

# Transportation

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```
library(lpSolve)
```

```
# Solve the transportation Problem in R and formulate it.
```

```
# use Dataframe
```

```
transport = matrix(c(22,14,30,600,100,
```

```
16,20,24,625,120,
```

```
80,60,70,"-","-"),ncol=5,byrow=TRUE)
```

```
colnames(transport)=c("Warehouse-1","Warehouse-2","Warehouse-3","Production cost","Production capacity")
```

```
rownames(transport)=c("Plant-A","Plant-B","Demand")
```

```
transport
```

```
##           Warehouse-1 Warehouse-2 Warehouse-3 Production cost Production capacity
```

```
## Plant-A  "22"         "14"         "30"         "600"         "100"
```

```
## Plant-B  "16"         "20"         "24"         "625"         "120"
```

```
## Demand   "80"         "60"         "70"         "-"          "-"
```

```
# THE Transportation model and the Objective Function solved below
```

```
# Minimization:: The combined cost of a production and shipping
```

```
# Min TM = 22x11 + 14x12 + 30x13+ 16x21 + 20x22+ 24x23
```

```
# which is Subjected to supply constraints:
```

```
# x11 + x12 + x13 <= 100 (Plant-A)
```

```
# x21 + x22 + x23 >= 120 (Plant-B)
```

```
# Demand Constraints
```

```
# x11 + x21 >= 80 (Warehouse-1)
```

```
# x12 + x22 >= 60 (Warehouse-2)
```

```
# x13 + x23 >= 70 (Warehouse-3)
```

```
# Seems to be the transportation problem is unbalanced because demand < supply by 10.
```

```
# Use dummy variable method column 4 with the transportation cost = 0 and demand = 10.
```

```
# Transportation problem in R
```

```
tp <- matrix(c(622,614,630,0,
```

```
641,645,649,0), ncol = 4, byrow = TRUE)
```

```
# Column names, row names
```

```
colnames(tp) <- c("Warehouse-1", "Warehouse-2", "Warehouse-3", "Dummy")
```

```
row.names(tp) <- c("Plant-A", "Plant-B")
```

```
tp <- as.table(tp)
```

```
tp
```

```
##           Warehouse-1 Warehouse-2 Warehouse-3 Dummy
```

```
## Plant-A           622           614           630      0
```

```
## Plant-B           641           645           649      0
```

```

# Production Capacity set row :
# supply end
rowsign <- rep("<=", 2)
rowrhs <- c(100,120)

# demand end
colsign <- rep(">=", 4)
colrhs <- c(80,60,70,10)

# LP Transport to find min.cost
lpt <- lp.transport(tp, "min", rowsign, rowrhs, colsign, colrhs)

# solution
lpt$solution

```

```

##      [,1] [,2] [,3] [,4]
## [1,]    0   60   40    0
## [2,]   80    0   30   10

```

```

# objective function
lpt$objval

```

```

## [1] 132790

```

```

# Objective function is 132790
# Plant A they should ship 40 to Warehouse 1 and 60 units to Warehouse 2, from Plant B they should ship 80 to Warehouse 1 and 30 units to Warehouse 2.

# The dual
lpt$duals

```

```

##      [,1] [,2] [,3] [,4]
## [1,]    0    0    0    0
## [2,]    0    0    0    0

```

```

# Dual is the shadow prices of primal.

```

```

# 3. Make an economic interpretation of the dual
# Warehouse-1 <= 622 + Plant-A
# Warehouse-2 <= 614 + Plant-A
# Warehouse-3 <= 630 + Plant-A
# Warehouse-1 <= 641 + PlantB
# Warehouse-2 <= 645 + PlantB
# Warehouse-3 <= 649 + PlantB

```

```

#We conclude that Warehouse-1 - Plant-A >= 622$$ that can be exponented as arehouse-1 <= 622 + Plant-A
# Warehouse-1 is considered as the price payments being received at the origin which is nothing
# Therefore the equation turns, out to be MarketRevenue >= MarginalCost_1

```

```

# For a profit maximization, The Marginal Revenue (MR) should be equal to Marginal Costs MR_1 = M

```

*#Based on above interpretation, we can conclude that, Profit maximization takes place if MC is equal*

*# If  $MR < MC$ , We must lower plant costs in order to reach the Marginal Revenue (MR)*

*#If  $MR > MC$ , We must boost manufacturing supply if we are to reach the Marginal Revenue (MR)*

*4.# Conclusion from the primal*

**## [1] 4**

*# 60x12 which is 60 Units from Plant A to Warehouse 2.*

*# 40x13 which is 40 Units from Plant A to Warehouse 3.*

*# 80x21 which is 60 Units from Plant B to Warehouse 1.*

*# 30x23 which is 60 Units from Plant B to Warehouse 3.*

*# from the dual*

*# So,  $MR=MC$ . Five of the six  $MR \leq MC$ . The only equation that does not satisfy this requirement is Plant A to Warehouse 2.*

*# Warehouse 2.*

*#The primal that we will not be shipping any AED device there*