ProgAsDataAs4

Mads Ljungberg

September 2021

1 4.1

Compiling and loading the micro-ML evaluator and parser (Fun/README.TXT) Archive fun1.zip (lecture 3) contains the files used in points A-C below, and archive fun2.zip (lecture 4) contains additional files used in points D-F. A. Loading the micro-ML evaluator, with abstract syntax only fsharpi Absyn.fs Fun.fs open Absyn;; open Fun;; let res = run (Prim("+", CstI 5, CstI 7));;#q;; D:\GitHubRepoes\BPRD\Assignment4\Fun>fsi Absyn.fs Fun.fs Microsoft (R) F# Interactive version 12.0.30815.0 Copyright (c) Microsoft Corporation. All Rights Reserved. For help type #help;; $[Loading D: \ GitHubRepoes \ BPRD \ Assignment 4 \ Fun \ Absyn. fs$ Loading D:\GitHubRepoes\BPRD\Assignment4\Fun\Fun. fs]namespace FSI_0002 type expr =| CstI of int CstB of bool | Var of string Let of string * expr * expr

| Prim of string * expr * expr

```
namespace FSI_0002
            type 'v_env_=_(string_*_'v) list
            val lookup : env:(string * 'a)_list -> x:string -> 'a
            type value =
                   | Int of int
                   Closure of string * string * Absyn.expr * value env
            \verb|val| eval| : e: Absyn. expr| -\!\!\!> env: \verb|value| env| -\!\!\!> int|
            val run : e:Absyn.expr -> int
            val ex1 : Absyn.expr
            val ex2 : Absyn.expr
            val ex3 : Absyn.expr
            val rundeep : n:int \rightarrow int
            val ex4 : Absyn.expr
            val ex5 : Absyn.expr
         > open Absyn;;
         > open Fun;;
         > let res = run (Prim("+", CstI 5, CstI 7));;
         val res : int = 12
         > #q;;
         D: \ BPRD \ Assignment 4 \ Fun>
B. Generating and compiling the lexer and parser, and loading them:
   fsyacc — module FunPar FunPar.fsy
   fslex —unicode FunLex.fsl
    fsharpi -r ~/fsharp/FsLexYacc.Runtime.dll Absyn.fs FunPar.fs FunLex.fs Parse.fs
// fsharpi should for me be fsi
   open Parse;;
   let e1 = fromString "5+7";;
   \label{eq:constring} \mbox{let $=$} 2 = \mbox{fromString "let $\_$} y = 7 \mbox{lin $\_$} y + 2 \mbox{lend"};;
   let e3 = fromString "let _{\perp}f_{\perp}x_{\perp}=_{\perp}x_{\perp}+_{\perp}7_{\perp}in_{\perp}f_{\perp}2_{\perp}end";;
         D:\GitHubRepoes\BPRD\Assignment4\Fun>bin\fsyacc —module FunPar FunPar.fsy
         building tables
         computing first function...time: 00:00:00.0871566
         building kernels...time: 00:00:00.0576248
```

