Model Predictive Control in Adaptive Cruise Control

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Abstract

This paper presents a method of using MPC into Adaptive Cruise Control (ACC). The MPC is a powerful tool for solving the optimal control problem. We present a linear model of the system.

1 Problem Discreption

Adaptive Cruise Control (ACC) is a driver assistance system that helps maintain a safe distance from the vehicle in front, especially in heavy traffic or on long trips. With the advancement of commercial radar, lidar, and camera technologies, the popularity of ACC systems has increased.

Although Model Predictive Control (MPC) [1] is a popular method for solving the ACC problem, it still presents challenges due to the computational load involved in solving large-scale optimization problems. Therefore, this paper proposes a method to linearize the ACC system model and use the powerful CasADi toolbox[2] for solving the optimal control problem.

2 Formulation

2.1 ACC system

In this paper, there are three parameters that can be measured as below by the ACC system:

- Δd : Inter-vehicle distance following error, it represents the error between the desired inter-vehicle distance d_r and actual inter-vehicle distance d. st. $\Delta d = d d_r$. It's supposed to converge to zero if the ACC system works well.
- Δv : The speed following error, it represents the speed error between the host vehicle speed v_h and target vehicle speed v_r . st. $\Delta v = v_h v_r$. It's supposed to converge to zero.
- $\dot{v_h}$: the acceleration of the host vehicle. It's supposed to converge to be zero if target vehicle speed v_r is constant. Because it's a simple linear model, we suppose the velocity of the target vehicle is constant.

2.2 Vehicle Dynamics

A vehicle dynamics model[3] will be used to describe the vehicle dynamics and to build the MPC. The logitudinal dynamics of the host vehicle is given by (2.1):

$$m\dot{v_h} = F_f - r_{travel} \tag{2.1}$$

where m is the mass of the host vehicle, F_f is the total traction force of the host vehicle, r_{travel} is the rolling resistance of the host vehicle. The input/output relationship of the vehicle dynamics model is given by the differential equation (2.2):

$$\begin{cases} \dot{x}_f = f_{act}(x_f, u) \\ a_f = h_{act}(x_f) \end{cases}$$
 (2.2)

where $x_f = \mathbb{R}^{n_f}$ is the state of the vehicle dynamics model, u is the input of the vehicle system (2.2) which is often a control input calculated by embedde micro cruise controller. r_{travel} is travel resistance which can be calculated by the following equation (2.3):

$$r_{travel} = r_{air}v_h^2 + r_{roll}(v_h) + r_{accel}\dot{v_h} + r_{arad}(\theta)$$
(2.3)

where r_{air} is the air resistance coefficient, r_{roll} is the rolling resistance, the r_{accel} is the acceleration resistance coefficient, r_{grad} is the gradient resistance, θ is the slope angle.

2.3 State-Space Model for ACC System

To construct a plant model of the Adaptive Cruise Control (ACC) system, it is necessary to consider both the desired inter-vehicle distance d_r and the minimum inter-vehicle distance d_0 .

$$d_r = T_{hw}v_h + d_0 (2.4)$$

where T_{hw} is the headway time, d_0 is the minimum inter-vehicle distance.

In this paper, the state variables of the ACC system are as $x = [\Delta d, \Delta v, x_f^T]^T$, $x \in \mathbb{R}^{2+n_f}$, the state-space model is formulated as (2.5):

$$\begin{cases} \dot{x} = f_{act}(x, u) + Gv + Hw \\ y = Cx + Jv \end{cases}$$
 (2.5)

where
$$f_{act}(x, u) = \begin{bmatrix} \Delta v - T_{hw} x_f \\ -h_{act}(x_f) \\ f_{act}(x_f, u) \end{bmatrix}$$
, $G = \begin{bmatrix} T_{hw}/m \\ 1/m \\ 0 \end{bmatrix}$, $H = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$, $C = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$, $J = \begin{bmatrix} 0 \\ 0 \\ -1/m \end{bmatrix}$.

where $u \in \mathbb{R}$ is the input of the plant and $y = [\Delta d, \Delta v, v_h]^T \in \mathbb{R}^3$ is the output of the plant.

3 Optimal-based Control Method

3.1 Controller Model Design

In order to reduce the computational cost, the ACC system model is linearized as (3.1):

$$\begin{cases}
\dot{a_f} = A_f(t)a_f + B_f(t)u \\
a_f = C_f x_f
\end{cases}$$
(3.1)

where the acceleration of the linearized model is $a_f \in \mathbb{R}$, the input of the linearized model is u, the output of the linearized model is a_f and $A_f(t)$, $B_f(t)$, C_f are shown as (3.2):

$$A_{f}(t) = \begin{cases} -\frac{1}{T_{eng}}, & \text{if } u(t) \ge a_{thr-off} \\ -\frac{1}{T_{brk}}, & \text{if } u(t) < a_{thr-off} \end{cases}$$

$$B_{f}(t) = \begin{cases} \frac{K_{eng}(t)}{T_{eng}}, & \text{if } u(t) \ge a_{thr-off} \\ \frac{K_{brk}(t)}{T_{brk}}, & \text{if } u(t) < a_{thr-off} \end{cases}$$

$$C_{f} = 1.$$

$$(3.2)$$

where T_{eng} is the constant of acceleration of acceleration engine, T_{brk} is time constant of deceleration using brake, a_{thr_off} is the threshold of acceleration, $K_{eng}(t)$ and $K_{brk}(t)$ are the gain of acceleration engine and brake respectively.

In the system (3.1), the dynamics of the vehicle is simplified as a first-order delay system. The system has two modes:a acceleration mode and a deceleration mode.

So the prediction model (2.5) can be simplified as (3.3).

$$\begin{cases} \dot{x} = A(t)x + B(t)u + Gv + Hw \\ y = Cx + Jv \end{cases}$$
 (3.3)

where
$$x \in \mathbb{R}^3$$
 and $A(t) = \begin{bmatrix} 0 & 1 & -T_{hw} \\ 0 & 0 & -1 \\ 0 & 0 & A_f(t) \end{bmatrix}$, $B(t) = \begin{bmatrix} 0 \\ 0 \\ B_f(t) \end{bmatrix}$.

3.2 Optimization Problem

4 Preliminary Results

5 Conclusion

In this paper, we proposed a MPC controller for ACC system.

References

- [1] J Rawlings and D Mayne. Postface to model predictive control: Theory and design. *Nob Hill Pub*, 5:155–158, 2012.
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- [3] Taku Takahama and Daisuke Akasaka. Model predictive control approach to design practical adaptive cruise control for traffic jam. *International Journal of Automotive Engineering*, 9(3):99–104, 2018.