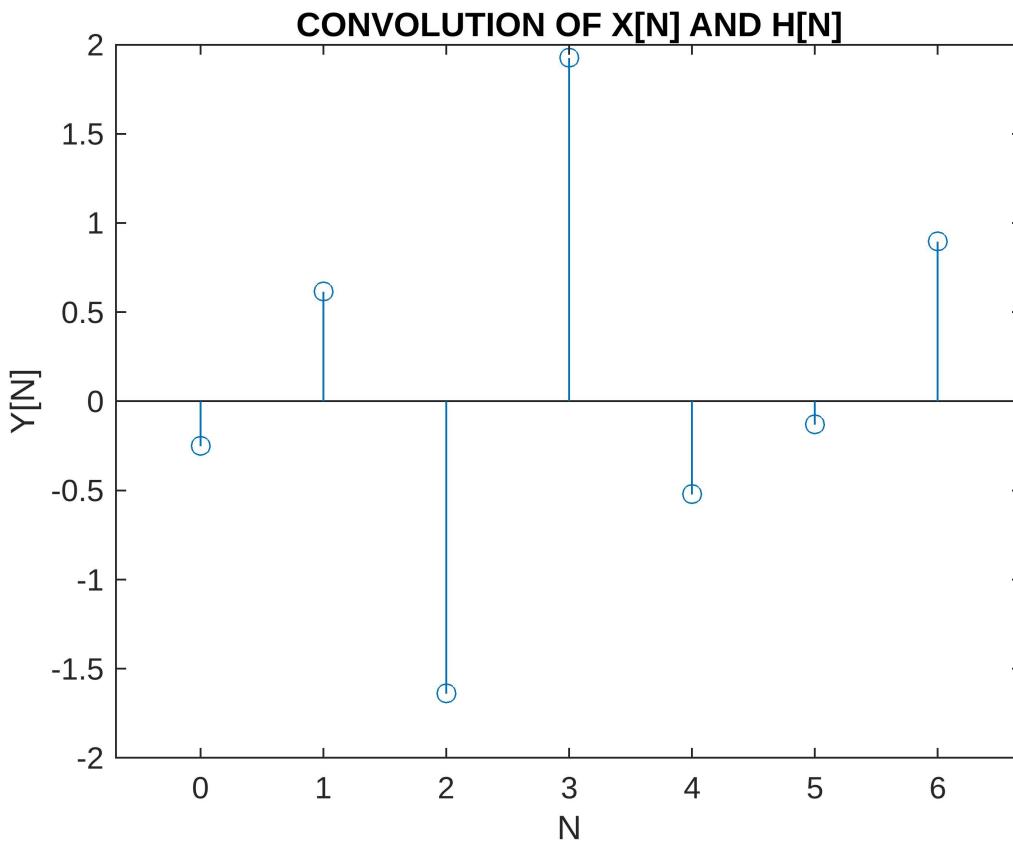
True

Question 6:

```

m = 3;
h_n = a + (b-a).*rand(1,m+1);
x_n = c + (d-c).* rand(1,m+1);
y_n1 = CONV_EE23B039(x_n,h_n);
n = 0:1:2*m;
stem(n,y_n1);
xlabel("N");
ylabel("Y[N]");
title("CONVOLUTION OF X[N] AND H[N]");

```



```

y_n2 = conv(x_n,h_n);
if(y_n1 == y_n2)
    disp("True");
else
    disp("False");
end

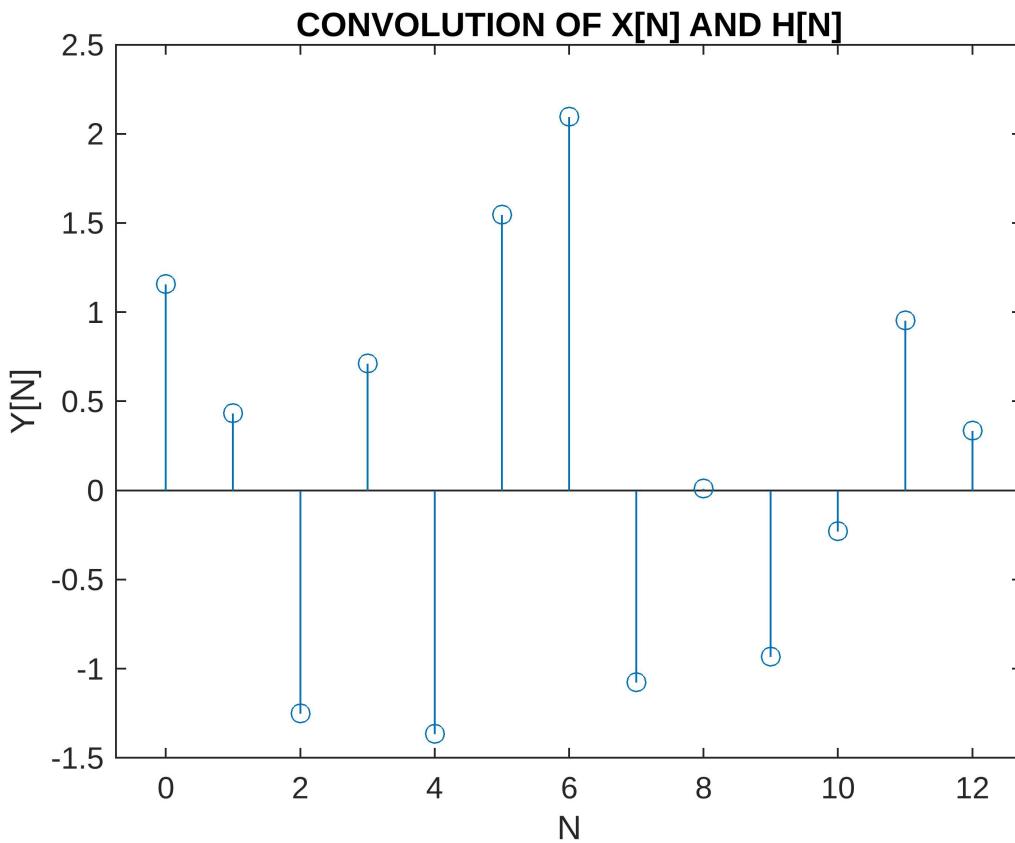
```

True

```

m = 6;
h_n = a + (b-a).*rand(1,m+1);
x_n = c + (d-c).* rand(1,m+1);
y_n1 = CONV_EE23B039(x_n,h_n);
n = 0:1:2*m;
stem(n,y_n1);
xlabel("N");
ylabel("Y[N]");
title("CONVOLUTION OF X[N] AND H[N]");

```



```

y_n2 = conv(x_n,h_n);
if(y_n1 == y_n2)
    disp("True");
else
    disp("False");
end

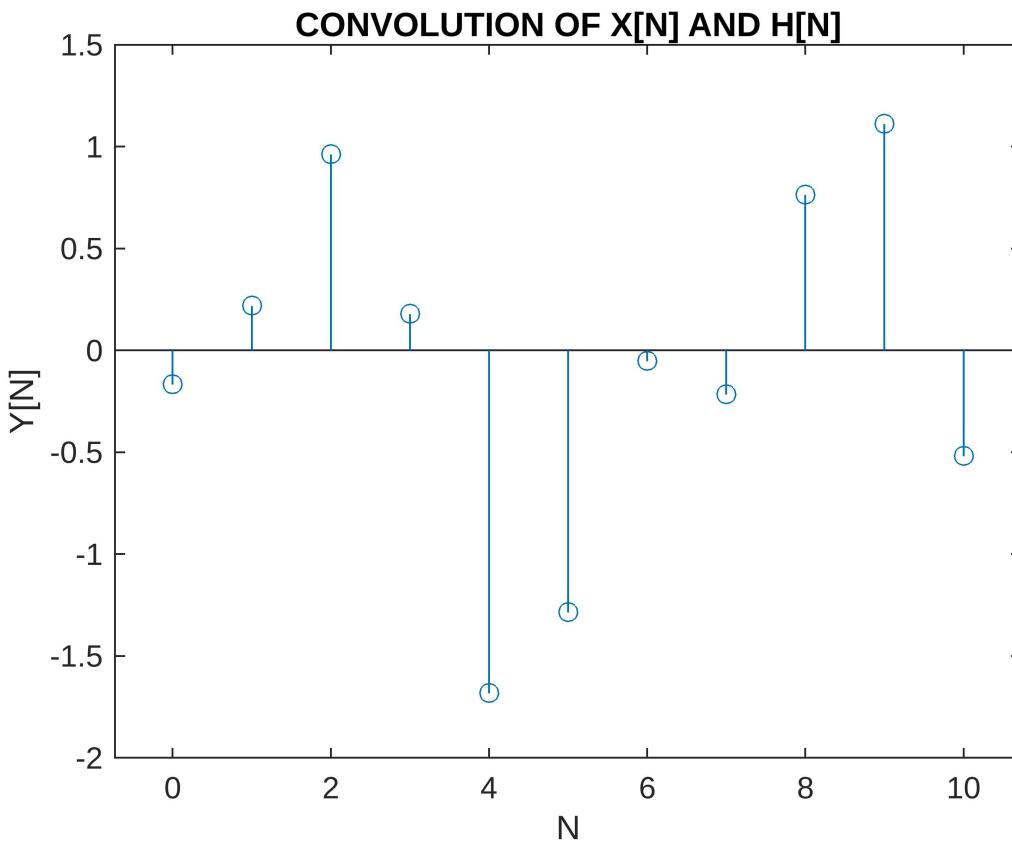
```

True

```

m = 5;
h_n = a + (b-a).*rand(1,m+1);
x_n = c + (d-c).* rand(1,m+1);
y_n1 = CONV_EE23B039(x_n,h_n);
n = 0:1:2*m;
stem(n,y_n1);
xlabel("N");
ylabel("Y[N]");
title("CONVOLUTION OF X[N] AND H[N]");

```



```

y_n2 = conv(x_n,h_n);
if(y_n1 == y_n2)
    disp("True");
else
    disp("False");
end

```

True

B. SYSTEMS IN PARALLEL

1. Generate a random $h_1[n]$ $0 \leq n \leq m_1$ and $h_2[n]$ $0 \leq n \leq m_2$.
2. Generate random $x[n]$ $0 \leq n \leq N$.
3. Obtain $y_1[n] = x[n] * h_1[n]$ and $y_2[n] = x[n] * h_2[n]$ using your command. Compute $Y_a[n] = y_1[n] + y_2[n]$.
4. Similarly obtain $Y_b[n] = x[n] * (h_1[n] + h_2[n])$.
5. Compare $Y_a[n]$ with $Y_b[n]$. Report your observations.
6. Repeat the experiments for a few values of random generated $h_1[n], h_2[n]$ and $x[n]$.

Question 1

```

m1=7;
m2=9;
h1_n = 0+m1.*rand(1,8);
h2_n = 0+m2.*rand(1,8);

```

Question 2

```
N = 15;  
x_n = N.*rand(1,N+1);
```

Question 3

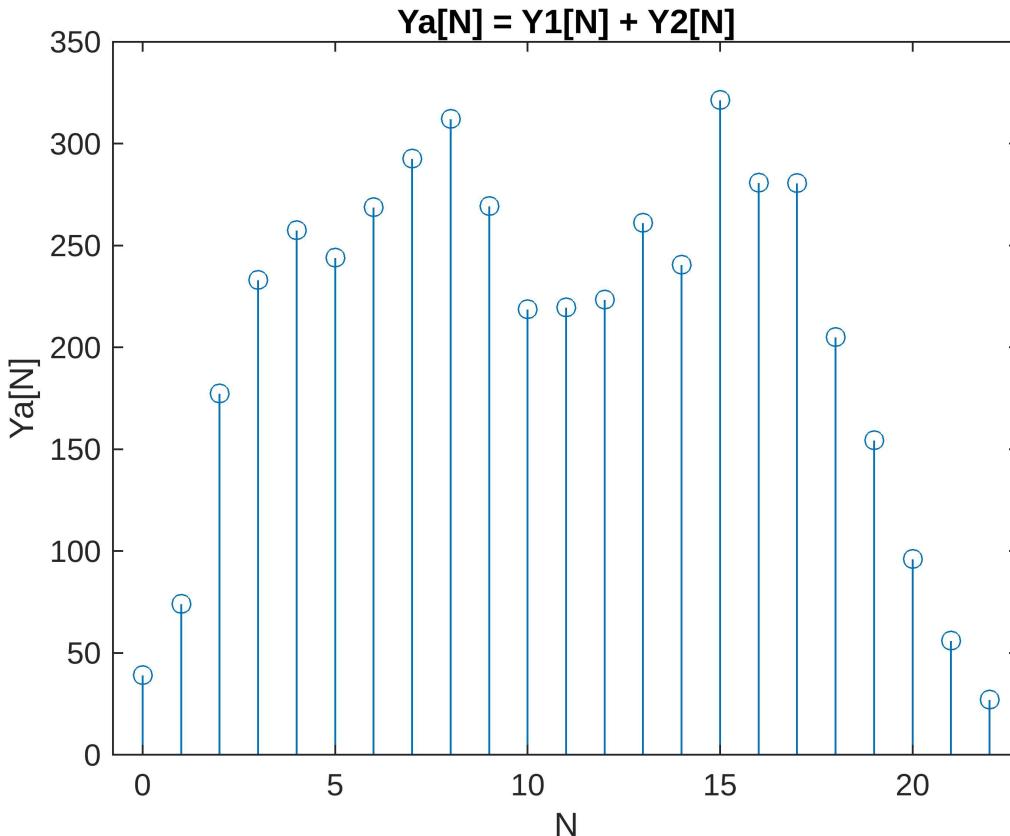
```
y1_n = conv(x_n,h1_n);  
y2_n = conv(x_n,h2_n);  
Ya_n = y1_n + y2_n;
```