| If of expr * expr * expr

| Call of expr * expr

Letfun of string * string * expr * expr

```
building kernel table...time: 00:00:00.0146807
computing lookahead relations ......
\dots \dots \dots  time: 00:00:00.0460465
building lookahead table...time: 00:00:00.0153142
building action table ... state 21: shift/reduce error on GT
state 21: shift/reduce error on LT
state 21: shift/reduce error on GE
state 21: shift/reduce error on LE
state 22: shift/reduce error on GT
state 22: shift/reduce error on LT
state 22: shift/reduce error on GE
state 22: shift/reduce error on LE
state 23: shift/reduce error on GT
state 23: shift/reduce error on LT
state 23: shift/reduce error on GE
state 23: shift/reduce error on LE
state 24: shift/reduce error on GT
state 24: shift/reduce error on LT
state 24: shift/reduce error on GE
state 24: shift/reduce error on LE
time: 00:00:00.0610508
building goto table ... time: 00:00:00.0018371
returning tables.
16 shift/reduce conflicts
58 states
6 nonterminals
29 terminals
26 productions
#rows in action table: 58
D:\GitHubRepoes\BPRD\Assignment4\Fun>bin\fslex —unicode FunLex.fsl
compiling to dfas (can take a while...)
30 states
writing output
D:\GitHubRepoes\BPRD\Assignment4\Fun>fsi -r bin\FsLexYacc.Runtime.dll Absyn.fs
FunPar.fs FunLex.fs Parse.fs
Microsoft (R) F# Interactive version 12.0.30815.0
Copyright (c) Microsoft Corporation. All Rights Reserved.
For help type #help;;
[Loading D:\GitHubRepoes\BPRD\Assignment4\Fun\Absyn.fs]
 Loading D:\GitHubRepoes\BPRD\Assignment4\Fun\FunPar.fs
 Loading \ D: \ \ GitHubRepoes \ \ \ BPRD \ \ Assignment \ \ \ \ \ Fun \ \ \ Fun Lex. \ fs
```

