

અધ્યાય - ૭

દ્વિપદ પ્રમેય

(Binomial Theorem)

Formulas →

$$(i) (a+b)^n = {}^nC_0 a^n + {}^nC_1 a^{n-1} b + {}^nC_2 a^{n-2} b^2 + {}^nC_3 a^{n-3} b^3 + \dots + {}^nC_n b^n$$

$$(ii) (a-b)^n = {}^nC_0 a^n - {}^nC_1 a^{n-1} b + {}^nC_2 a^{n-2} b^2 - {}^nC_3 a^{n-3} b^3 + \dots - {}^nC_n b^n$$

$$(iii) (a+b)^n = \sum_{r=0}^n {}^nC_r a^{n-r} b^r$$

$$(iv) (a+b)^n - (a-b)^n = 2({}^nC_1 a^{n-1} b + {}^nC_3 a^{n-3} b^3 + {}^nC_5 a^{n-5} b^5 + \dots)$$

$$(v) (a+b)^n + (a-b)^n = 2({}^nC_0 a^n + {}^nC_2 a^{n-2} b^2 + {}^nC_4 a^{n-4} b^4 + \dots)$$

$$(vi) (1+x)^n = {}^nC_0 + {}^nC_1 x + {}^nC_2 x^2 + {}^nC_3 x^3 + \dots$$

$$(vii) (1-x)^n = {}^nC_0 - {}^nC_1 x + {}^nC_2 x^2 - {}^nC_3 x^3 + \dots$$

$$(viii) (a-b)^n = \sum_{r=0}^n (-1)^r {}^nC_r a^{n-r} b^r$$

$${}^nC_0 = 1$$

$${}^nC_n = 1$$

$${}^nC_1 = n$$

$${}^nC_2 = \frac{n(n-1)}{2!}$$

$${}^nC_3 = \frac{n(n-1)(n-2)}{3!}$$

$${}^nC_4 = \frac{n(n-1)(n-2)(n-3)}{4!}$$