

Problem 1 within project 1

September 1, 2022

We are interested in the solution for

$$-\frac{d^2u}{dx^2} = 100e^{-10x}$$

It is claimed that $u(x) = 1 - (1 - e^{-10})x - e^{-10x}$ is a solution. Inserting this into the lefthand side of the original expression will show that this is indeed a solution if both sides of the equation still match:

$$\begin{aligned} & -\frac{d^2}{dx^2} (1 - (1 - e^{-10})x - e^{-10x}) \\ &= -(-100e^{-10x}) = 100e^{-10x} \end{aligned}$$

As such, we've shown that $u(x) = 1 - (1 - e^{-10})x - e^{-10x}$ is an exact solution.