 $Loading \ D: \ \ BPRD \ \ Assignment 4 \ \ Fun \ \ Parse. \ fs \]$

```
name space \ FSI\_0002
  type expr =
        | CstI of int
          CstB of bool
          Var of string
          Let of string * expr * expr
            Prim \ of \ string \ * \ expr \ * \ expr \\
          If of expr * expr * expr
           Letfun of string * string * expr * expr
          Call of expr * expr
name space \ FSI\_0002
  type token =
          EOF
          LPAR
          RPAR
          EQ
          NE
          GT
          LT
          \times
          LE
          PLUS
          MINUS
          TIMES
          DIV
          MOD
          ELSE
          END
          FALSE
           _{\mathrm{IF}}
          IN
          LET
          NOT
          THEN
          TRUE
          CSTBOOL of bool
          NAME of string
         CSTINT of int
  type tokenId =
          TOKEN_EOF
          TOKENLPAR
          TOKEN_RPAR
          TOKEN_EQ
          TOKEN_NE
          TOKEN_GT
          TOKEN_LT
```

```
TOKEN_GE
       TOKENLE
       TOKEN_PLUS
       TOKEN_MINUS
       TOKEN_TIMES
       TOKEN_DIV
       TOKENMOD
       TOKEN_ELSE
       TOKEN_END
       TOKEN_FALSE
       TOKEN_IF
       TOKEN_IN
       TOKENLET
       TOKEN NOT
       TOKEN_THEN
       TOKEN_TRUE
       TOKEN_CSTBOOL
       TOKEN_NAME
       TOKEN_CSTINT
       TOKEN_end_of_input
       TOKEN\_error
type nonTerminalId =
       NONTERM\_startMain
       NONTERM_Main
       NONTERM_Expr
       NONTERM_AtExpr
       NONTERM_AppExpr
       NONTERM_Const
val tagOfToken : t:token -> int
val tokenTagToTokenId : tokenIdx:int -> tokenId
val prodIdxToNonTerminal : prodIdx:int -> nonTerminalId
val _fsyacc_endOfInputTag : int
val _fsyacc_tagOfErrorTerminal : int
val token_to_string : t:token -> string
val _fsyacc_dataOfToken : t:token -> System.Object
val _fsyacc_gotos : uint16 []
val _fsyacc_sparseGotoTableRowOffsets : uint16 []
val _fsyacc_stateToProdIdxsTableElements : uint16 []
val _fsyacc_stateToProdIdxsTableRowOffsets : uint16 []
val _fsyacc_action_rows : int
val _fsyacc_actionTableElements : uint16 []
val _fsyacc_actionTableRowOffsets : uint16
val _fsyacc_reductionSymbolCounts : uint16 []
val _fsyacc_productionToNonTerminalTable : uint16 []
val _fsyacc_immediateActions : uint16 []
val _fsyacc_reductions : unit -> (Text.Parsing.IParseState -> obj) []
val tables : unit -> Text.Parsing.Tables<token>
val engine:
```

```
lexer: (Text. Lexing. LexBuffer<'a>_->_token)_->
 ____lexbuf:Text.Lexing.LexBuffer<'a> -> startState:int -> obj
                                val Main:
                                                     lexer: (Text. Lexing. LexBuffer<'a>_->_token)_->
   ____lexbuf: Text. Lexing. LexBuffer<'a> -> Absyn.expr
                          namespace FSI_0002
                                 val lexemeAsString : lexbuf:Text.Lexing.LexBuffer<char> -> string
                                 val commentStart : Text.Lexing.Position ref
                                 val commentDepth : int ref
                                 val keyword : s:string -> FunPar.token
                                 val trans : uint16 [] array
                                 val actions : uint16 []
                                 val _fslex_tables : Text.Lexing.UnicodeTables
                                 val _fslex_dummy : unit -> 'a
___val_Token_: _lexbuf: Text. Lexing. LexBuffer <char>_->_FunPar. token
___val_SkipComment_:_lexbuf:Text.Lexing.LexBuffer<char>_->_unit
____val__fslex_Token_:
\verb| LexBuffer < char > \_ - State: int \_ - > \_ lexbuf: Text. Lexing. LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - > \_ - = \_ - > \_ FunPar. to kend | LexBuffer < char > \_ - - > \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ - = \_ -
 ____val__fslex_SkipComment_:
____fslex_state:int_->_lexbuf:Text.Lexing.LexBuffer<char>_->_unit
____namespace_FSI_0002
___val_fromString_:_str:string_->_Absyn.expr
___val_fromFile_:_filename:string_->_Absyn.expr
____val_e1_:_Absyn.expr
____val_e2_:_Absyn.expr
____val_ex1_:_Absyn.expr
___val_ex3_:_Absyn.expr
LLLLLLLvallex4::Absyn.expr
____val_ex5_:_Absyn.expr
---->-open_Parse;;
= - from String = 5 + 7;
___val_e1_: _Absyn.expr_=_Prim_("+", CstI_5, CstI_7)
= 1et_e2 =
 let _e3 = from String_" let _f_x = x_+ 7_i in_f_2 end";; 
alle3: Absyn.expr=
____Letfun_("f","x",Prim_("+",Var_"x",CstI_7),Call_(Var_"f",CstI_2))
```

```
C. Using the lexer, parser and first-order evaluator together:
___fsyacc_—module_FunPar_FunPar.fsy
___fslex_—unicode_FunLex.fsl
___fsharpi_-r_^/fsharp/FsLexYacc.Runtime.dll_Absyn.fs_FunPar.fs_FunLex.fs_Parse.fs_Fun
__open_ParseAndRun;;
--run-(fromString-"5+7");;
___run_(fromString_"let_y_=_7_in_y_+_2_end");;
==x_+=7_i in =f_2 end ");;
____building_tables
computing first function ... time: 00:00:00.0855374
____building_kernels...time:_00:00:00.0564305
\verb| uullding_kernel_table...time: 00:00:00.0147743|
____computing_lookahead_relations .....
_____time:_00:00:00.0449269
building lookahead table ... time: 00:00:00.0146503
____building_action_table...state_21:_shift/reduce_error_on_GT
____state_21:_shift/reduce_error_on_LT
state 21: shift/reduce error on GE
____state_21:_shift/reduce_error_on_LE
____state_22:_shift/reduce_error_on_GT
____state_22:_shift/reduce_error_on_LT
____state_22:_shift/reduce_error_on_GE
state_22:_shift/reduce_error_on_LE
state 23: shift/reduce error on GT
state 23: shift/reduce error on LT
state 23: shift/reduce error on GE
____state_23:_shift/reduce_error_on_LE
____state_24:_shift/reduce_error_on_GT
____state_24:_shift/reduce_error_on_LT
____state_24:_shift/reduce_error_on_GE
state_24:_shift/reduce_error_on_LE
log_{10} = log_{10} 
____building_goto_table ... time:_00:00:00.0016027
returning tables.
____16_shift/reduce_conflicts
_{\text{----}}58\_states
____6_nonterminals
____29_terminals
____26_productions
```

