

# Contention Management for 5G

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## Abstract

This article treats about Contention Management for 5G.

## 1 Introduction

- Context and problematic
- Related works
- Article contribution

## 2 Model, Problems

### 2.1 Definitions

We consider a symmetric directed graph  $G = (V, A)$  modelling a network. Each arc  $(u, v)$  in  $A$  is labeled by an integer  $Dl(u, v) \geq 1$  that we call the delay and which represents the number of time slots taken by a signal to go from  $u$  to  $v$  using this arc. Note that for any arc  $(u, v)$ ,  $Dl(u, v) = Dl(v, u)$ .

A **route**  $r$  in  $G$  is a sequence of consecutive arcs  $a_0, \dots, a_{k-1}$ , with  $a_i = (u_i, u_{i+1}) \in A$ .

The **latency** of a vertex  $u_i$  in  $r$ , with  $i \geq 1$ , is defined by

$$\lambda(u_i, r) = \sum_{0 \leq j < i} Dl(a_j)$$

We also define  $\lambda(u_0, r) = 0$ . The latency of the route  $r$  is defined by  $\lambda(r) = \lambda(u_k, r)$ .

A **routing function**  $\mathcal{R}$  in  $G$  associates to each pair of vertices  $(u, v)$  a route from  $u$  to  $v$ . Let  $\mathcal{C}$  be an **assignment** in  $G$ , i.e., a set of couples of different vertices of  $G$ . We denote by  $\mathcal{R}_{\mathcal{C}}$  the set of routes  $\mathcal{R}(u, v)$  for any  $(u, v)$  in  $\mathcal{C}$ . **TODO: Est-ce qu'on doit ajouter que le routage est cohérent ?**

## 2.2 Slotted time Model

Consider now a positive integer  $P$  called the **period**. A  $P$ -**periodic affectation** of  $\mathcal{R}_C$  consists in a set  $\mathcal{M} = (m_0, \dots, m_{c-1})$  of  $c$  integers that we call **offsets**, with  $c$  the cardinal of  $\mathcal{C}$ . In our problem the messages we send in the network will be periodic of period  $P$  and thus we consider slices of time of  $P$  slots. The number  $m_i$  represents the number of the first slot used by the route  $r_i \in \mathcal{R}_C$  at its source in a period. We define the first time slot at which a message reaches any vertex  $v$  in this route by

$$t(v, r_i) = m_i + \lambda(v, r_i) \mod P.$$

A message usually cannot be transported in a single time slot. We denote by  $\tau$  the number of slots necessary to transmit a message. Let us call  $[t(v, r_i)]$  the index of the time slots used by a route  $r_i$  at a vertex  $v$  in a period  $P$ . Those values are forming a consecutive set of values starting at  $t(v, r_i)$  and ending at  $t(v, r_i) + \tau \mod P$ . A  $P$ -periodic affectation must have no **collision** between two routes in  $\mathcal{R}_C$ , that is  $\forall (r_i, r_j) \in \mathcal{R}_C^2, i \neq j$ , we have

$$[t(u, r_i)] \cap [t(u, r_j)] = \emptyset.$$

## 2.3 Problems

**TODO: Mettre une phrase ou deux pour faire le lien avec le problème concret, plus facile faire une fois l'intro écrite** The main theoretical problem we have to deal with in this context is the following.

### Problem Periodic Routes Assignment (PRA)

**Input:** a graph  $G = (V, A)$ , a set  $\mathcal{C}$  of pair of vertices, a routing function  $\mathcal{R}$  and an integer  $P$ .

**Question:** does there exist a  $P$ -periodic affectation of  $\mathcal{C}$  in  $(G, \mathcal{R})$ ?

We deal in next section with the complexity of the Problem PRA.

In the context of cloud-RAN applications, we consider here the digraph  $G = (V, A)$  modeling the target network and two disjoint subsets of vertices  $S$  and  $L$ , where  $S$  is the set of BBU and  $L$  is the set of RRH. We denote by  $n$  the size of  $S$  and  $L$ . We are given a period  $P$ , a routing function  $\mathcal{R}$  and a bijection  $\rho : L \rightarrow S$  which defines two disjoint assignments  $\mathcal{C}_1 = \{(l, \rho(l))\}_{l \in L}$  and  $\mathcal{C}_2 = \{(s, \rho^{-1}(s))\}_{s \in S}$ . Let  $\mathcal{M} = (m_1, \dots, m_n)$  and  $\mathcal{W} = (w_1, \dots, w_n)$  be two  $P$ -periodic affectations, of respectively  $\mathcal{R}_{\mathcal{C}_1}$  and  $\mathcal{R}_{\mathcal{C}_2}$ .