Question 4

```
h_n = h1_n + h2_n;  
Yb_n = conv(x_n,h_n);
```

Question 5

```
n=0:1:22;  
stem(n,Ya_n);  
xlabel("N");  
ylabel("Ya[N]");  
title("Ya[N] = Y1[N] + Y2[N]");
```

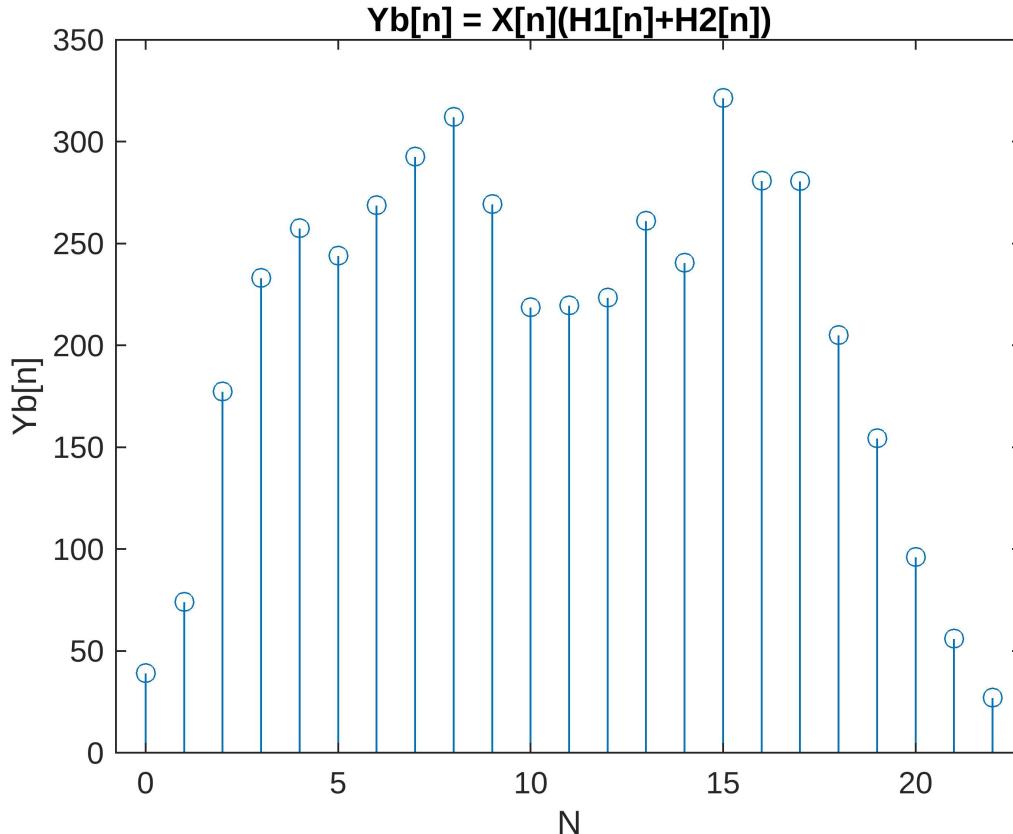


```
stem(n,Yb_n);  
xlabel("N");
```

```

ylabel("Yb[n]");
title("Yb[n] = X[n](H1[n]+H2[n])")

```



```

% As we can see both Ya[n] and Yb[n] both are same , this shows that the
% property of the system being in parallel.

```

Question 6

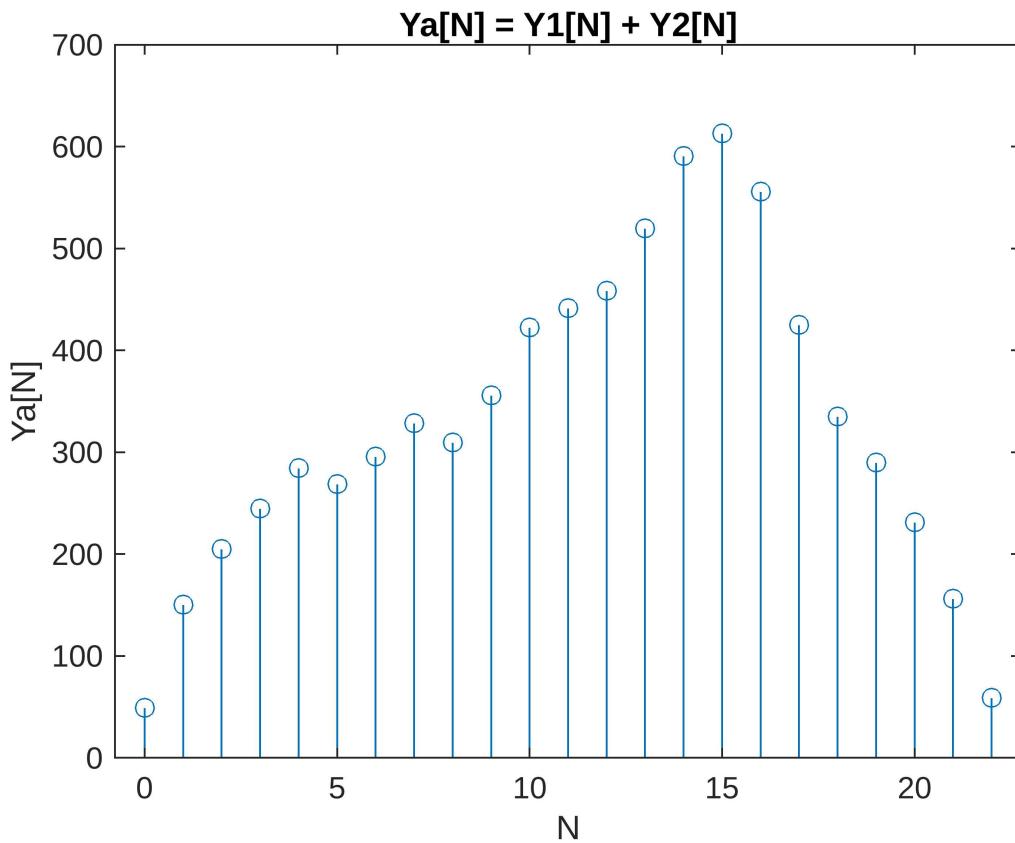
```
display("MORE EXAMPLES");
```

"MORE EXAMPLES"

```

h1_n = 0+m1.*rand(1,8);
h2_n = 0+m2.*rand(1,8);
x_n = N.*rand(1,N+1);
y1_n = conv(x_n,h1_n);
y2_n = conv(x_n,h2_n);
Ya_n = y1_n + y2_n;
h_n = h1_n + h2_n;
Yb_n = conv(x_n,h_n);
n=0:1:22;
stem(n,Ya_n);
xlabel("N");
ylabel("Ya[N]");
title("Ya[N] = Y1[N] + Y2[N]");

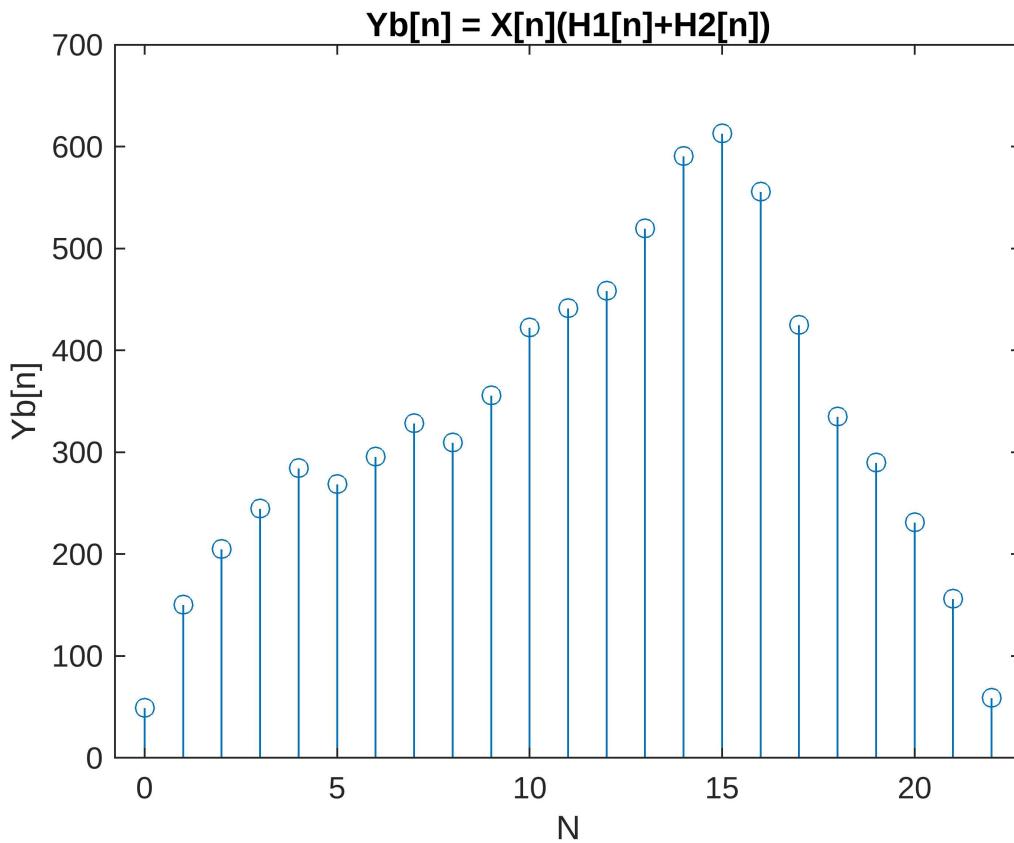
```



```

stem(n,Yb_n);
xlabel("N");
ylabel("Yb[n]");
title("Yb[n] = X[n] (H1[n]+H2[n])")