____#rows_in_action_table:_58

```
\verb| Luculu | D: \ GitHubRepoes \\ BPRD \ Assignment \\ 4 \ Fun > bin \ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ \verb| Luculu | micode \\ \verb| FunLex. \\ fslex \\ fsl
____compiling_to_dfas_(can_take_a_while...)
_{\text{----}}30\_states
____writing_output
____D:\GitHubRepoes\BPRD\Assignment4\Fun>fsi_-r_bin\FsLexYacc.Runtime.dll_Absyn.fs
____FunPar.fs_FunLex.fs_Parse.fs_Fun.fs_ParseAndRun.fs
____ Microsoft_(R)_F#_Interactive_version_12.0.30815.0
Copyright (c) Microsoft Corporation . All Rights Reserved.
\verb| Lucul For Lhelp type \# help;;
[Loading_D:\GitHubRepoes\BPRD\Assignment4\Fun\Absyn.fs
\verb| Loading_D: \land GitHubRepoes \land BPRD \land Assignment 4 \land Fun \land FunPar. fs \\
\verb| Loading_D: \land GitHubRepoes \land BPRD \land Assignment 4 \land Fun \land FunLex. fs | \\
\verb| Loading_D: \land GitHubRepoes \land BPRD \land Assignment 4 \land Fun \land Parse. fs \\
Loading D:\GitHubRepoes\BPRD\Assignment4\Fun\Fun. fs
____Loading_D:\GitHubRepoes\BPRD\Assignment4\Fun\ParseAndRun.fs]
____namespace_FSI_0002
___type_expr =
_____|_CstB_of_bool
Let_of_string_*_expr_*_expr
_____|_If_of_expr_*_expr_*expr
_____|_Letfun_of_string_*_string_*_expr_*_expr
_____|_Call_of_expr_*_expr
unamespace FSI_0002
____type_token =
LLLLLLLLL | LEOF
____| LPAR
LULLING LINE | LRPAR
____| _EQ
____| _NE
____| _GT
____| _LT
____| _GE
____| _LE
LLLLLLL LLLLLL | LPLUS
LLLLLLLLLL | LMINUS
LILLINGS LILLINGS
____| _DIV
```

