3

2

2

### **FACULTY OF ENGINEERING**

## B.E. 3/4 (CSE) I – Semester (Main) Examination, November 2013

**Subject: Automata Languages and Computation** 

Time: 3 hours Max. Marks: 75

Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.

## PART – A (25 Marks)

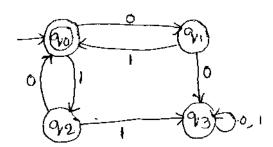
- 1. Obtain a DFA to accept strings of 0's, is and 2's beginning with a '0' followed by odd no. of 1's and ending with a '2'.
- 2. Obtain a regular expression to accept strings of a's and b's whose length is either even or multiples of 3 or both.
- 3. If  $\Sigma = \{0,1\}$ ,  $\Gamma = \{1,2,3\}$ , h(0) = 3122, h(1) = 1322 What is (0+1)\* (00)\*?
- 4. Consider the following grammar 3
  - S → aCa
  - C → aCalb

What is the language generated by this grammar?

- 5. Define Chomsky Normal Form (CNF).
- 6. Prove that reversal of a CFL is also an CFL. 3
- 7. What do you understand by the term LBA? 3
- 8. Define turning machine. How a TM accepts a language? 3
- 9. Define MPCP. 2
- 2 10. What is universal language?

#### **PART – B** (50 Marks)

- 11.a) Construct a DFA to accept decimal strings divisible by 3. 5 5
  - b) Convert the FA to regular expression.



- 12.a) Prove that  $(00^*1)^*1 = 1 + 0(0 + 10)^*11$ .
  - b) State and prove pumping lemma for CFL.

5 5 13. Obtain a TM to accept a palindrome consisting of a's and b's of any length.

14.a) Convert the following grammar into GNF.

5

$$A \rightarrow BC$$
  $B \rightarrow CA/b$   $C \rightarrow AB/a$ 

b) Obtain a CFG for the following PDA.

5

$$\delta(q_0, a, z) = (q_0, AZ), \qquad \delta(q_0, a, A) = (q_0, A)$$

$$\delta(q_0, b, A) = (q_1, \in) , \quad \delta(q_1, \in, z) = (q_2, \in)$$

15.a) Prove that PCP is undecidable.

5

b) State PCP and find whether given instances of PCP has solution or not.

5

|   | List A | List B |
|---|--------|--------|
| 1 | 10     | 101    |
| 2 | 011    | 11     |
| 3 | 101    | 011    |

16.a) Obtain a TM to multiply two unary no's separated by the delimiter '1'.

b) Consider the CFG  $S \rightarrow A_1A_2|A_2 A_3$ ,  $A1 \rightarrow A_2A_1|0$ 

4

$$A_2 \to \, A_3 A_3 | 1, \;\; A_3 \to \, A_1 A_2 | 0$$

Test 10010 is a member or not using CYK algorithm

17. Minimize the following DFA:

10

|     | 0 | 1 |
|-----|---|---|
| → A | В | Α |
| В   | Α | С |
| С   | D | В |
| * D | D | Α |
| E   | D | F |
| F   | D | Е |
| G   | F | G |
| Н   | G | D |

\*\*\*\*

Max. Marks: 75

# **FACULTY OF ENGINEERING**

# B.E. 3/4 (CSE) I-Semester (Suppl.) Examination, July 2014

**Subject : Automata Languages and Computation** 

Note: Answer all questions of Part - A and answer any five questions from Part-B.

PART – A (25 Marks)

Time: 3 Hours

| 1<br>2<br>3<br>1<br>1<br>5<br>7<br>3<br>3<br>9 | Define $\delta$ in a TM. State pumping lemma for CFL's. Define Church's hypothesis. Define the term LBA and explain. Prove that $(O+1)^*$ 100 regular or not. State the closure properties of Regular Languages. Define PCP and MPCP. Construct a right linear grammar for $(0+1)^*$ 00(0+1)*. Convert to CNF. $S \rightarrow aB \mid bA$ $A \rightarrow a \mid aS \mid bAA$ $B \rightarrow b \mid bS \mid aBB$ What are intractable problem ? Explain. | (2)<br>(2)<br>(2)<br>(3)<br>(2)<br>(2)<br>(3)<br>(3) |
|--|---|--|
|  | PART – B (50 Marks)   |  |
| 11   | <ul><li>(a) Construct a DFA equivalent to the regular expression 10+(0+11)0*1.</li><li>(b) Differentiate between NFA and DFA.</li></ul>   | (6)<br>(4)   |
| 12   | <ul> <li>(a) Given CFG G = ({S, A}, {a, b}, P, S) where P consists of S → aAS   a</li></ul>   | (5)<br>(5)   |
| 13   | Design a PDA to accept equal no of a's and b's over the alphabet (a+b) <sup>+</sup> .   | (10)   |
| 14   | <ul> <li>(a) Write short notes on Universal TM .</li> <li>(b) Design a TM for L {WW<sup>R</sup>   W ∈ (0+1)*, R stands for Reverse}.</li> </ul>   | (5)<br>(5)   |
| 15   | Reduce to GNF $S \rightarrow AA \mid O$ $A \rightarrow SS \mid 1$   | (10)   |
| 16   | <ul><li>(a) Define Chomsky hierarchy.</li><li>(b) What are recursively enumerable languages? Give example.</li><li>(c) Explain undecidability.</li></ul>  | (3)<br>(3)<br>(4)                                    |
| 17   | <ul><li>(a) Explain a restricted satisfiability problem.</li><li>(b) Explain the classes of P, NP and explain the terms NP - complete and NP-nard.</li></ul>  | (5)<br>(5)   |

\*\*\*\*