```

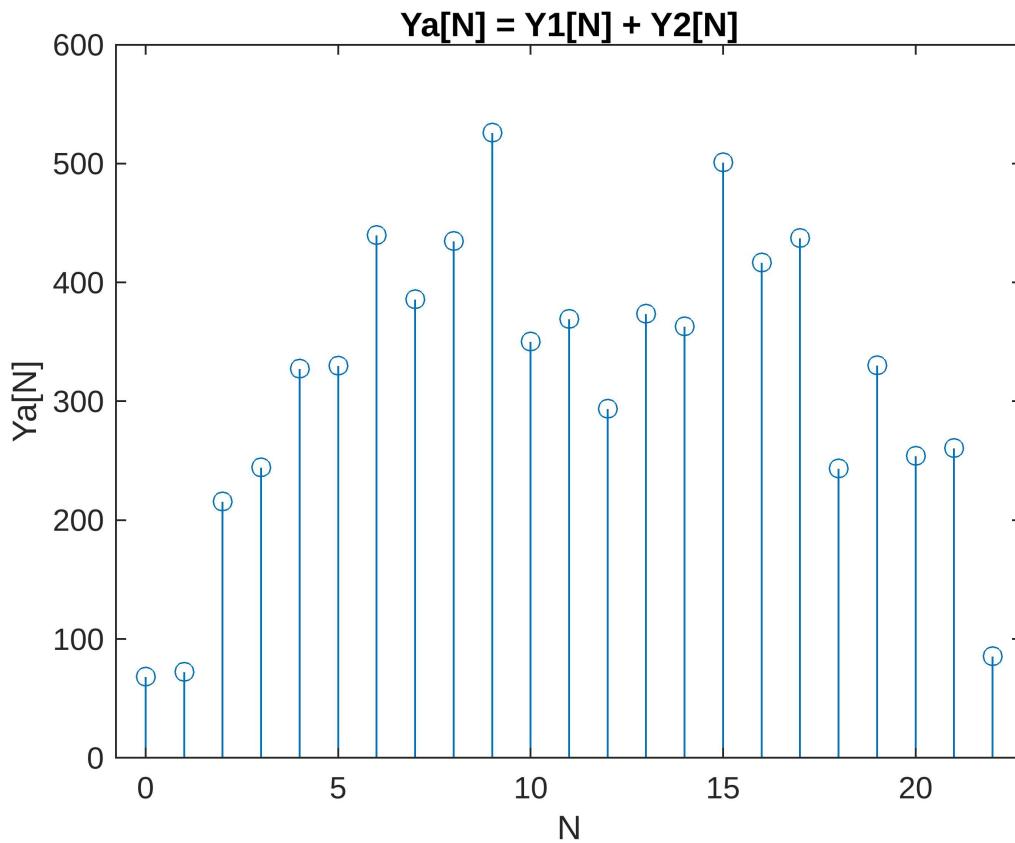


```
display("Example 2");
```

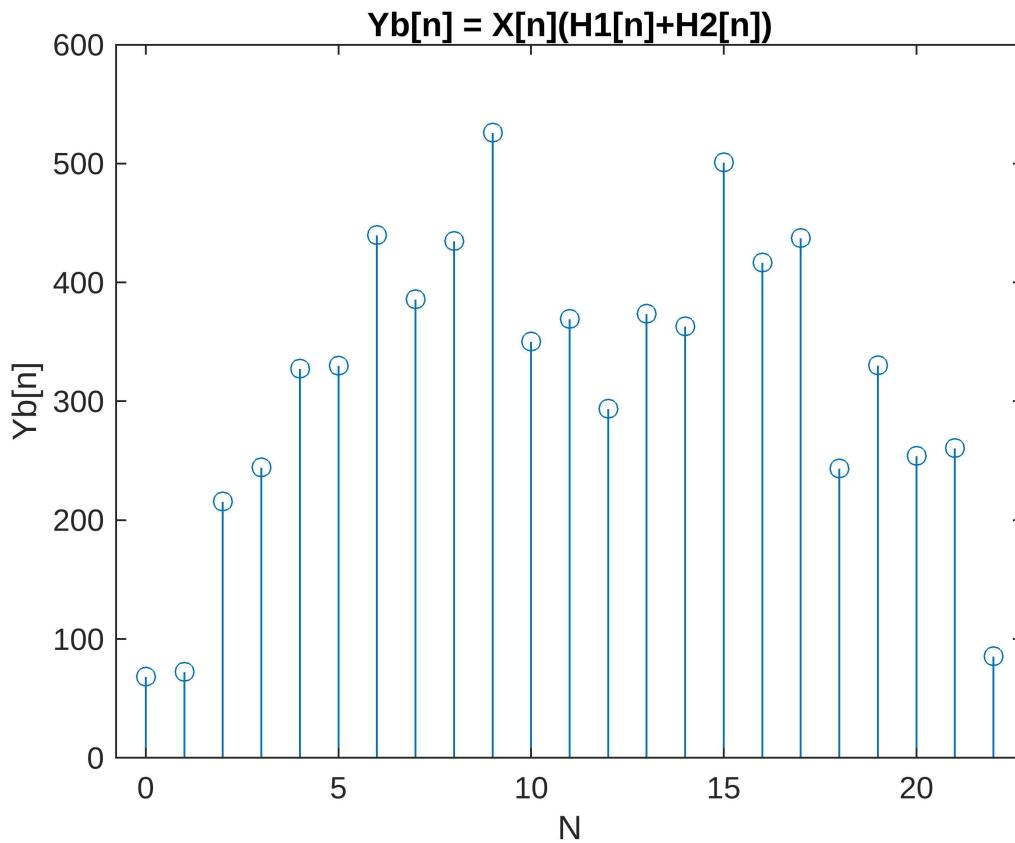
```
"Example 2"
```

```

h1_n = 0+m1.*rand(1,8);
h2_n = 0+m2.*rand(1,8);
x_n = N.*rand(1,N+1);
y1_n = conv(x_n,h1_n);
y2_n = conv(x_n,h2_n);
Ya_n = y1_n + y2_n;
h_n = h1_n + h2_n;
Yb_n = conv(x_n,h_n);
n=0:1:22;
stem(n,Ya_n);
xlabel("N");
ylabel("Ya[N]");
title("Ya[N] = Y1[N] + Y2[N]");
```



```
stem(n,Yb_n);
xlabel("N");
ylabel("Yb[n]");
title("Yb[n] = X[n] (H1[n]+H2[n])")
```



C. SYSTEMS IN CASCADE

1. Generate a random $h1[n]$ $0 \leq n \leq m1$ and $h2[n]$ $0 \leq n \leq m2$.
2. Generate random $x[n]$ $0 \leq n \leq N$.
3. Obtain
 - i) $x1[n] = x[n] * h1[n]$
 - ii) $Ya[n] = x1[n] * h2[n]$
4. Similarly compute
 - i) $x2[n] = x[n] * h2[n]$
 - ii) $Yb[n] = x2[n] * h1[n]$
5. Finally obtain
 - i) $h[n] = h1[n] * h2[n]$
 - ii) $Yc[n] = x[n] * h[n]$
6. Compare $Ya[n]$, $Yb[n]$ and $Yc[n]$. Report your observations.
7. Repeat the experiments for a few values of random generated $h1[n]$, $h2[n]$ and $x[n]$.

Question 1

```
m1=3;  
m2=5;  
h1_n = 0+m1.*rand(1,m1+1);  
h2_n = 0+m2.*rand(1,m2+1);
```

Question 2

```
N = 10;  
x_n = N.*rand(1,N+1);
```

Question 3

```
x1_n = conv(x_n,h1_n);  
Ya_n = conv(x1_n,h2_n);
```

Question 4

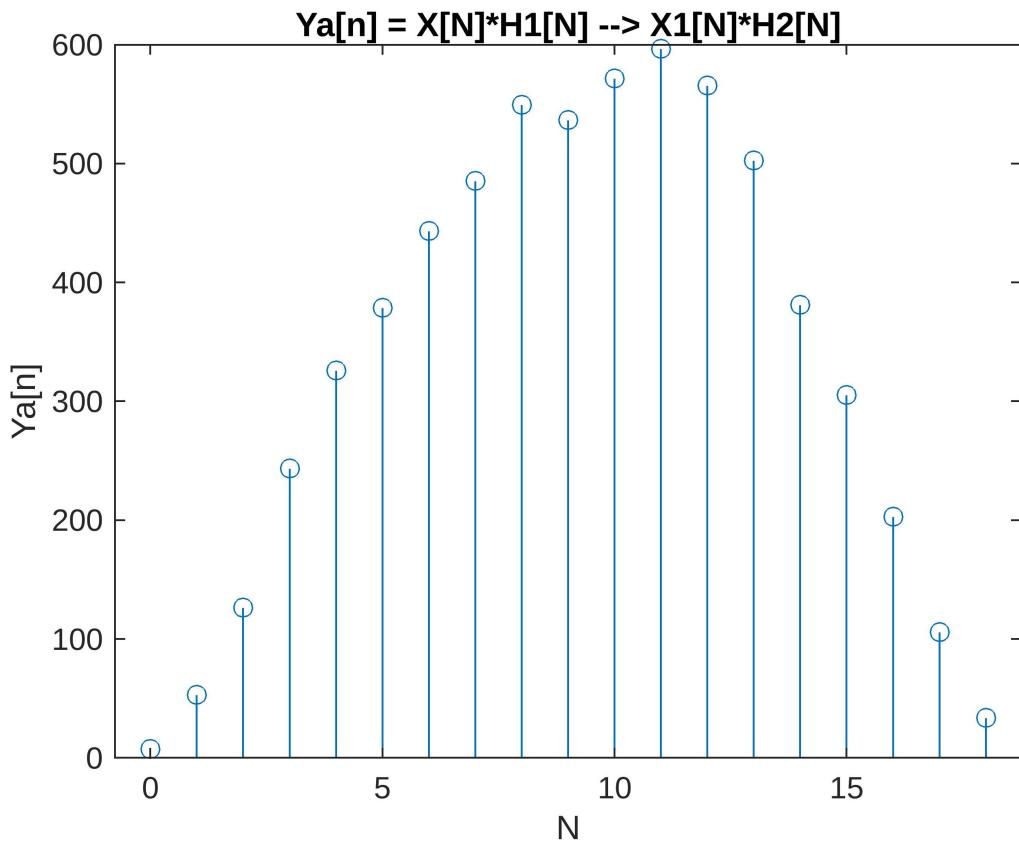
```
x2_n = conv(x_n,h2_n);  
Yb_n = conv(x2_n,h1_n);
```

Question 5

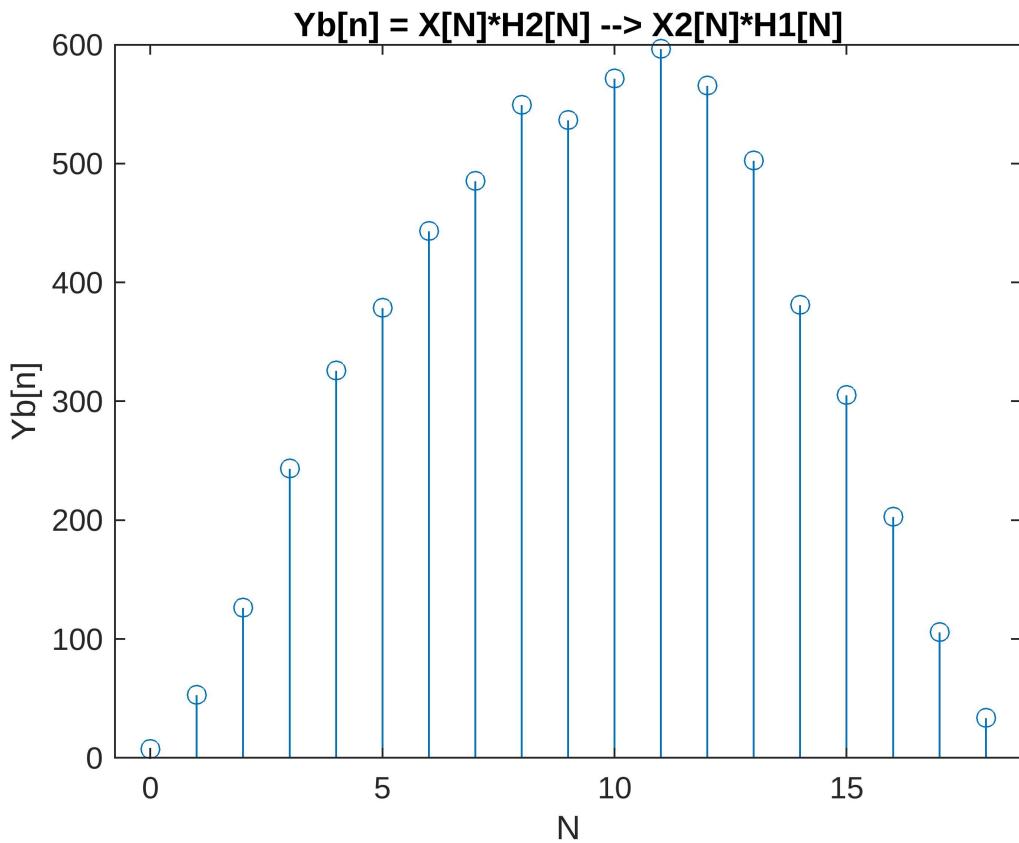
```
h_n = conv(h1_n,h2_n);  
Yc_n = conv(x_n,h_n);
```

Question 6

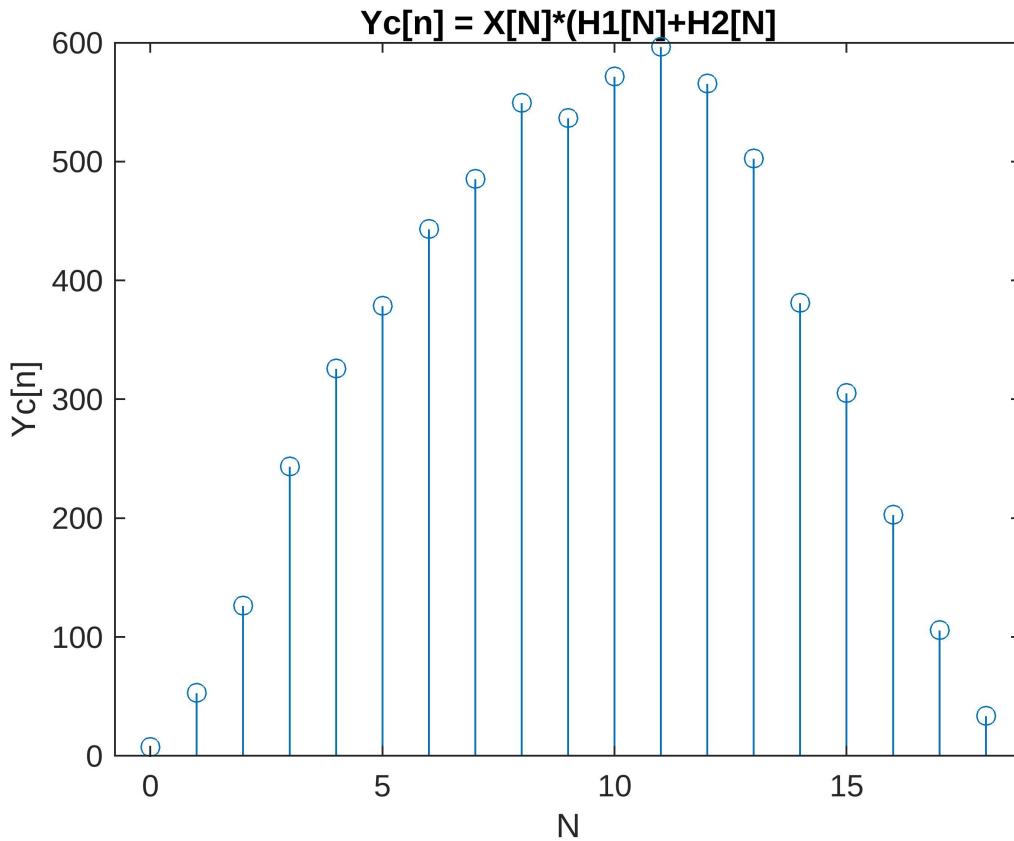
```
n = 0:1:18;  
stem(n,Ya_n);  
xlabel("N");  
ylabel("Ya[n]");  
title("Ya[n] = X[N]*H1[N] --> X1[N]*H2[N]");
```



```
stem(n,Yb_n);
xlabel("N");
ylabel("Yb[n]");
title("Yb[n] = X[N]*H2[N] --> X2[N]*H1[N]");
```



```
stem(n, Yc_n);
xlabel("N");
ylabel("Yc[n]");
title("Yc[n] = X[N] * (H1[N]+H2[N])");
```



```
% As we can see all the plots of Ya[n] , Yb[n] and Yc[n] are same. It show
% the property of cascade systems.
```

