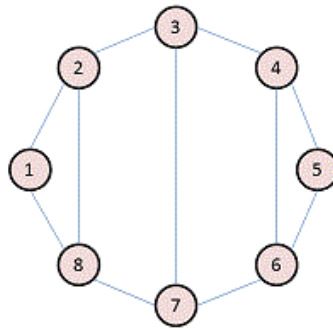


# Communities

Question 1:

For the following graph:



Write the adjacency matrix  $A$ , the degree matrix  $D$ , and the Laplacian matrix  $L$ . For each, find the sum of all entries and the number of nonzero entries.

Adjacent Matrix:

	1	2	3	4	5	6	7	8
1	0	1	0	0	0	0	0	1
2	1	0	1	0	0	0	0	1
3	0	1	0	1	0	0	1	0
4	0	0	1	0	1	1	0	0
5	0	0	0	1	1	0	0	0
6	0	0	0	1	1	0	1	0
7	0	0	1	0	0	1	0	1
8	1	1	0	0	0	0	1	0

Number of non-zero entries = 22, Sum of all elements = 22

Degree Matrix:

	1	2	3	4	5	6	7	8
1	2	0	0	0	0	0	0	0

2	0	3	0	0	0	0	0	0
3	0	0	3	0	0	0	0	0
4	0	0	0	3	0	0	0	0
5	0	0	0	0	2	0	0	0
6	0	0	0	0	0	3	0	0
7	0	0	0	0	0	0	3	0
8	0	0	0	0	0	0	0	3

Number of non- zero entries = 8, Sum of all entries = 8

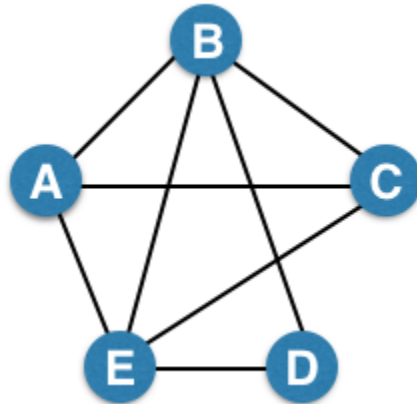
Laplacian Matrix ( $L = D - A$ )

	1	2	3	4	5	6	7	8
1	2	-1	0	0	0	0	0	-1
2	-1	3	-1	0	0	0	0	-1
3	0	-1	3	-1	0	0	-1	0
4	0	0	-1	3	-1	-1	0	0
5	0	0	0	-1	2	-1	0	0
6	0	0	0	-1	-1	3	-1	0
7	0	0	-1	0	0	-1	3	-1
8	-1	-1	0	0	0	0	-1	3

Number of non-zero entries = 30, Sum of all entries = 0

**Question 2:**

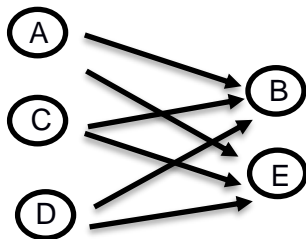
Consider the following undirected graph (i.e., edges may be considered bidirectional):



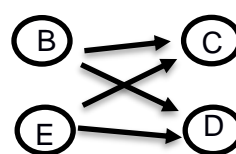
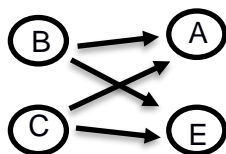
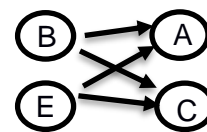
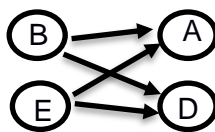
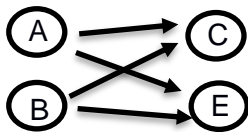
Run the "trawling" algorithm for finding dense communities on this graph and find all complete bipartite subgraphs of types  $K_{3,2}$  and  $K_{2,2}$ . Note: In the case of  $K_{2,2}$ , we consider  $\{\{W, X\}, \{Y, Z\}\}$  and  $\{\{Y, Z\}, \{W, X\}\}$  to be identical.

From the given graph  $A = \{B, C, E\}$ ;  $B = \{A, C, D, E\}$ ;  $C = \{A, B, E\}$ ;  $D = \{B, E\}$ ;  $E = \{A, B, C, D\}$

So, B and E have support more than 3 Therefore, Bipartite subgraph of  $K_{3,2}$

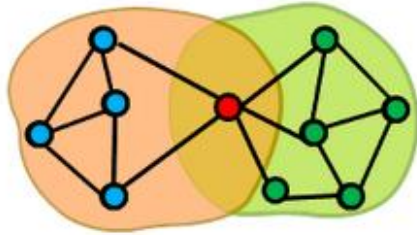


Bipartite subgraph of  $K_{2,2}$

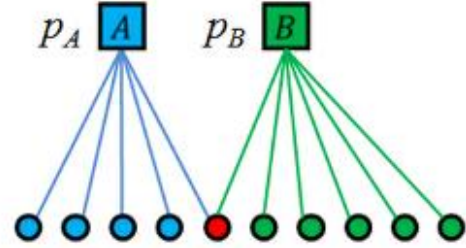


**Question 3:**

We fit AGM to the network on the left, and found the parameters on the right:



Network



Learned AGM parameters

**Find the optimal values for  $p_A$  and  $p_B$ .**

a)  $P_a = \frac{\text{No. of edges in the network}}{\text{Total possible no. of edges}} = \frac{7}{\frac{5}{2}c} = \frac{7}{10} = 0.7$

b)  $P_b = \frac{\text{No. of edges in the network}}{\text{Total possible no. of edges}} = \frac{9}{\frac{6}{2}c} = \frac{9}{15} = 0.6$