The process realized periodically (i.e. initiated in each window of size  $P$ ) for each leaf  $l \in L$  is the following one (see Figure ??). First, a message of  $\tau$  slots is sent from  $l$  to  $\rho(l)$  on  $\mathcal{R}(l, \rho(l))$  at slot  $m_l$  in the current window. After receiving this message,  $\rho(l)$  computes it during a time equal to  $\theta$  slots. **TODO: Je suis contre le theta dans le modèle, car il ne set à rien. On peut dire par contre dans le blabla autour du modèle qu'on simule le temps de calcul par des arêtes plus longues**

Then, a message of  $\tau$  slots containing the computed result is sent back from  $\rho(l)$  to  $l$  on  $\mathcal{R}(\rho(l), l)$ , after waiting for  $w_l$  slots. Thus, the whole process time for  $l$  is equal to

$$PT(l) = \lambda(\mathcal{R}(l, \rho(l))) + \theta + w_l + \lambda(\mathcal{R}(\rho(l), l)).$$

**TODO:** Il manque le fait qu'il n'y a pas de collisions ni à l'aller ni au retour.

The **maximum process time** of  $(\mathcal{M}, \mathcal{W})$  is defined by  $MT((\mathcal{M}, \mathcal{W})) = \max_{l \in L} PT(l)$ . The problem we want to solve, is the following.

#### Problem Periodic Assignment for Low Latency(PALL)

**Input:** a digraph  $G$ , a matching  $\rho$  of a set  $S$  into a set  $L$  in  $G$ , a routing function  $\mathcal{R}$ , a period  $P$ , an integer  $T_{max}$ .

**Question:** does there exist a pair of  $(\mathcal{M}, \mathcal{W})$   $P$ -periodic affectation  $\mathcal{M}$  of  $\mathcal{C}_\rho$  in  $(G, \mathcal{R})$  such that  $MT(\mathcal{M}) \leq T_{max}$ ?

## 3 PRA Solving

### 3.1 NP-Hardness

**TODO:** Definition of the load. La preuve se réfère à la précédente qui n'a pas été retenue, il faut du coup tout expliquer.

**Theorem 1.** *Problem PRA cannot be approximated within a factor  $n^{1-o(1)}$  unless  $P = NP$  even when the load is two and  $n$  is the number of pairs in the assignment.*

*Proof.* We reduce PRA to graph coloring. Let  $G$  be a graph instance of the  $k$ -coloring problem. We define  $H$  in the following way: for each vertex  $v$  in  $G$ , there is a route  $r_v$  in  $H$ . Two routes  $r_v$  and  $r_u$  share an edge if and only if  $(u, v)$  is an edge in  $G$  and this edge is only in this two routes. We put a weight inbetween shared edges in a route so that there is a delay  $k$  between two such edges.

As in the previous proof, a  $k$ -coloring of  $G$  gives a  $k$ -periodic schedule of  $H$  and conversly. Therefore if we can approximate the value of PRA within a factor  $f$ , we could approximate the minimal number of colors needed to color a graph within a factor  $f$ , by doing the previous reduction for all possible  $k$ . The proof follows from the hardness of approximability of finding a minimal coloring [?].  $\square$

### 3.2 MIN-PRA

Exemple de cas simple

## 4 Proposed Solutions, solving PALL

In this section, we consider a particular case of the model, in which for each  $(u, v)$ , the route is the same in both directions. This means that  $\mathcal{R}(u, v)$  uses the same arcs as  $\mathcal{R}(v, u)$  in the opposite orientation.

## 4.1 Intro

PALL NP-Hard car PRA NP-Hard

Résultats valables sur Topologie 1 avec nos paramètres **TODO: J'ai viré star affectation, car je pense qu'il n'y a rien à dire là dessus.**

## 4.2 No waiting times

### 4.2.1 Shortest-longest

Algo

Period

### 4.2.2 Exhaustive generation

Décrire l'algo, expliquer les coupes

### 4.2.3 Results

Resultats des simulations : Shortest-longest optimal pour ces parametres.

## 4.3 Allowing waiting times

### 4.3.1 Intro

Importance des waiting times quand la période est donnée (Résultats D'expériences et preuve avec l'exemple)

### 4.3.2 LSG

Algorithm

**Analysis** Parler de LSO et expliquer pourquoi LSG mieux avec nos params

### 4.3.3 Results

Random

Distributions

## 5 Conclusion