	LELSE
	LEND
	LFALSE
	LIF
	LIN
	LET
	LNOT
	_THEN _TRUE
	LCSTBOOL_of_bool
	NAME_of_string
	_CSTINT_of_int
type-to	
	LTOKEN LDAD
	LTOKENLPAR
	_TOKEN_RPAR
	_TOKEN_EQ
	LTOKEN NE
	_TOKEN_GT
	LTOKENLT
	_TOKEN_GE
	_TOKEN_LE
	_TOKEN_PLUS
	_TOKEN_MINUS
	_TOKEN_TIMES
	_TOKEN_DIV
	_TOKEN_MOD
	_TOKEN_ELSE
	_TOKEN_END
	_TOKEN_FALSE
	_TOKEN_IF
	_TOKEN_IN
	LTOKENLET
	_TOKEN_NOT
	_TOKEN_THEN
	_TOKEN_TRUE
	_TOKEN_CSTBOOL
	_TOKEN_end_of_input
= $=$ $=$ $=$ $=$ $=$ $=$ $=$ $=$ $=$	
	$ _NONTERM__startMain $
	_NONTERM_Main
	_NONTERM_Expr
	_NONTERM_AppExpr
	_NONTERM_Const

```
\_\_\_val\_tagOfToken\_:\_t:token\_->\_int
____val_tokenTagToTokenId_:_tokenIdx:int_->_tokenId
___val_prodIdxToNonTerminal_:_prodIdx:int_->_nonTerminalId
____val__fsyacc_endOfInputTag_:_int
___val__fsyacc_tagOfErrorTerminal_:_int
___val_token_to_string_: t:token_->_string
____val__fsyacc_dataOfToken_: _t:token__>_System.Object
____val__fsyacc_sparseGotoTableRowOffsets_:_uint16_[]
____val__fsyacc_stateToProdIdxsTableElements_:_uint16_[]
\verb| val_fsyacc_stateToProdIdxsTableRowOffsets_:= uint16\_[]|
\verb""" under under
uint16.[]
___val__fsyacc_actionTableRowOffsets_:_uint16_[]
____val__fsyacc_reductionSymbolCounts_:_uint16_[]
___val__fsyacc_productionToNonTerminalTable_:_uint16_[]
\_\_\_\_\_val\_\_fsyacc\_immediateActions\_:\_uint16\_[]
___val__fsyacc_reductions_:_unit_->_(Text.Parsing.IParseState_->_obj)_[]
____val_tables_:_unit_->_Text.Parsing.Tables<token>
___val_engine_:
lexbuf:Text.Lexing.LexBuffer<'a>_->_startState:int_->_obj
____val_Main_:
= Lexing . LexBuffer < 'a> -> token =
                                lexbuf: Text. Lexing. LexBuffer < 'a> _-> _Absyn.expr
____namespace_FSI_0002
___val_lexemeAsString_:_lexbuf:Text.Lexing.LexBuffer<char>_->_string
____val_commentStart_:_Text.Lexing.Position_ref
____val_commentDepth_:_int_ref
____val_keyword_: _s: string _->_FunPar.token
___val_trans_:_uint16_[]_array
___val_actions_:_uint16_[]
___val__fslex_tables_:_Text.Lexing.UnicodeTables
----val--fslex-dummy-:-unit-->-'a
                  val Token : lexbuf:Text.Lexing.LexBuffer<char> -> FunPar.token
                  val SkipComment : lexbuf:Text.Lexing.LexBuffer<char> -> unit
                  val _fslex_Token :
                             _fslex_state:int -> lexbuf:Text.Lexing.LexBuffer<char> -> FunPar.token
                  val _fslex_SkipComment :
                             _fslex_state:int -> lexbuf:Text.Lexing.LexBuffer<char> -> unit
              namespace FSI_0002
                  val from String : str:string -> Absyn.expr
                  val from File : filename:string -> Absyn.expr
```

