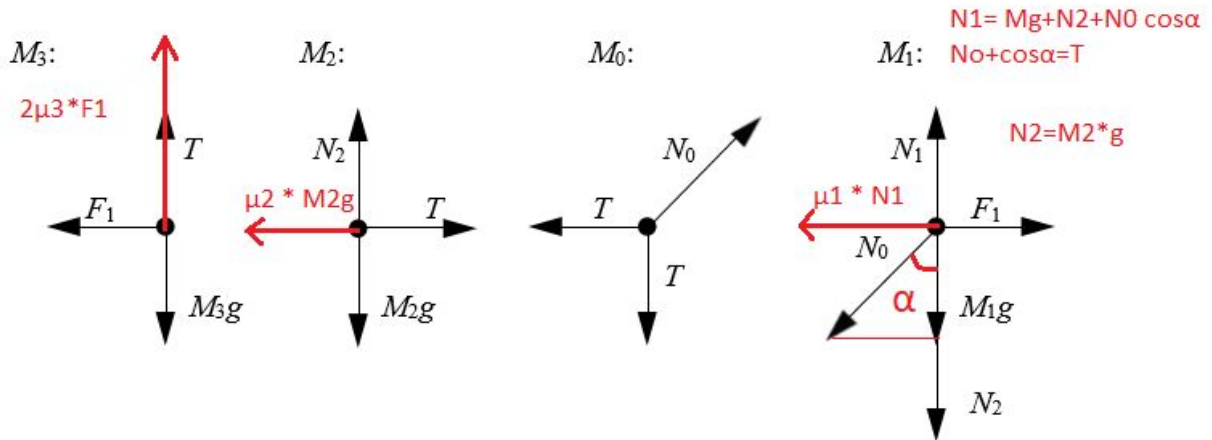


Margarita Zargaryan

Project 2 , explanation of the results used in coding part



Constraint 1: Lrope = Lhorizontal + Lvertical = $x_1 - x_2 + y_1 - y_3 = \text{const}$

$$x_1'' - x_2'' + y_1'' - y_3'' = a_1 - a_2 - a_3 y = 0$$

Constraint 2: M₃ cannot leave the hole in M₁ $x_1 = x_3$ $x_1'' = x_3''$ $a_1 = a_3 x$

For M₁ in x : $F_1 - T - \mu_1 M_1 g - \mu_1 M_1 g + \mu_1 T = M_1 a_1$

For M₂ in x : $T - \mu_2 M_2 g = M_2 a_2$

M₃ in x: $-F_1 = M_3 a(3x)$

M₃ in y: $T - M_3 g + 2 \mu_3 F_1 = M_3 (a_1 - a_2)$

M₀ in x : $N_0 x - T = M_0 a_0 = 0$

$$a_1 - a_2 - a_3 y = 0$$

$$a_1 = a_3 x$$

$$-M_3 a_1 - M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 (M_2 a_2 + \mu_2 M_2 g) = M_1 a_1$$

$$a_1 (M_1 + M_3) = -M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 M_2 a_2 + \mu_1 \mu_2 M_2 g$$

$$a_1 = (-M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 M_2 a_2 + \mu_1 \mu_2 M_2 g) / (M_1 + M_2)$$

$$M_2 a_2 + \mu_2 M_2 g - M_3 g + 2 \mu_3 F_1 = M_3 (a_1 - a_2)$$

$$M_2 a_2 + \mu_2 M_2 g - M_3 g + 2 \mu_3 F_1 = M_3 ((-M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 M_2 a_2 + \mu_1 \mu_2 M_2 g) / (M_1 + M_2) - a_2)$$

$$M_2 a_2 + \mu_2 M_2 g - M_3 g + 2 \mu_3 F_1 = M_3 ((-M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 M_2 a_2 + \mu_1 \mu_2 M_2 g) / (M_1 + M_3) - M_1 a_2 - M_3 a_2) / (M_1 + M_3)$$

$$(M_1 + M_3) (M_2 a_2 + \mu_2 M_2 g - M_3 g + 2 \mu_3 F_1) = M_3 (-M_2 a_2 + \mu_2 M_2 g - \mu_1 M_1 g + \mu_1 M_2 a_2$$

$$+\mu_1\mu_2M_2g - M_1a_2-M_3a_2)$$

$$a_2^*M_2^*(M_1+M_3)+(M_1+M_3)(\mu_2^*M_2^*g-M_3^*g+2^*\mu_3^*F_1)=a_2^*M_3^*(-M_2+\mu_1^*M_2-M_1-M_3) \\ +M_3^*(\mu_2^*M_2^*g-\mu_1^*M_1^*g+\mu_1^*\mu_2^*M_2^*g)$$

$$a_2^*(M_2^*(M_1+M_3)-M_3^*(-M_2+\mu_1^*M_2-M_1-M_3))=-(M_1+M_3)^*(\mu_2^*M_2^*g-M_3^*g+2^*\mu_3^*F_1)+ \\ M_3^*(\mu_2^*M_2^*g-\mu_1^*M_1^*g+\mu_1^*\mu_2^*M_2^*g)$$

$$a_2^*=(-(M_1+M_3)^*(\mu_2^*M_2^*g-M_3^*g+2^*\mu_3^*F_1)+M_3^*(\mu_2^*M_2^*g-\mu_1^*M_1^*g+\mu_1^*\mu_2^*M_2^*g))/ \\ (M_2^*(M_1+M_3)-M_3^*(-M_2+\mu_1^*M_2-M_1-M_3))$$

$$\text{As } x(t) = x_0 + v_0t + \frac{1}{2} (a^* t^2)$$

$$\text{As starting from position 0 , with 0 velocity } \Rightarrow x(t) = \frac{1}{2} (a^* t^2)$$