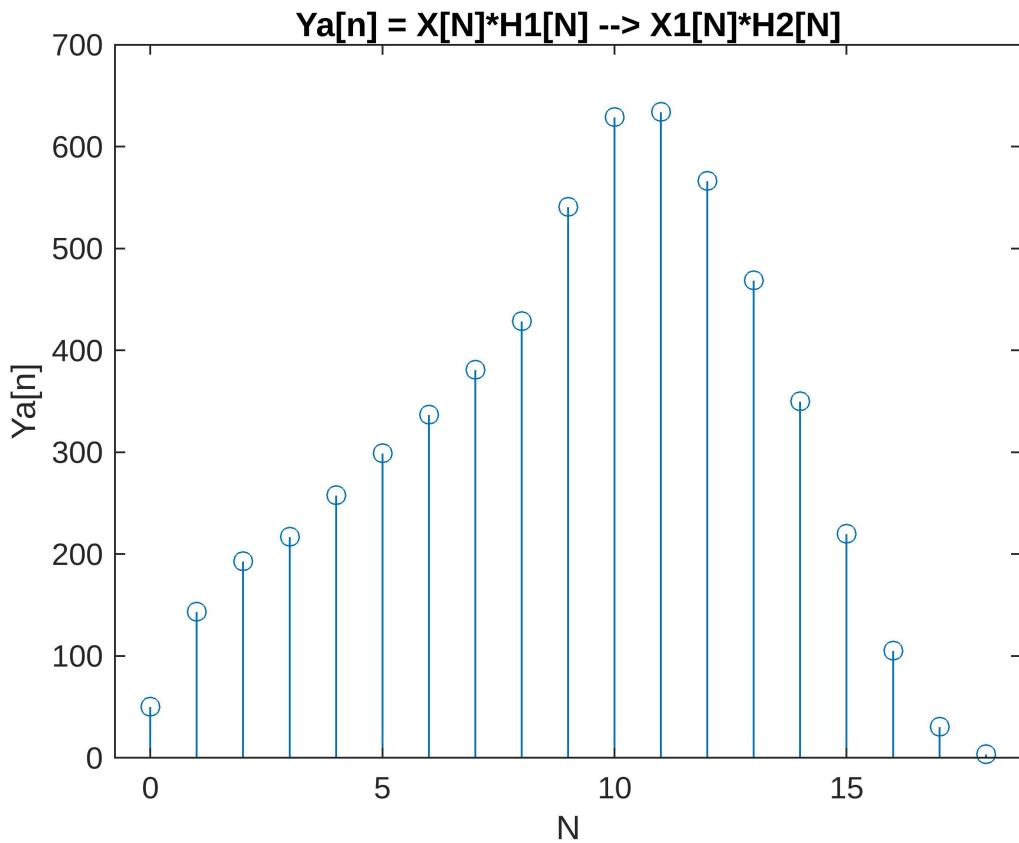
Question 7

```
display("More random generated examples")
```

```
"More random generated examples"
```

```

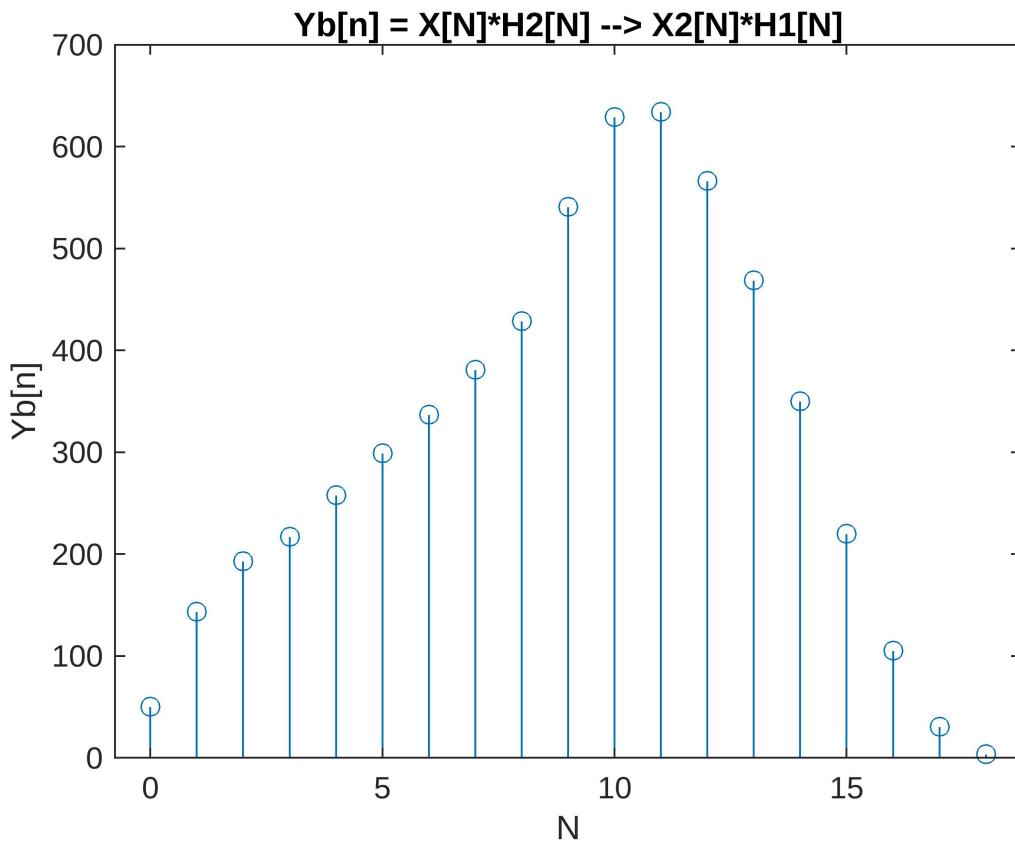
h1_n = 0+m1.*rand(1,m1+1);
h2_n = 0+m2.*rand(1,m2+1);
x_n = N.*rand(1,N+1);
x1_n = conv(x_n,h1_n);
Ya_n = conv(x1_n,h2_n);
x2_n = conv(x_n,h2_n);
Yb_n = conv(x2_n,h1_n);
h_n = conv(h1_n,h2_n);
Yc_n = conv(x_n,h_n);
n = 0:1:18;
stem(n,Ya_n);
xlabel("N");
ylabel("Ya[n]");
title("Ya[n] = X[N]*H1[N] --> X1[N]*H2[N]");
```



```

stem(n,Yb_n);
xlabel("N");
ylabel("Yb[n]");
title("Yb[n] = X[N]*H2[N] --> X2[N]*H1[N]");

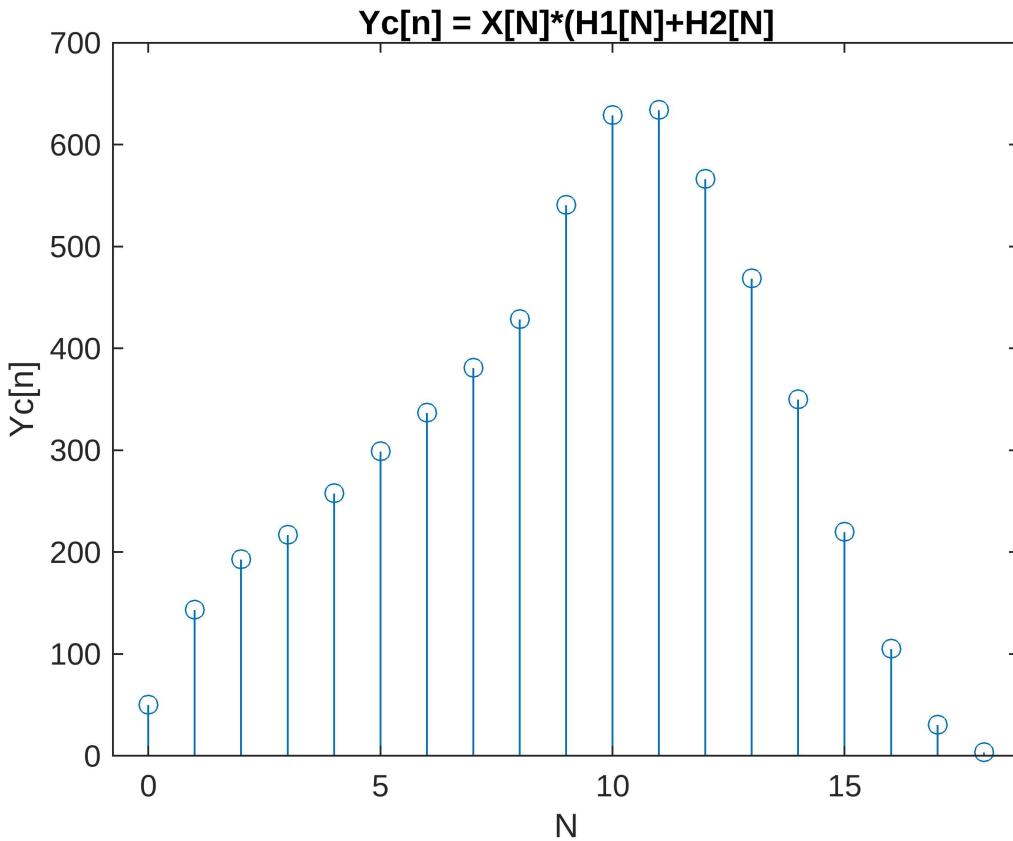
```



```

stem(n,Yc_n);
xlabel("N");
ylabel("Yc[n]");
title("Yc[n] = X[N]*(H1[N]+H2[N])");