val e1 : Absyn.expr

```
val e2 : Absyn.expr
         val ex1 : Absyn.expr
         val ex2 : Absyn.expr
         val ex3 : Absyn.expr
         val ex4 : Absyn.expr
         val ex5 : Absyn.expr
       namespace FSI_0002
         type 'v_env_=_(string_*_'v) list
         val lookup : env:(string * 'a)_list_->_x:string_->_'a
         type value =
               | Int of int
               Closure of string * string * Absyn.expr * value env
         val eval : e:Absyn.expr -> env:value env -> int
         val run : e:Absyn.expr -> int
         val ex1 : Absyn.expr
         val ex2 : Absyn.expr
         val ex3 : Absyn.expr
         val rundeep : n:int \rightarrow int
         val ex4 : Absyn.expr
         val ex5 : Absyn.expr
       namespace FSI_0002
         val from String : (string -> Absyn.expr)
         val eval : (Absyn.expr -> Fun.value Fun.env -> int)
         val run : e:Absyn.expr -> int
       > open ParseAndRun;;
       > run (fromString "5+7");;
       val it : int = 12
       > run (fromString "let_y = 7_in_y + 2_end");;
       val it : int = 9
       > run (fromString "let_f_x_=_x_+_7_in_f_2_end");;
       val it : int = 9
D. Loading the evaluator for a higher-order functional language (same
   abstract syntax as the first-order language):
   fsharpi Absyn.fs HigherFun.fs
   open HigherFun;;
   eval ex1 [];;
   open Absyn;;
```

```
Call (Call (Var "twice", Var "mul3"), CstI 2))));;
       #q;;
        (The above abstract syntax term corresponds to the concrete syntax
        term shown in point E below).
E. Using the lexer, parser and higher-order evaluator together:
        fsyacc — module FunPar FunPar.fsy
        fslex —unicode FunLex.fsl
        fsharpi -r ~/fsharp/FsLexYacc.Runtime.dll Absyn.fs FunPar.fs FunLex.fs Parse.fs Hig
        open ParseAndRunHigher;;
        run (from String @"let_twice_f_=_let_g_x_=_f(f(x))_in_g_end
 ___z*3_in_twice_mul3_2_end_end");;
       #q;;
F. Using the lexer, parser and polymorphic type inference together:
        fsyacc —module FunPar FunPar.fsy
        fslex —unicode FunLex.fsl
        fsharpi -r ~/fsharp/FsLexYacc.Runtime.dll Absyn.fs FunPar.fs FunLex.fs Parse.fs Typ
        open ParseAndType;;
        inferType (fromString "let_f_x_=_1_in_f_7_+_f_false_end");;
       #q;;
\mathbf{2}
         4.2
1) Summation of 1000 to 1...
> let sumt = run (from String "let _sum_n_=_ if _n_=_0 _then_n_ else _sum_ (n-1) _+_n_ in _sum_10
val~sumt~:~\mathbf{int}~=~500500
This wont do negative numbers.
2) Computing 3<sup>8</sup> in a naive way. with recursion.
> let facttt = run (fromString "let_fact_n_=_if_1_=_n_then_3_else_fact_(n-1)_*_3_in_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n_fact_n
val factt : int = 6561
Since the function only takes one argument 3 has to be hardcoded.
3)
> let sumfact = run (from String "let_fact_n_=_if_1_=_n_then_3_else_fact_(n-1)_*_3_in_l
val sumfact : int = 265720
4)
```

Letfun ("mul3", "z", Prim ("*", Var "z", CstI 3),

```
> let sum10fact8 = run (fromString "let_sum_a_=_if_0_<_a_then_let_pows_y_=_if_0_<_y_th
val sum10 fact8 : int = 167731334
3
    4.3
  //4.3
  | Letfun of string * string list * expr * expr (* (f, x, fBody, letBody) *)
  Call of expr * expr list
    //4.3 in Fun.fs
    | Letfun(f, x, fBody, letBody) ->
       let bodyEnv = (f, Closure(f, x, fBody, env)) :: env
       eval letBody bodyEnv
     | Call(Var f, eArg) ->
       let fClosure = lookup env f
       match fClosure with
       | Closure (f, x, fBody, fDeclEnv) \rightarrow
         (*let rec xValList args =
           match args with
           | [] -> failwith "_Empty_param"
           | e::rest -> Int(eval e env) :: xValList rest*)
         let values = List.map (fun e -> Int(eval e env)) eArg//xValList eArg
         let fBodyEnvZip = List.zip x values
         let fBodyEnv = fBodyEnvZip @ (f, fClosure) :: fDeclEnv
         eval fBody fBodyEnv
       _ -> failwith "eval_Call:_not_a_function"
4 4.4
//4.4 FunPar. fsy
MulArgs:
                                              \left\{ \begin{array}{c} \left\{ \begin{array}{c} \$1 \right\} \\ \$1 \end{array} \right. :: \ \$2 \quad \right\} 
    AtExpr
  | AtExpr MulArgs
AppExpr:
                                            { Call($1, $2)
    AtExpr MulArgs
                                                                     }
5
  4.5
  //4.5 FunLex. fsl
   "&&"
                      \{ AND \} // 4.5
  i "||"
                      { OR } // 4.5
```