```

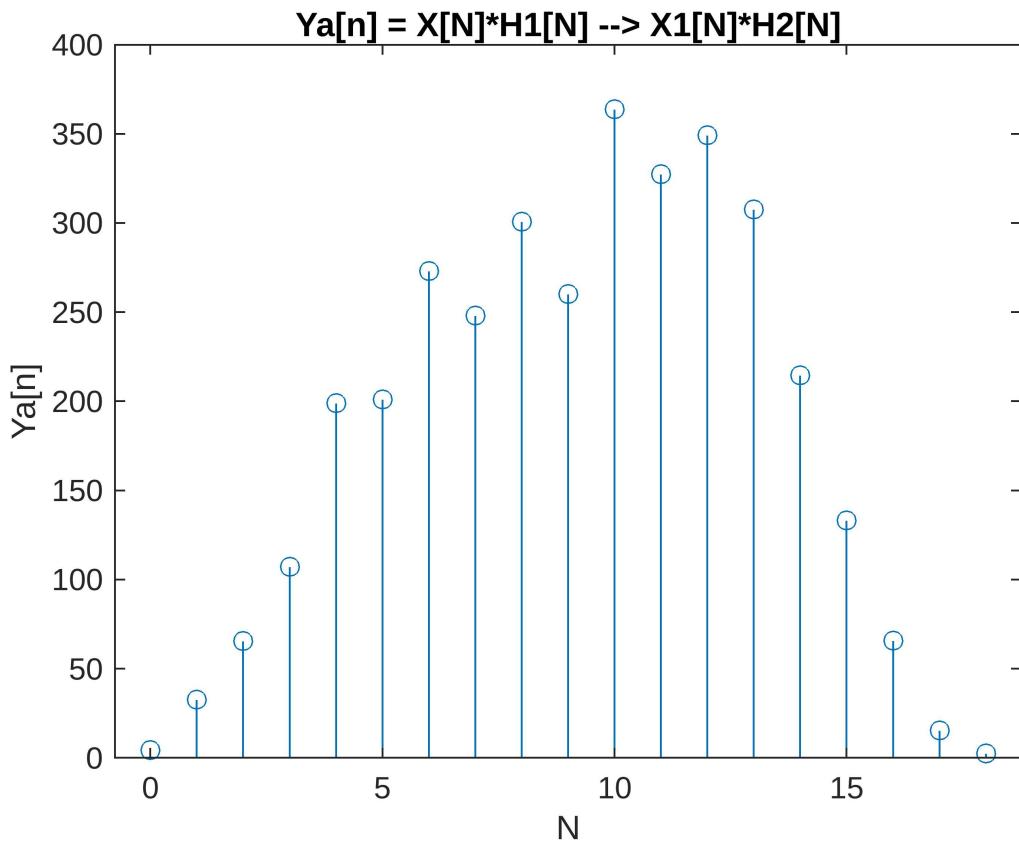


```
display("Example 2");
```

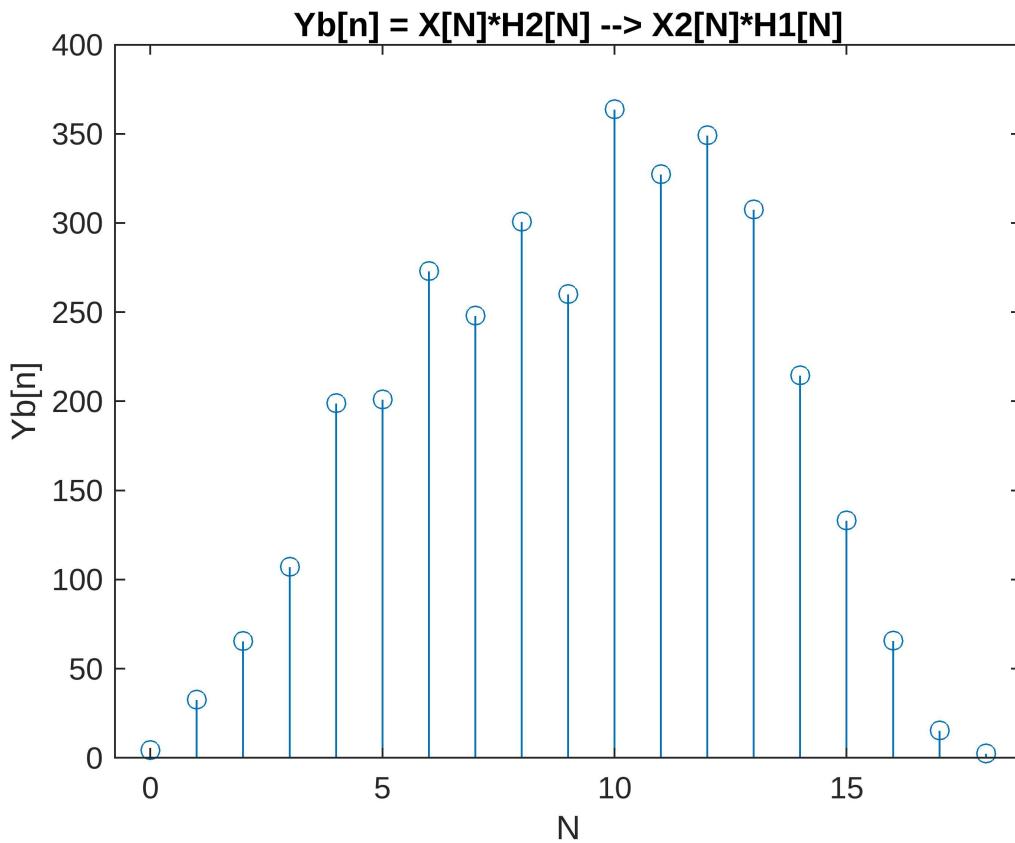
```
"Example 2"
```

```

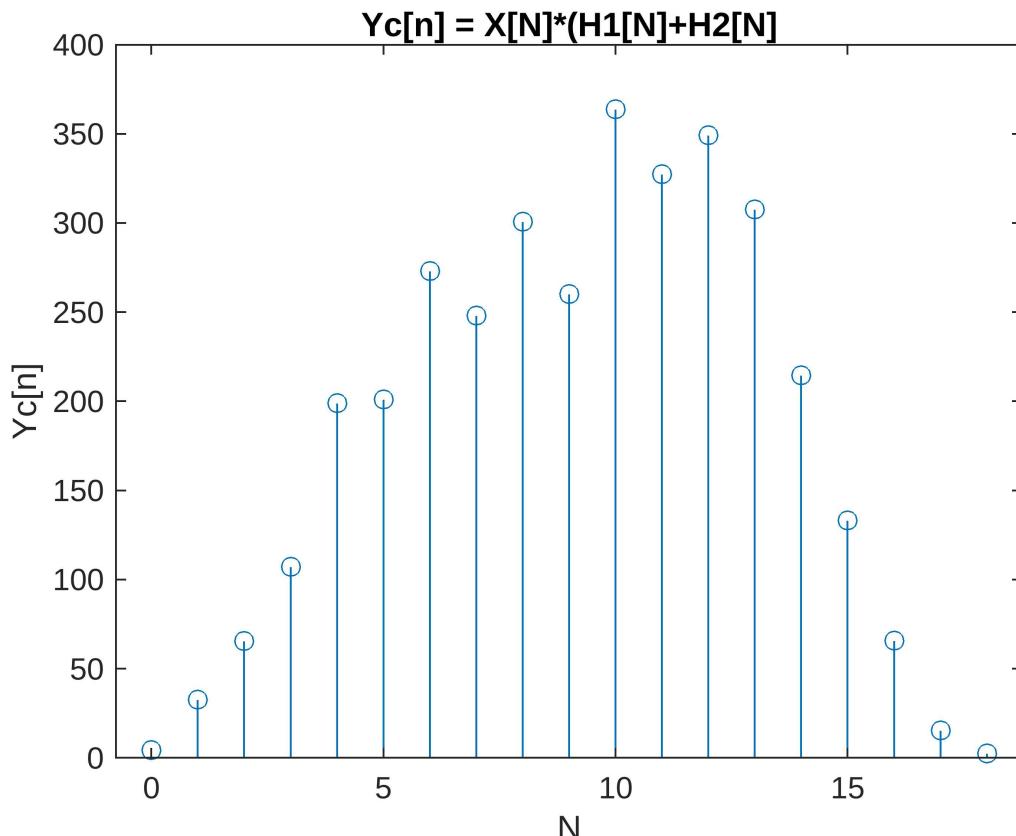
h1_n = 0+m1.*rand(1,m1+1);
h2_n = 0+m2.*rand(1,m2+1);
x_n = N.*rand(1,N+1);
x1_n = conv(x_n,h1_n);
Ya_n = conv(x1_n,h2_n);
x2_n = conv(x_n,h2_n);
Yb_n = conv(x2_n,h1_n);
h_n = conv(h1_n,h2_n);
Yc_n = conv(x_n,h_n);
n = 0:1:18;
stem(n, Ya_n);
xlabel("N");
ylabel("Ya[n]");
title("Ya[n] = X[N]*H1[N] --> X1[N]*H2[N]");
```



```
stem(n,Yb_n);
xlabel("N");
ylabel("Yb[n]");
title("Yb[n] = X[N]*H2[N] --> X2[N]*H1[N]");
```



```
stem(n,Yc_n);
xlabel("N");
ylabel("Yc[n]");
title("Yc[n] = X[N] * (H1 [N]+H2 [N])");
```



D. CONJUGATE SYMMETRY OF FOURIER TRANSFORM

1. Generate a random signal $x[n]$, $0 \leq n \leq N$.
 2. Compute the fourier transform of $x[n]$: $X[e^{j\omega n}] = \sum x[n] e^{-jn\omega}$ $n = N_1$ to N_2 for $\omega = -\pi$ to π
 3. plot i) ω vs $\operatorname{Re}\{X(e^{j\omega})\}$ ii) ω vs $\operatorname{Im}\{X(e^{j\omega})\}$ report your observations.
 4. plot i) ω vs $|X(e^{j\omega})|$ ii) ω vs $\operatorname{ang}(X(e^{j\omega}))$ Report your observations
 5. Repeat the experiments for a few values of random generated $x[n]$.

Question 1

```
N = 20;  
x n = 20.*rand(1,N);
```

Question 2

$$x^f \circ n = fft(x \circ n);$$

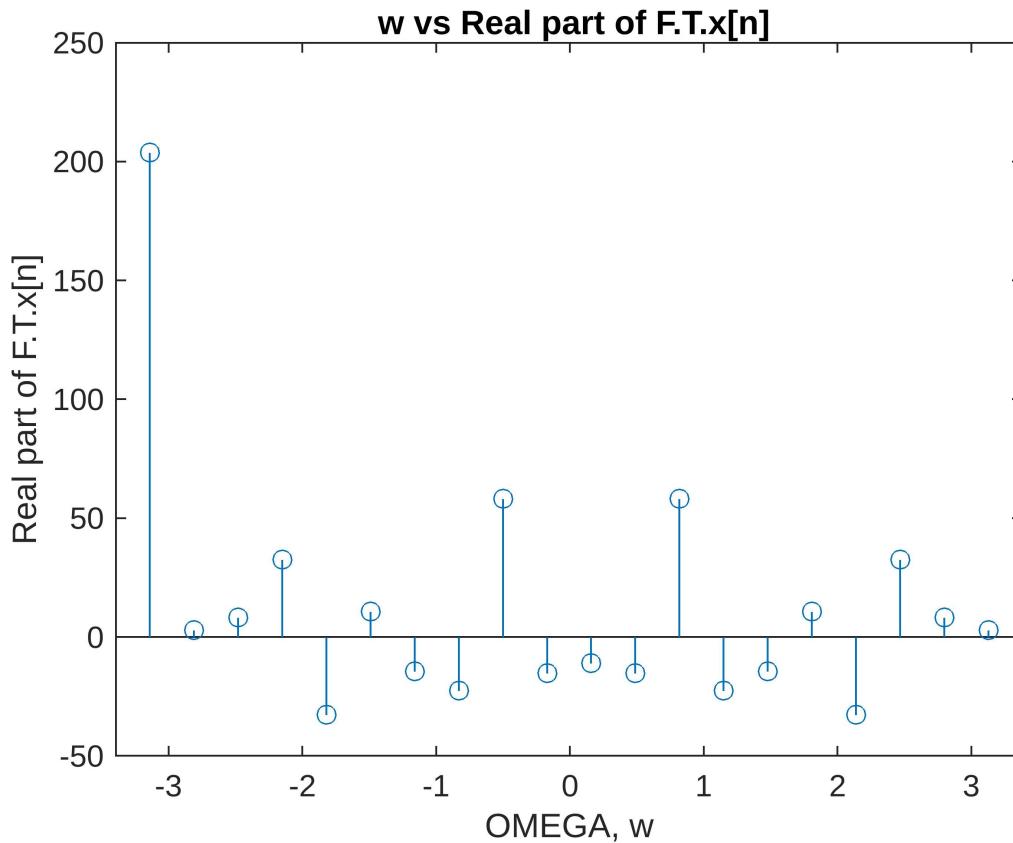
Question 3

```
w = -pi:0.33:pi;
stem(w,real(xf_n));
xlabel("OMEGA, w");
```

```

ylabel("Real part of F.T.{x[n]}");
title(" w vs Real part of F.T.{x[n]}")

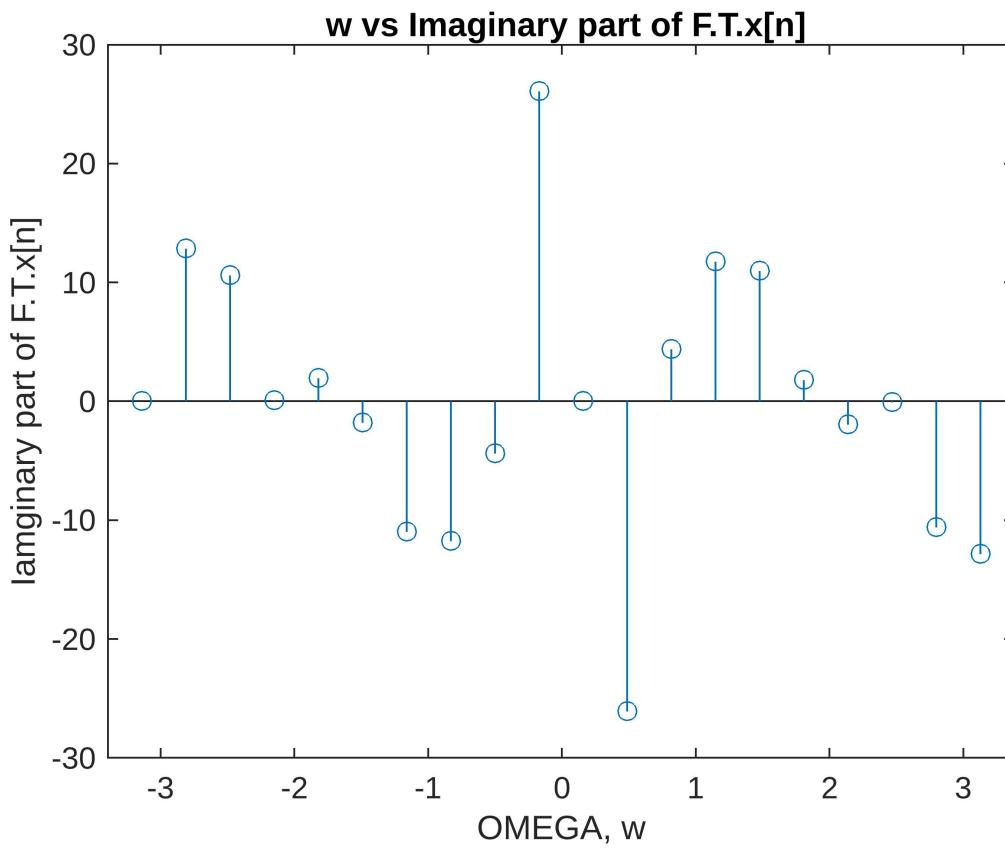
```



```

stem(w,imag(xf_n));
xlabel("OMEGA, w");
ylabel("Imaginary part of F.T.{x[n]}");
title(" w vs Imaginary part of F.T.{x[n]}");

```

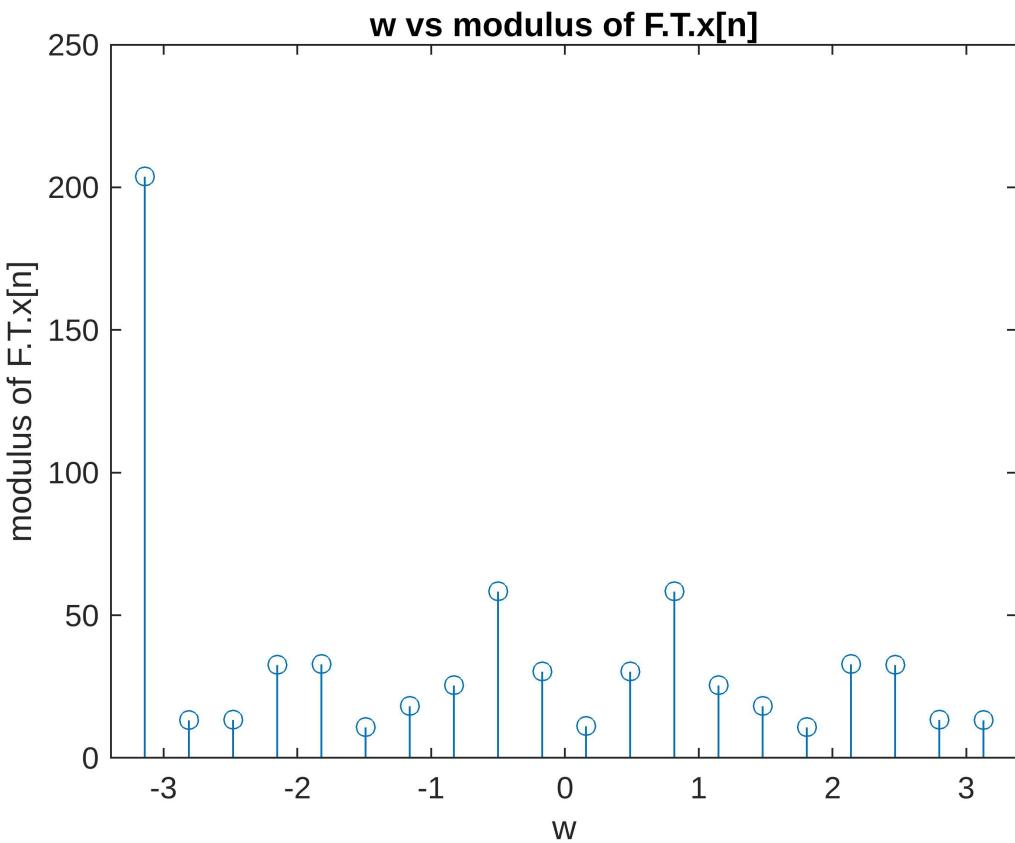


Question 4

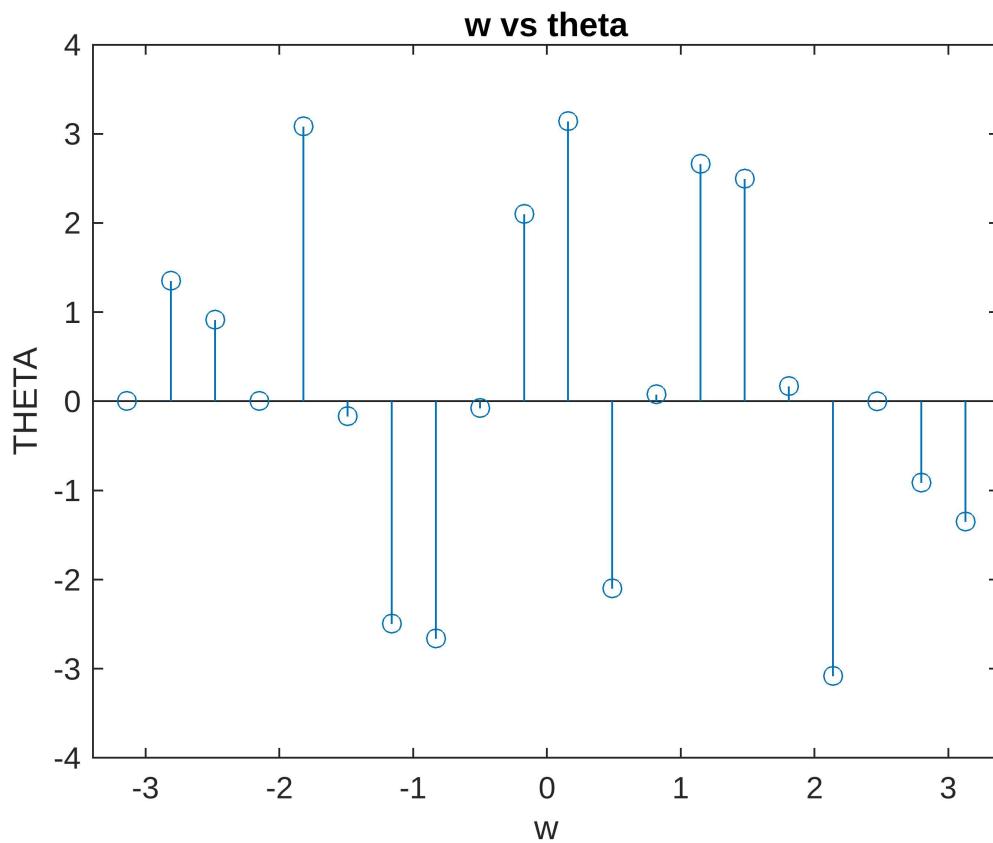
```

mod_xf = abs(xf_n);
stem(w,mod_xf);
xlabel("w");
ylabel("modulus of F.T.{x[n]}");
title("w vs modulus of F.T.{x[n]}");

```



```
theta = angle(xf_n);
stem(w,theta);
xlabel("w");
ylabel("THETA");
title("w vs theta");
```



Question 5

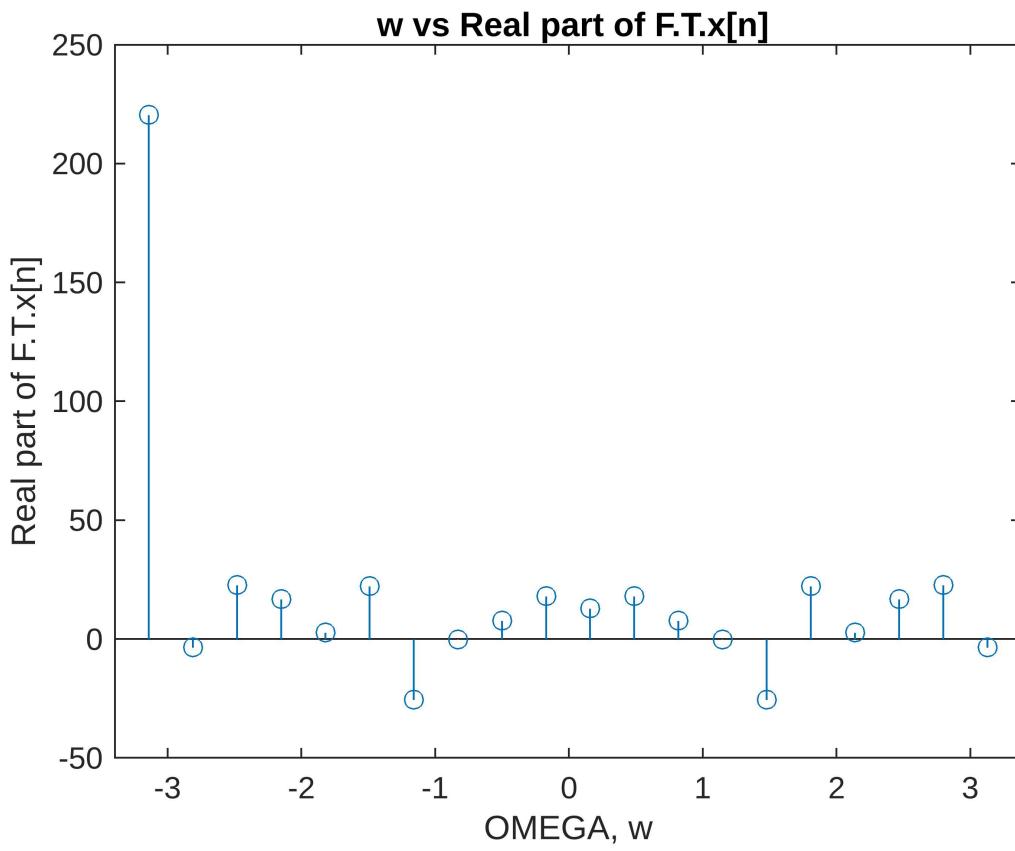
```

display("Different examples");

"Different examples"

x_n = 20.*rand(1,N);
xf_n = fft(x_n);
w = -pi:0.33:pi;
stem(w,real(xf_n));
xlabel("OMEGA, w");
ylabel("Real part of F.T.{x[n]}");
title(" w vs Real part of F.T.{x[n]}")

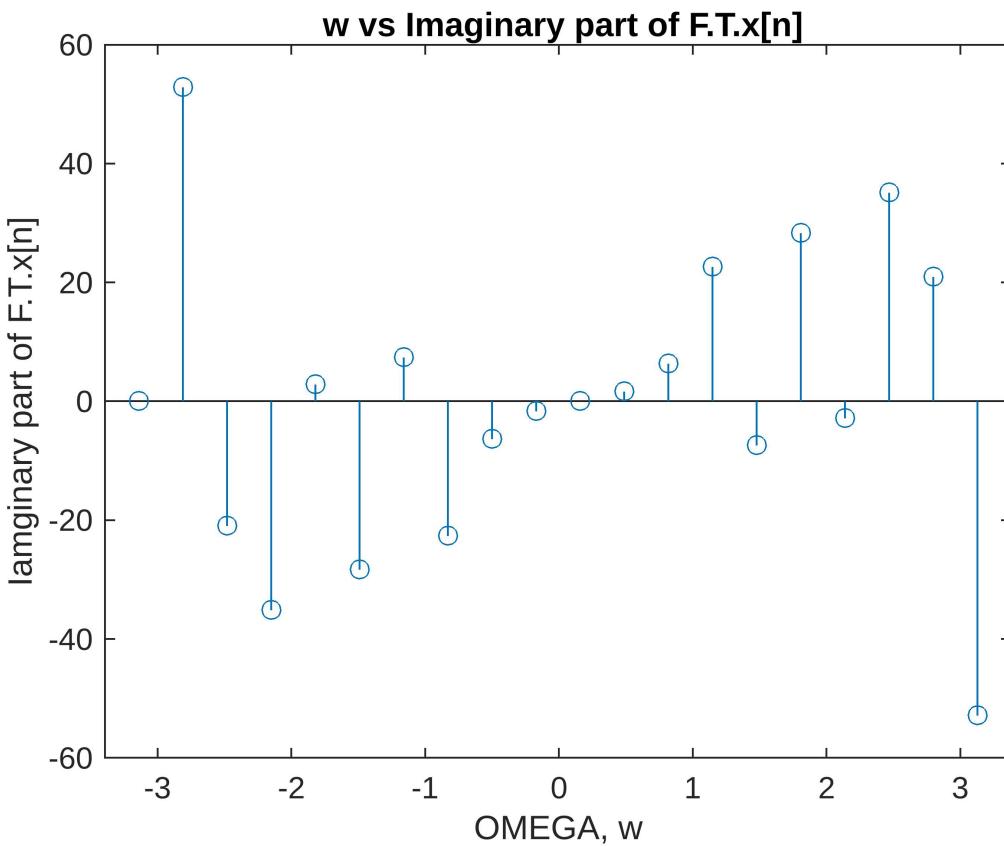
```



```

stem(w,imag(xf_n));
xlabel("OMEGA, w");
ylabel("Imaginary part of F.T.{x[n]}");
title(" w vs Imaginary part of F.T.{x[n]}");

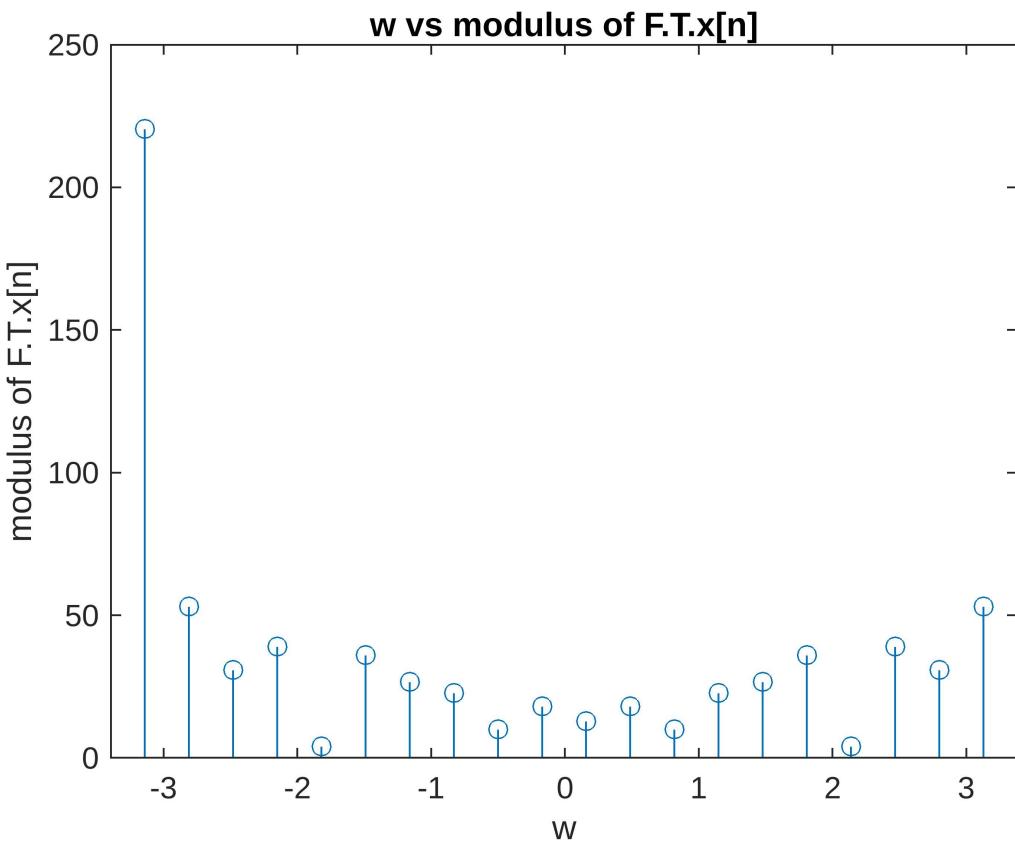
```



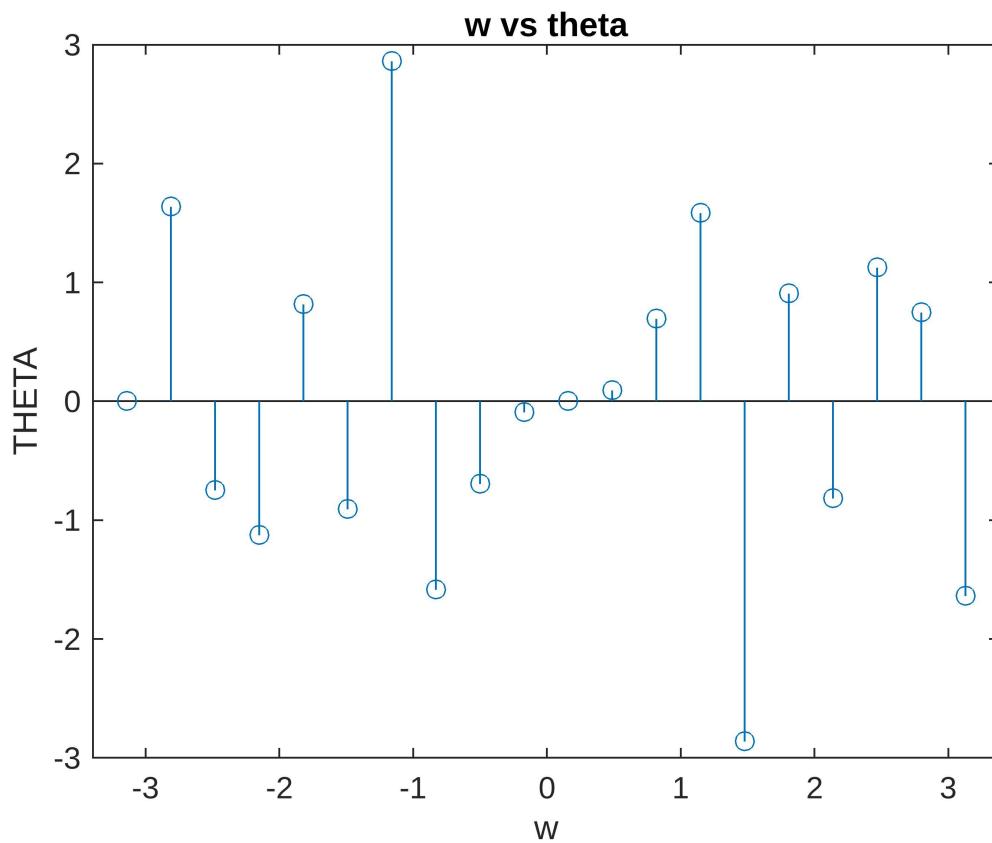
```

mod_xf = abs(xf_n);
stem(w,mod_xf);
xlabel("w");
ylabel("modulus of F.T.{x[n]}");
title("w vs modulus of F.T.{x[n]}");

```



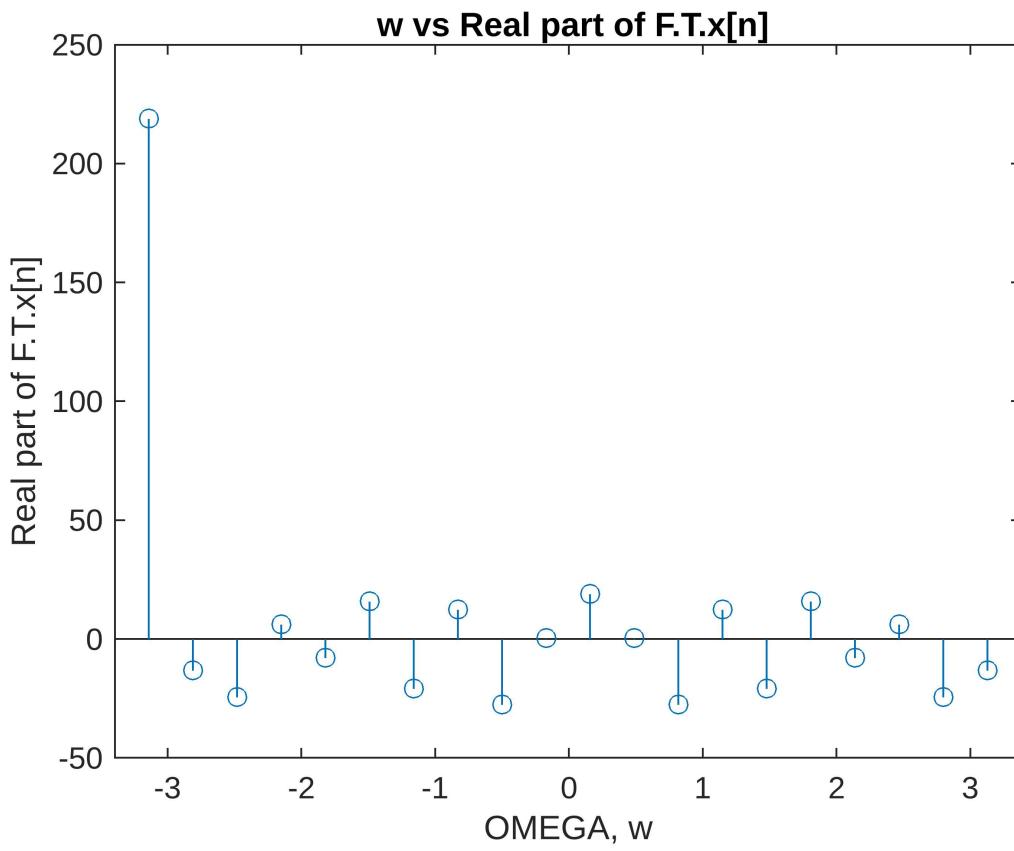
```
theta = angle(xf_n);
stem(w,theta);
xlabel("w");
ylabel("THETA");
title("w vs theta");
```



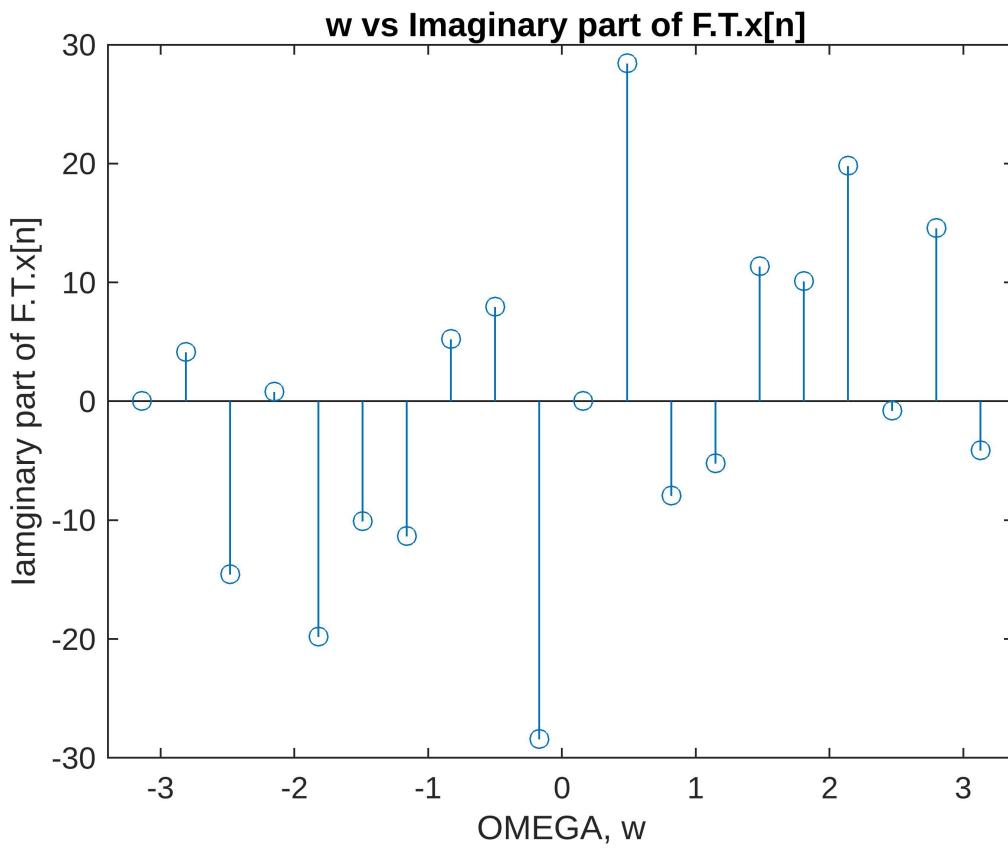
```
display("Example 2");
```

```
"Example 2"

x_n = 20.*rand(1,N);
xf_n = fft(x_n);
w = -pi:0.33:pi;
stem(w,real(xf_n));
xlabel("OMEGA, w");
ylabel("Real part of F.T.{x[n]}");
title(" w vs Real part of F.T.{x[n]}")
```



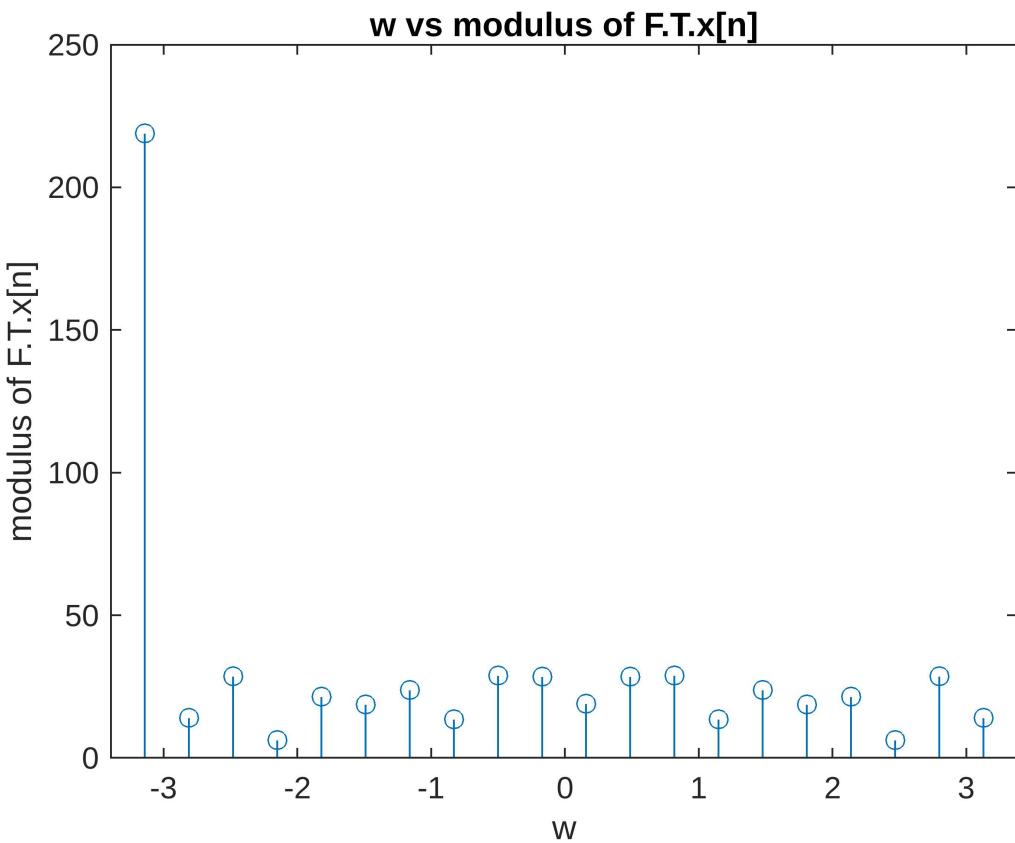
```
stem(w,imag(xf_n));
xlabel("OMEGA, w");
ylabel("Imaginary part of F.T.{x[n]}");
title(" w vs Imaginary part of F.T.{x[n]}");
```



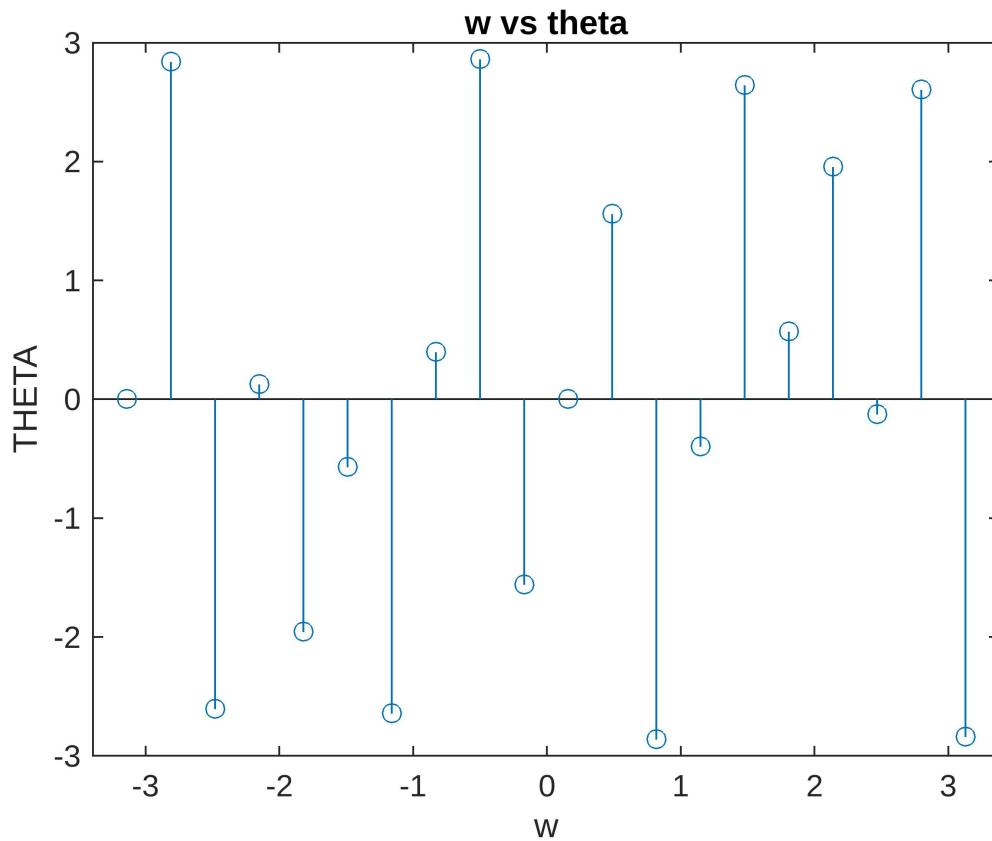
```

mod_xf = abs(xf_n);
stem(w,mod_xf);
xlabel("w");
ylabel("modulus of F.T.{x[n]}");
title("w vs modulus of F.T.{x[n]}");

```



```
theta = angle(xf_n);
stem(w,theta);
xlabel("w");
ylabel("THETA");
title("w vs theta");
```



E. FOURIER TRANSFORM OF EVEN OR ODD SIGNALS.

1. Generate a random signal $x[n]$, $0 \leq n \leq N$.
2. Compute the fourier transform of $x[n]$: $X[e^{j\omega n}] = \sum(x[n] * e^{-j\omega n})$ $n = N1$ to $N2$ for $\omega = -\pi$ to π .
3. Obtain even part of $X[n]$ i.e. $X_e[n]$.
4. Find F.T. of $X_e[n]$.
5. Plot and compare F.T.($X_e[n]$) and $\text{Re}(X(e^{j\omega}))$.
6. Similarly obtain odd part i.e. $X_o[n]$.
7. Find F.T.($X_o[n]$).
8. Plot and compare F.T.($X_o[n]$) and $\text{Im}(X(e^{j\omega}))$.

Question 1

```
N = 7;
x_n = 7.*rand(1,N);
```

Question 2

```
xf_n = fft(x_n);
```

Question 3

```
x_nn = fliplr(x_n);
Xe_n = (x_n + x_nn)./2;
```

Question 4

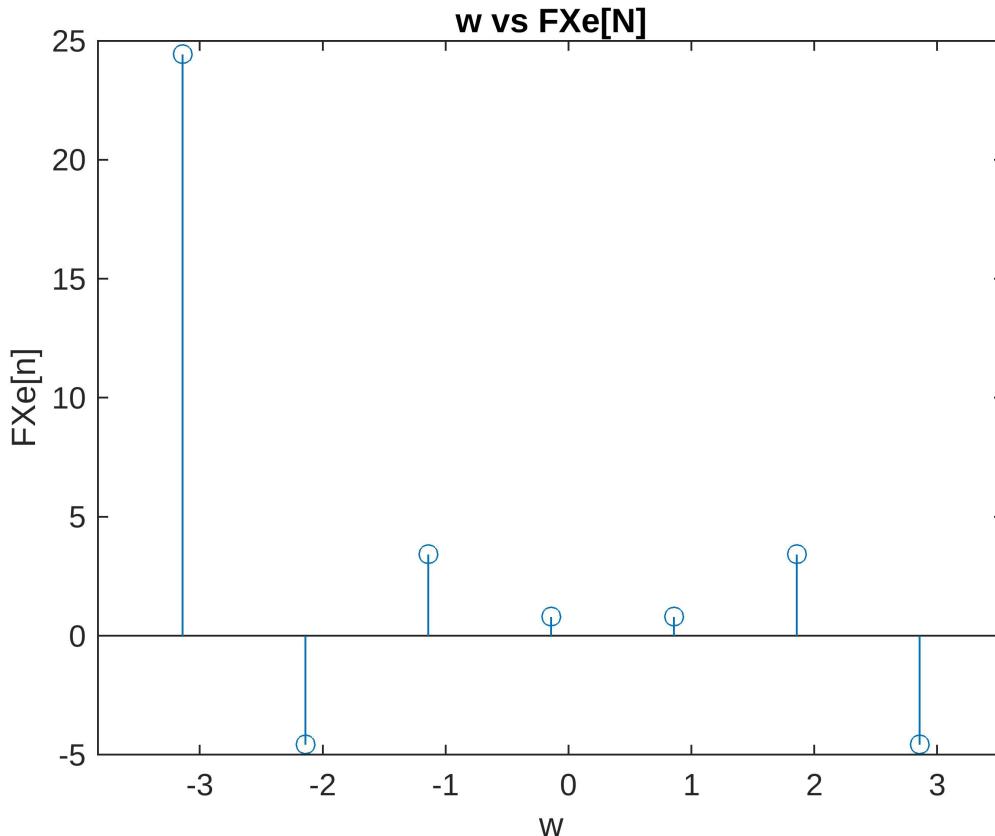
```
Xe_ft = fft(Xe_n);
```

Question 5

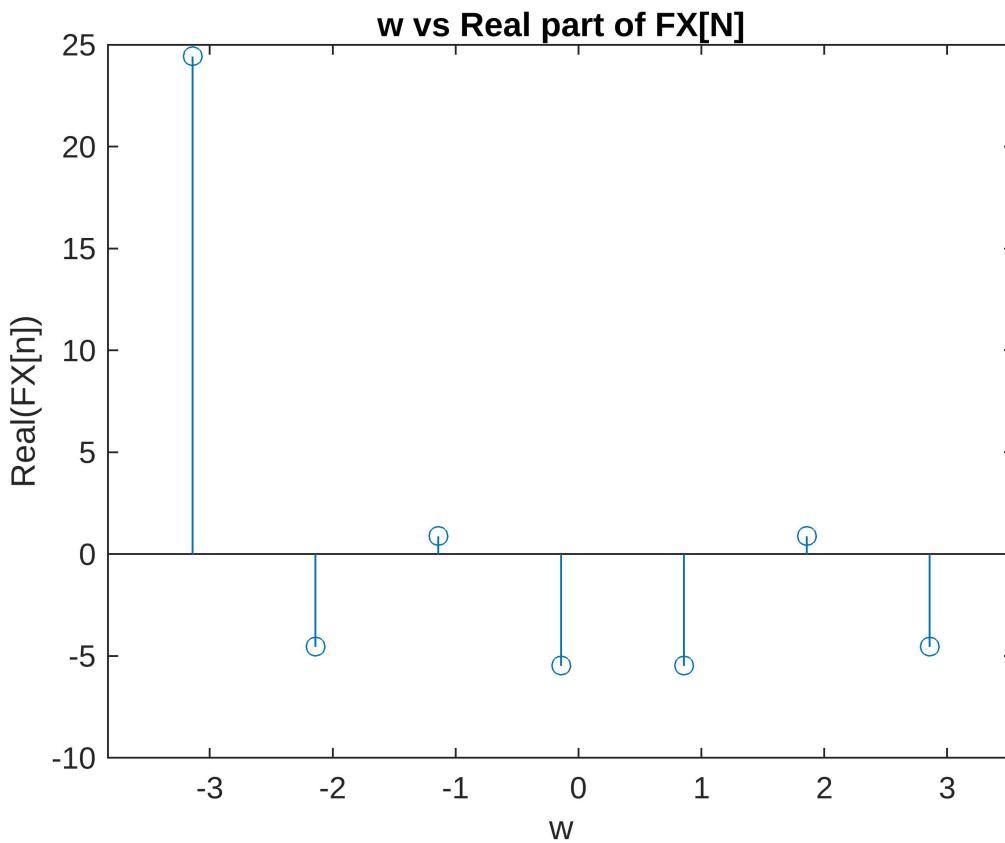
```
w = -pi:1:pi;
stem(w,Xe_ft);
```

Warning: Using only the real component of complex data.

```
xlabel("w");
ylabel("F{Xe[n]}");
title("w vs F{Xe[N]}");
```



```
stem(w,real(xf_n));
xlabel("w");
ylabel("Real(F{X[n]})");
title("w vs Real part of F{X[N]}");
```



Question 6

```
Xo_n = (x_n - x_nn)./2;
```

Question 7

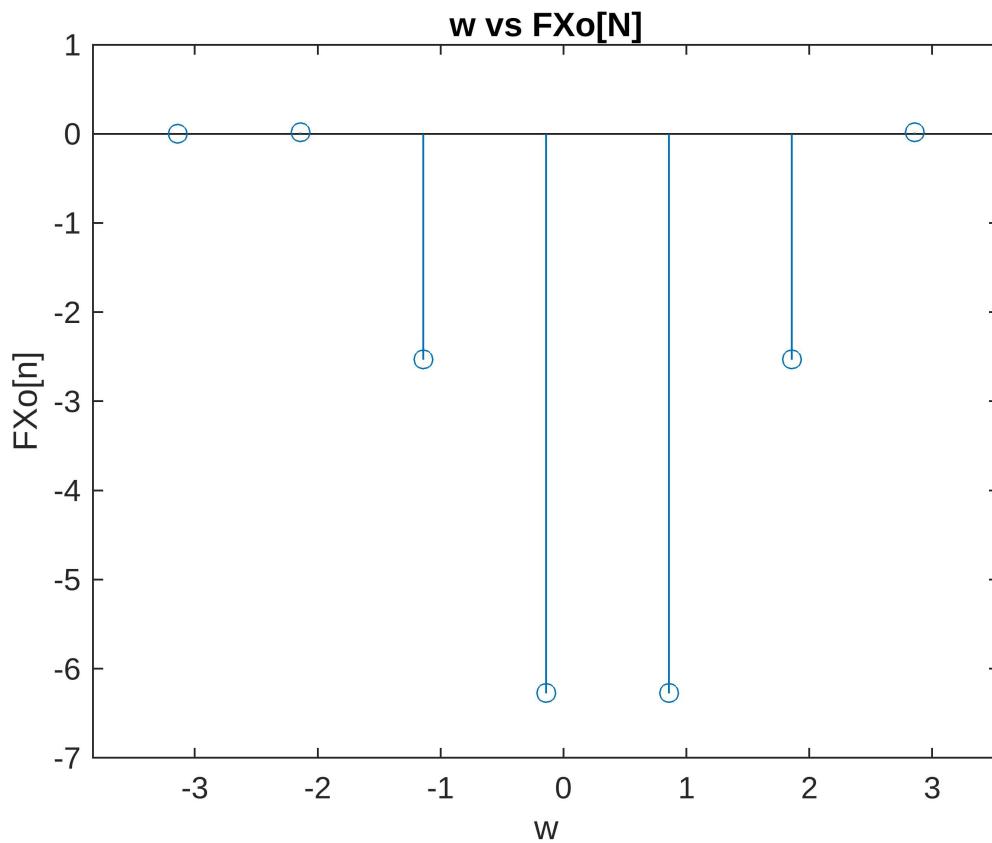
```
Xo_ft = fft(Xo_n);
```

Question 8

```
stem(w,Xo_ft);
```

Warning: Using only the real component of complex data.

```
xlabel("w");
ylabel("F{Xo[n]}");
title("w vs F{Xo[N]}");
```



```
stem(w, imag(xf_n));
xlabel("w");
ylabel("Imag(F{X[n]})");
title("w vs Imaginary part of F{X[N]}");
```

